



Institute of High Energy Physics, CAS

Reactor antineutrino anomaly in light of recent flux model refinements

Z. Xin (IHEP, Beijing)

May 08, 2024

Based on [C. Giunti, Y. F. Li, C. A. Ternes, **ZX**, Phys.Lett.B 829 \(2022\) 137054](#)

And [Y. F. Li, **ZX**, Phys.Rev.D 105 \(2022\) 7, 073003](#)

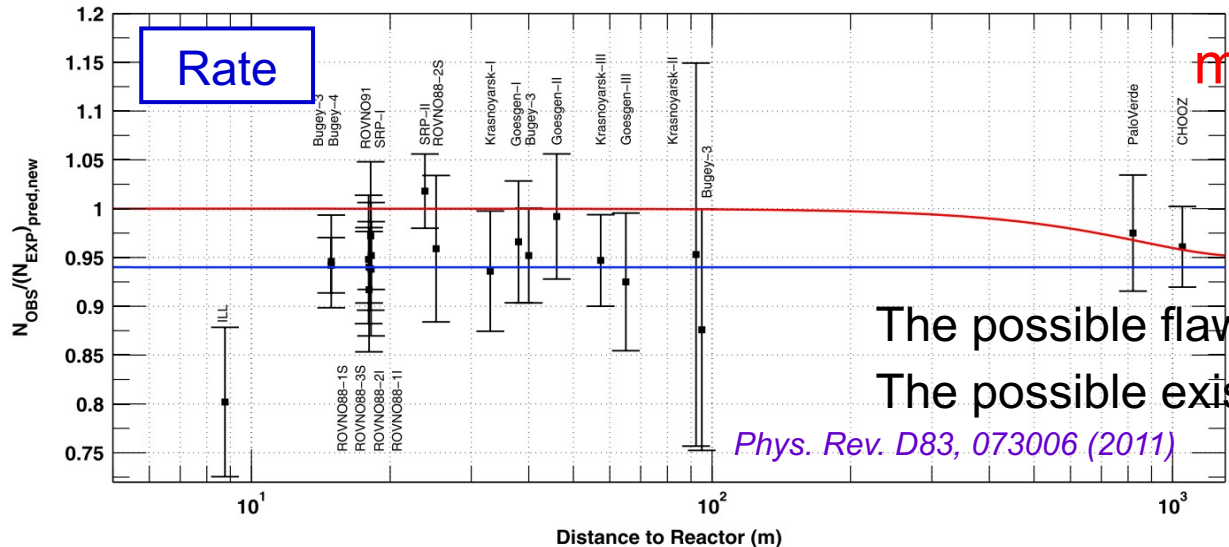
Conference on frontiers of underground and space particle physics and cosmophysics

Parallel Talk



Reactor antineutrino anomaly

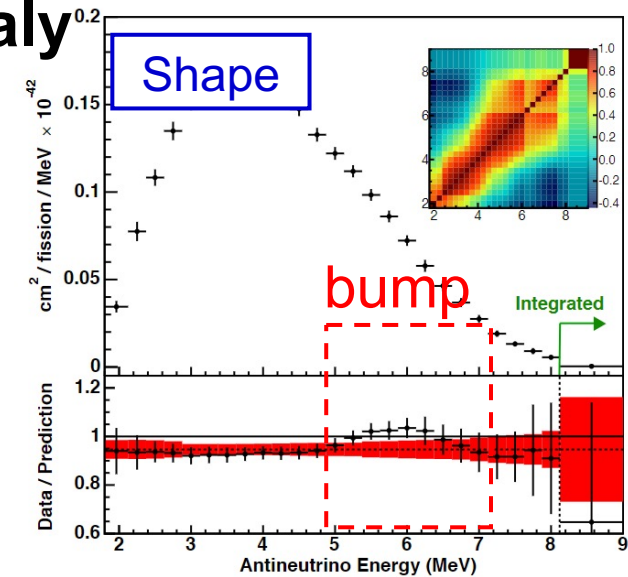
- Huber-Mueller model and Reactor antineutrino anomaly



mean averaged ratio:
 $\bar{R} = 0.943 \pm 0.024 (2.4 \sigma)$

The possible flaw of HM (and other models)
 The possible existence of light sterile neutrinos

Phys. Rev. D83, 073006 (2011)



Y. F. Li, ZX, Phys.Rev.D 105 (2022) 7, 073003
Data-driven Flux model ?

- Reactor data to test RAA for different models

Models → Best one ?

C. Giunti, Y. F. Li, C. A. Ternes, ZX, Phys.Lett.B 829 (2022) 137054

- Huber-Mueller model
- Hayen-Kostensalo-Severijns-Suhonen model
- Recent Kurchatov Institute measurements
 - HM → KI model
 - HKSS → HKSS-KI model
- Estienne-Fallot summation model

Reactor data

- Reactor rates data (27)
 - 80s-90s, 2000s, 2010s
 - Recent Prospect & STEREO
- Fuel evolution data (8+8)
 - Daya Bay
 - RENO

Reactor flux models: Huber-Mueller model



- How to predict reactor antineutrino spectra

- Conversion method

Measured β spectra \rightarrow neutrino spectra

- Summation method

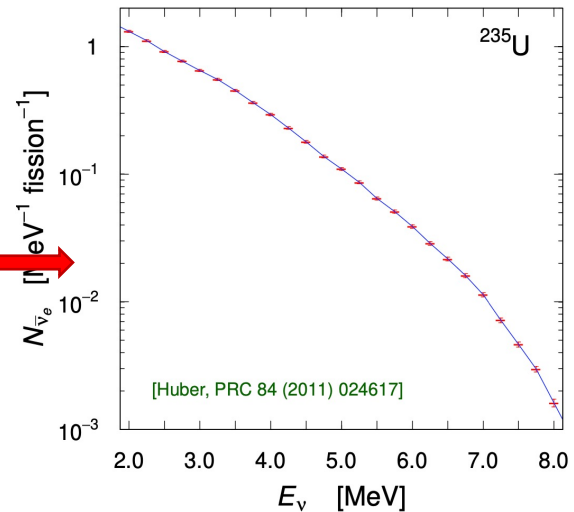
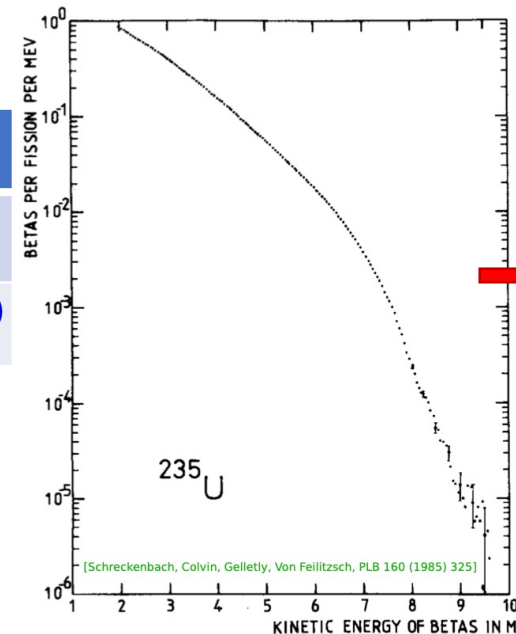
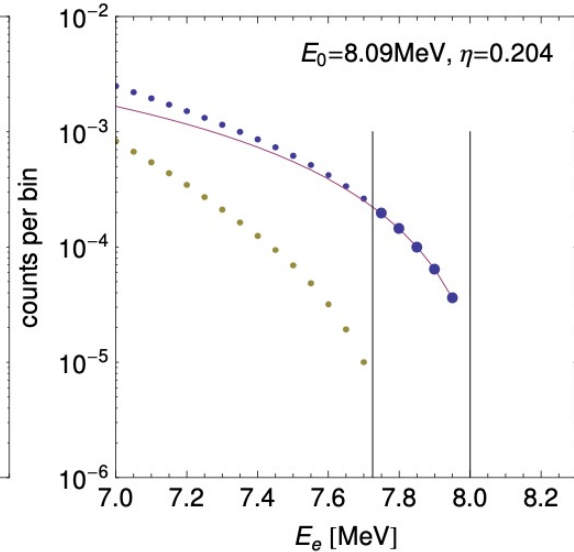
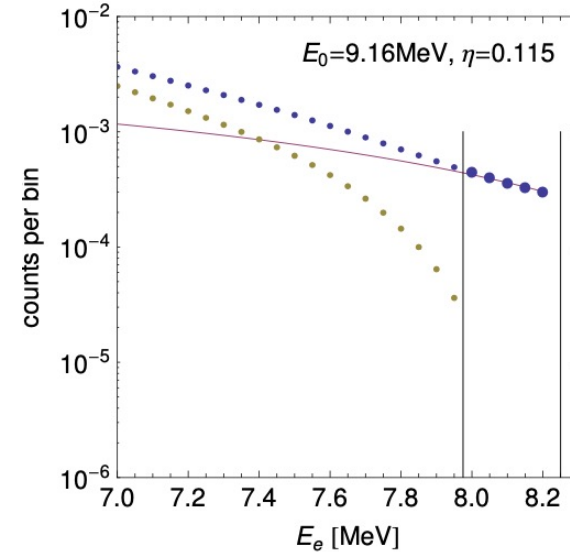
Sum of all the decay branches \leftarrow database

- Huber-Mueller model

^{235}U	^{239}Pu	^{241}Pu	^{238}U
ILL measurement \rightarrow neutrino spectra			Summation method
<i>Phys. Rev. C 85, 029901 (2012)</i>			<i>Phys. Rev. C 83, 054615 (2011)</i>

Only allowed transitions are considered in HM model.

How to convert ILL into neutrino spectra



Corrections to HM model



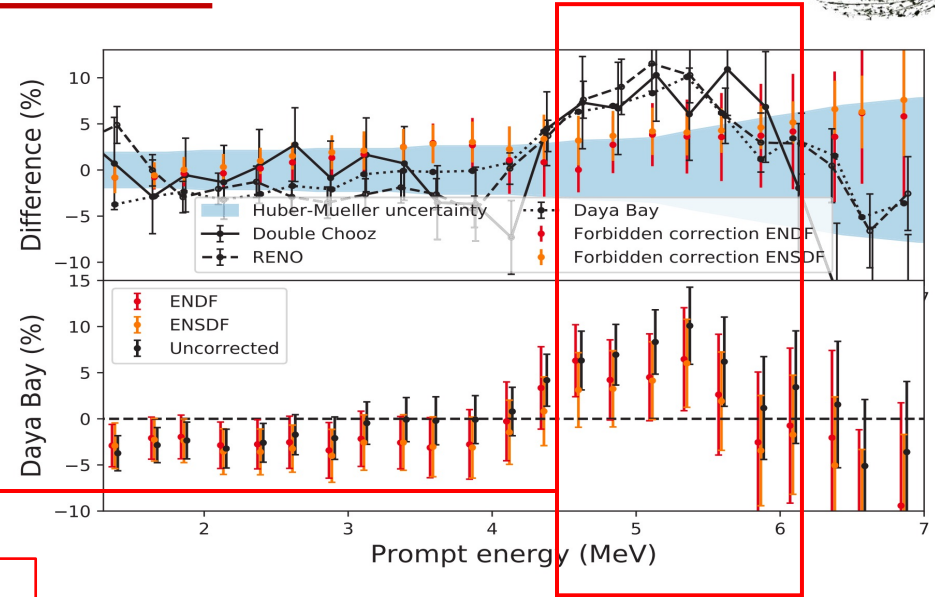
• HKSS model

Shape correction

HM model + Forbidden transitions (some branches)

235U	239Pu	241Pu	238U
ILL measurement → neutrino spectra			Summation method
<i>Phys. Rev. C 100, no.5, 054323 (2019)</i>			

Partially explain the '5 MeV Bump' ←

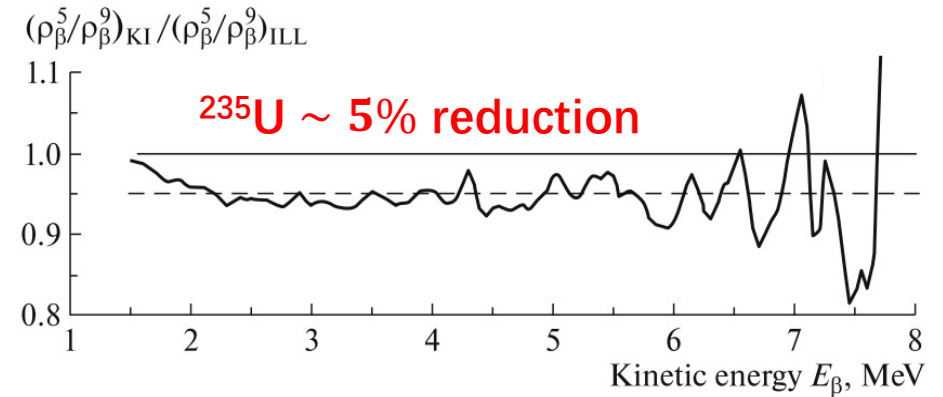


• Kurchatov Institute measurement

Rate correction

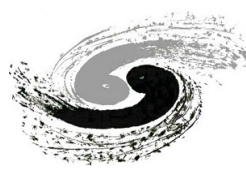
- Ratio of beta spectra: $(S_{\beta}^5/S_{\beta}^9)_{ILL} > (S_{\beta}^5/S_{\beta}^9)_{KI}$
- HM model → KI model *Phys. Rev. D 104 (2021) L071301*
- HKSS model → HKSS-KI model

	235U	238U	239, 241Pu
KI	KI measurement	Garching measurement	ILL measurement
HKSS-KI	KI measurement	Summation method	ILL measurement



Phys. Atom. Nucl. 84, no.1, 1-10 (2021)

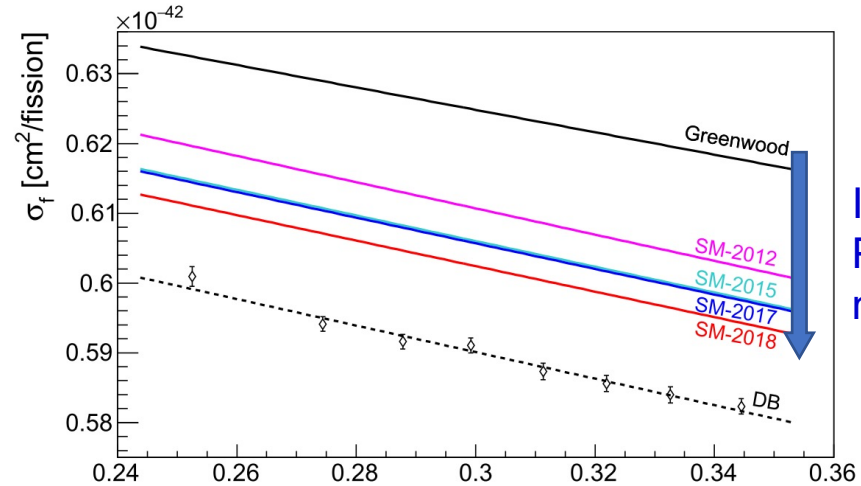
Reactor flux models: summation model



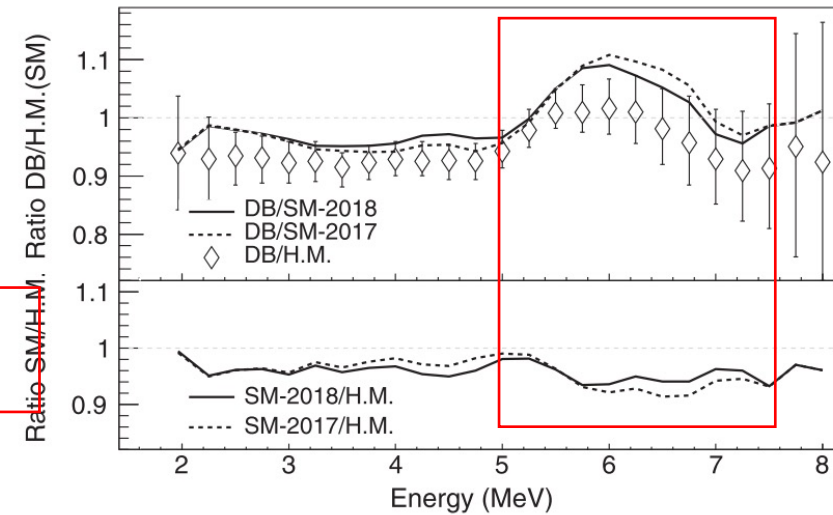
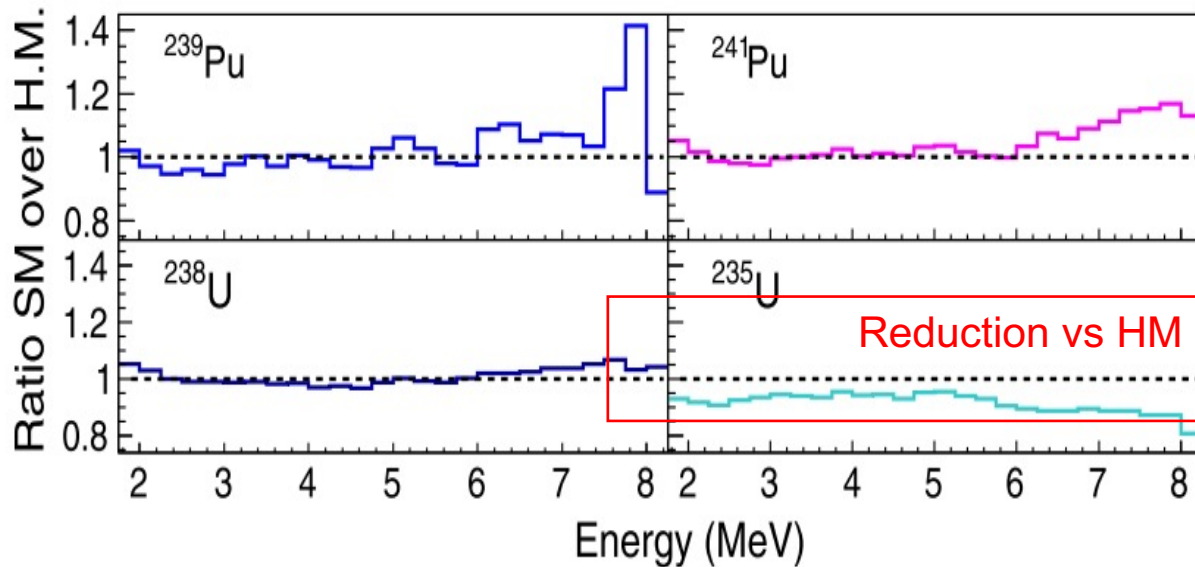
- Estienne-Fallot summation model

Phys. Rev. Lett. 123, no. 2, 022502 (2019)

- Summation method
- Nuclear data
 - Pandemonium-free data
 - ENSDF nuclear database
 - JEFF and ENDF database
- Reduction in ^{235}U versus HM
- Bump anomaly still exists



Including more Pandemonium-free nuclear data



Bump anomaly

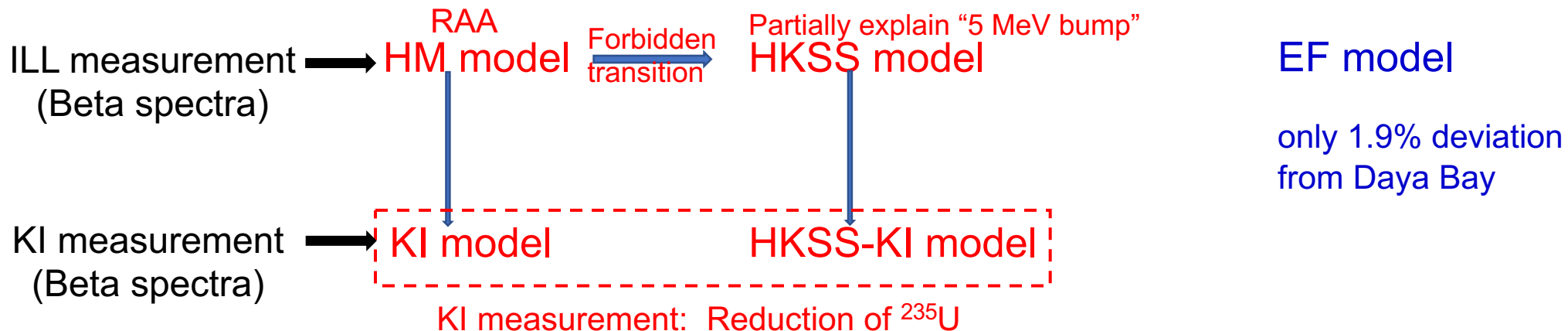
Reactor flux models: a brief summary



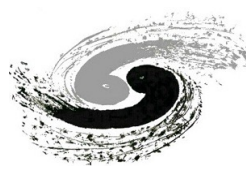
Models considered in this work Phys.Lett.B 829 (2022) 137054

Conversion model

Summation model



		^{235}U	^{238}U	$^{239, 241}\text{Pu}$
Conversion models	HM	ILL measurement	Summation method	ILL measurement
	HKSS	ILL measurement	Summation method	ILL measurement
	KI	KI measurement	Garching measurement	ILL measurement
	HKSS-KI	KI measurement	Summation method	ILL measurement
Summation models	EF	Summation method	Summation method	Summation method



IBD yields

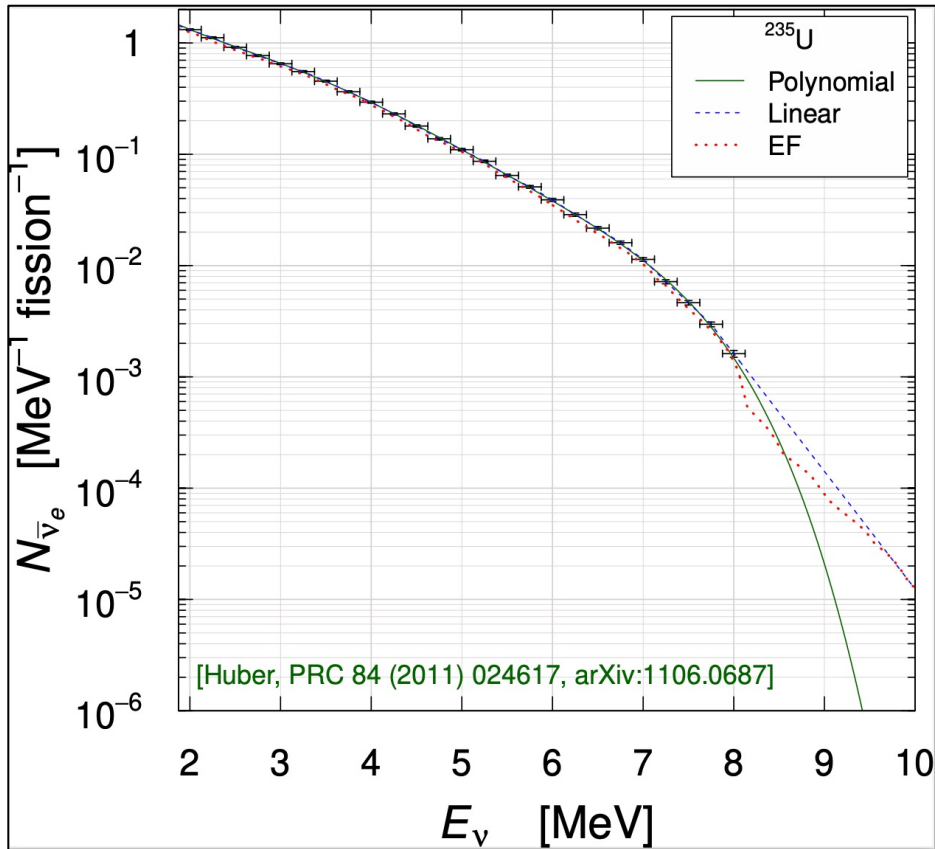
IBD yield → Reactor event rates

$$\sigma_i = \int_{E_{\min}}^{E_{\max}} dE \Phi_i(E) \sigma_{\text{IBD}}(E),$$

Phys. Lett. B 564 (2003) 42,

1. IBD cross section with radiative corrections
2. The high energy region

More details can be found in
C. Giunti, Y. F. Li, C. A. Ternes, ZX, Phys.Lett.B 829 (2022) 137054



Small contribution **above 8 MeV**:
 0.3% for ^{235}U , 0.9% for ^{238}U ,
 0.2% for ^{239}Pu , 0.3% for ^{241}Pu .

Model	σ_{235}	σ_{238}	σ_{239}	σ_{241}
HM	6.74 ± 0.17	10.19 ± 0.83	4.40 ± 0.13	6.10 ± 0.16
HKSS	6.82 ± 0.18	10.28 ± 0.84	4.42 ± 0.13	6.17 ± 0.16
KI	6.41 ± 0.14	9.53 ± 0.48	4.40 ± 0.13	6.10 ± 0.16
HKSS-KI	6.48 ± 0.14	10.28 ± 0.84	4.42 ± 0.13	6.17 ± 0.16
EF	6.29 ± 0.31	10.16 ± 1.02	4.42 ± 0.22	6.23 ± 0.31

Shape correction

σ_i 's ↑

σ_{235} ↓

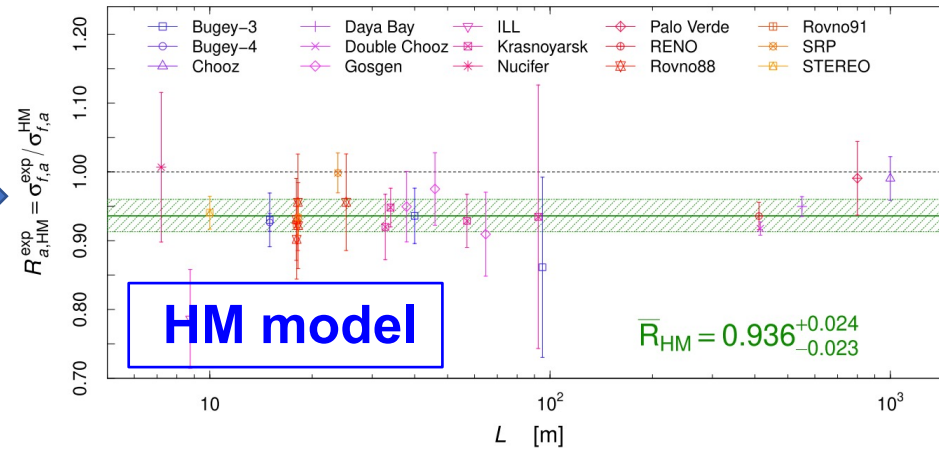
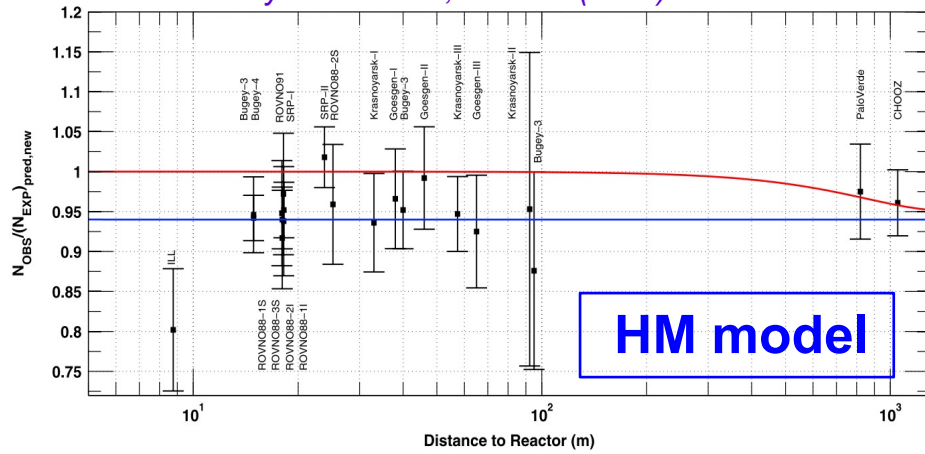
Rate correction

Fit of reactor rates

C. Giunti, Y. F. Li, C. A. Ternes, *ZX*,
Phys.Lett.B 829 (2022) 137054

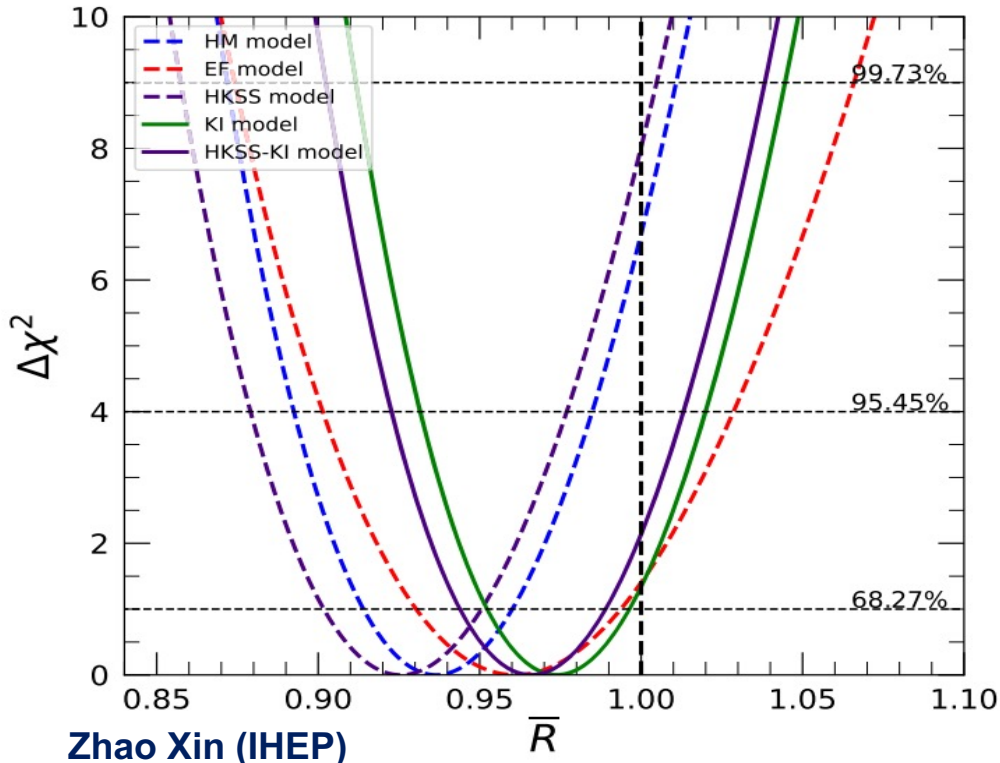


Phys. Rev. D 83, 073006 (2011)



RAA: 2.4 σ
 0.943 ± 0.024

 $0.936^{+0.024}_{-0.023}$
 RAA: 2.5 σ



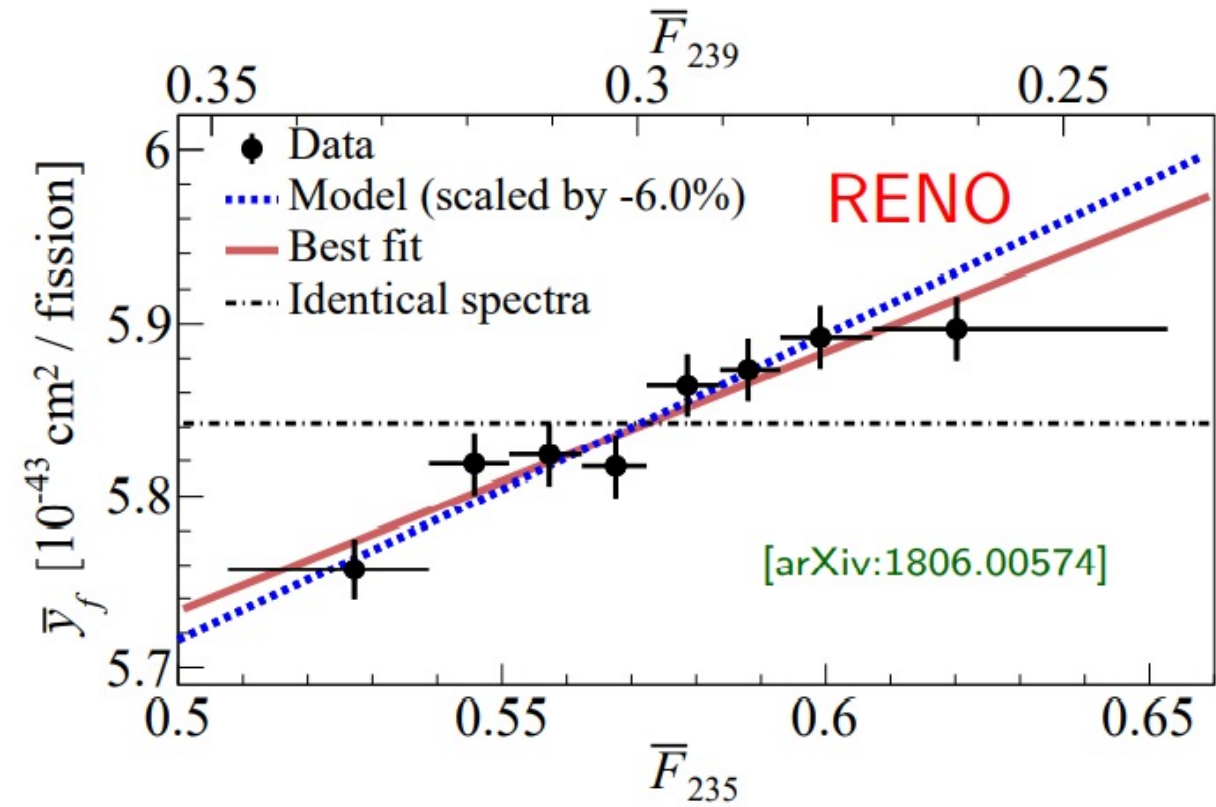
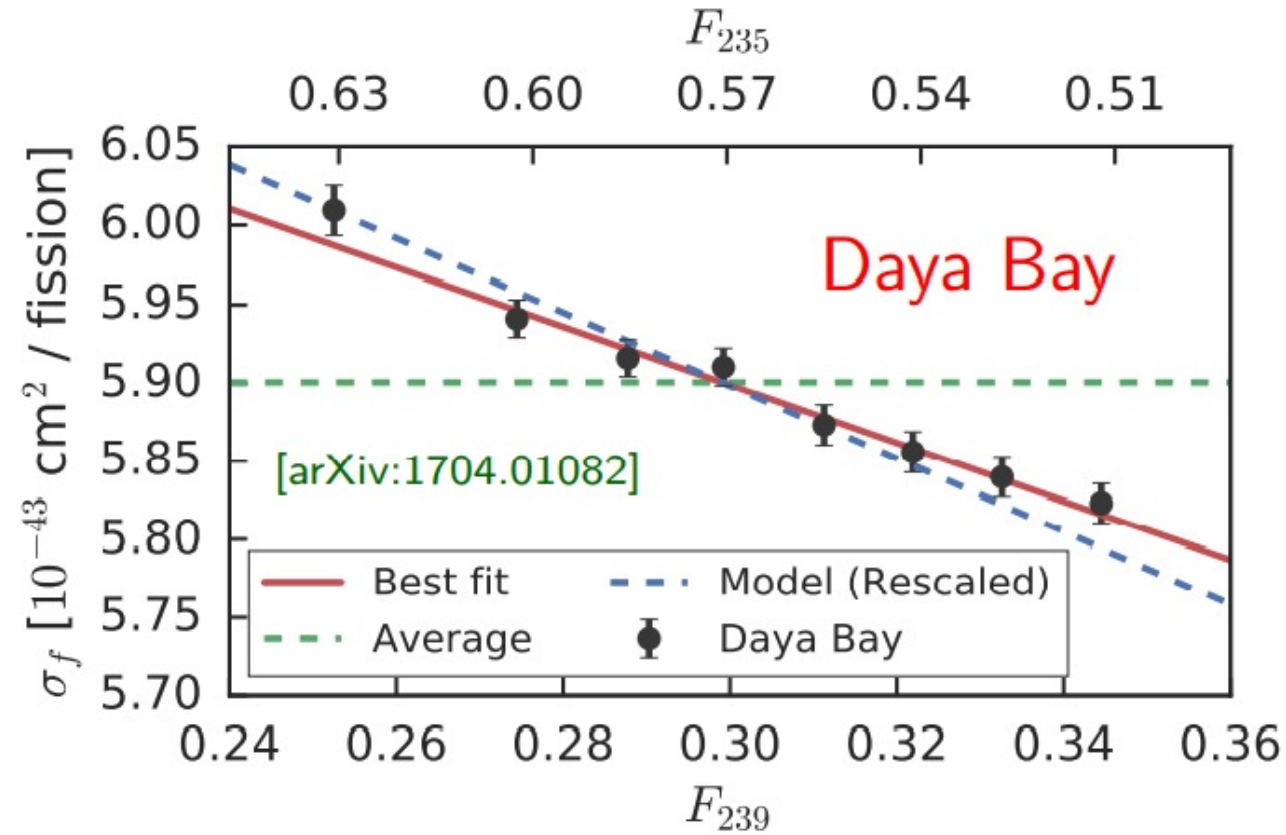
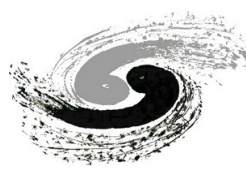
Model	\bar{R}	RAA
HM	$0.936^{+0.024}_{-0.023}$	2.5 σ
HKSS	$0.925^{+0.025}_{-0.023}$	2.9 σ
KI	$0.975^{+0.022}_{-0.021}$	1.1 σ
HKSS-KI	$0.964^{+0.023}_{-0.022}$	1.5 σ
EF	$0.960^{+0.033}_{-0.031}$	1.2 σ

Increase in σ_i 's enlarges RAA

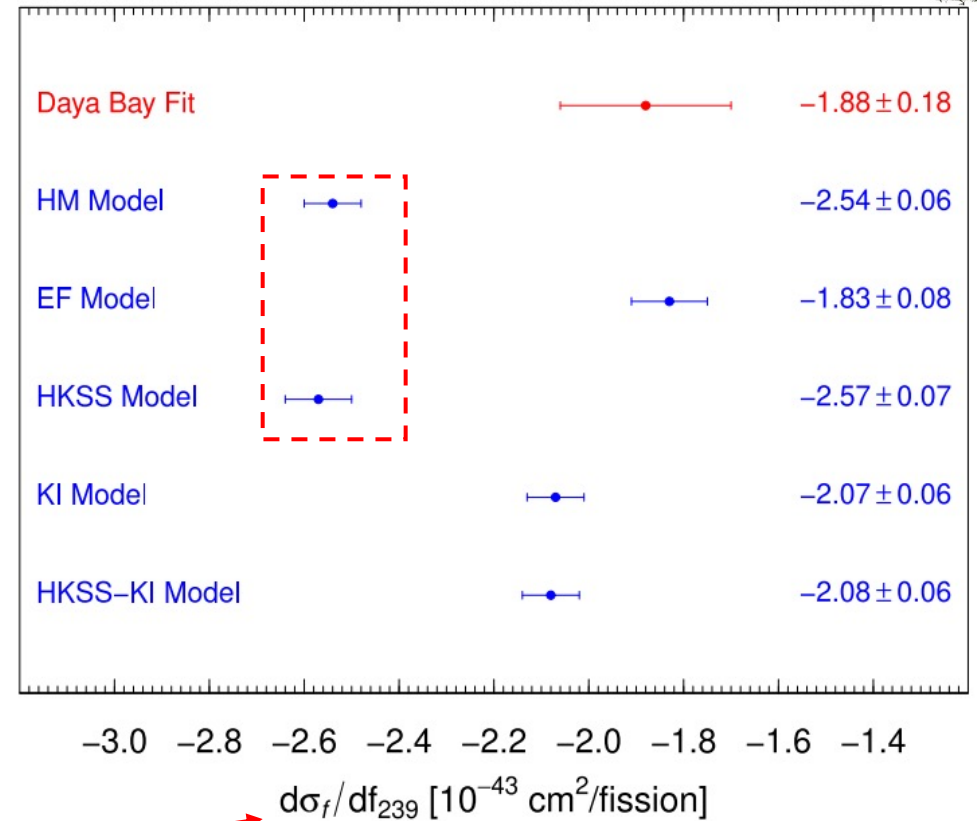
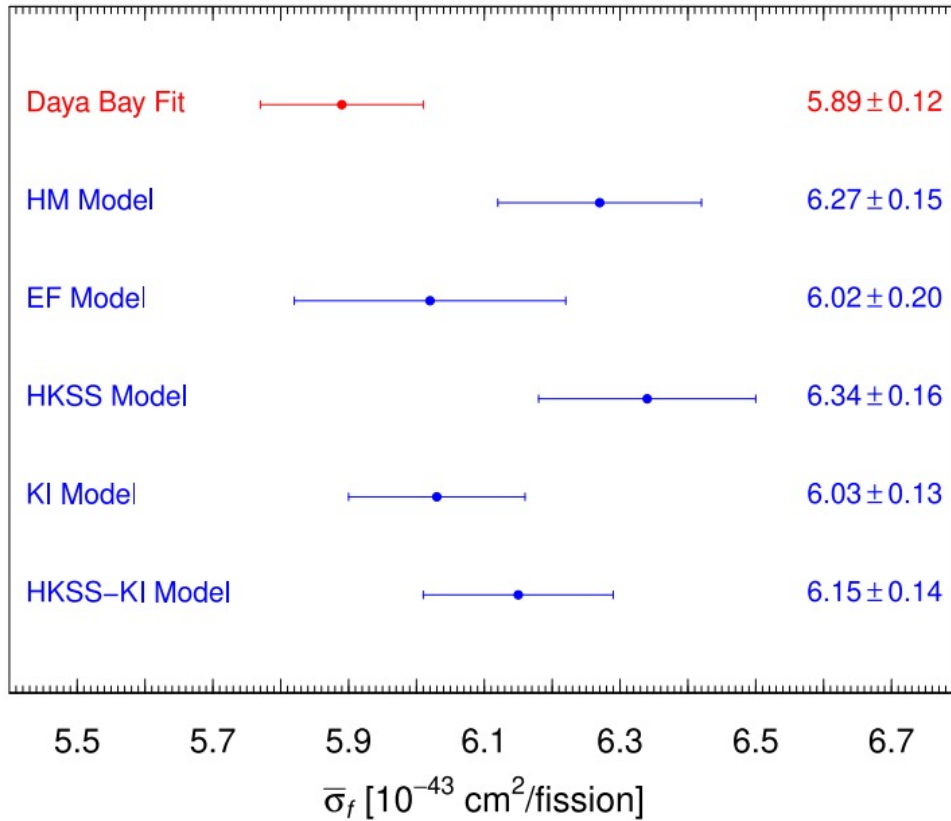
No RAA

Reduction in σ_{235} helps to decrease RAA

Data sets: evolution data



Fit of reactor fuel evolution data



A linear function $\sigma_{f,a}^{\text{lin}} = \bar{\sigma}_f + \frac{d\sigma_f}{df_{239}} (f_{239}^a - \bar{f}_{239})$

C. Giunti, Y. F. Li, C. A. Ternes, ZX,
Phys.Lett.B 829 (2022) 137054

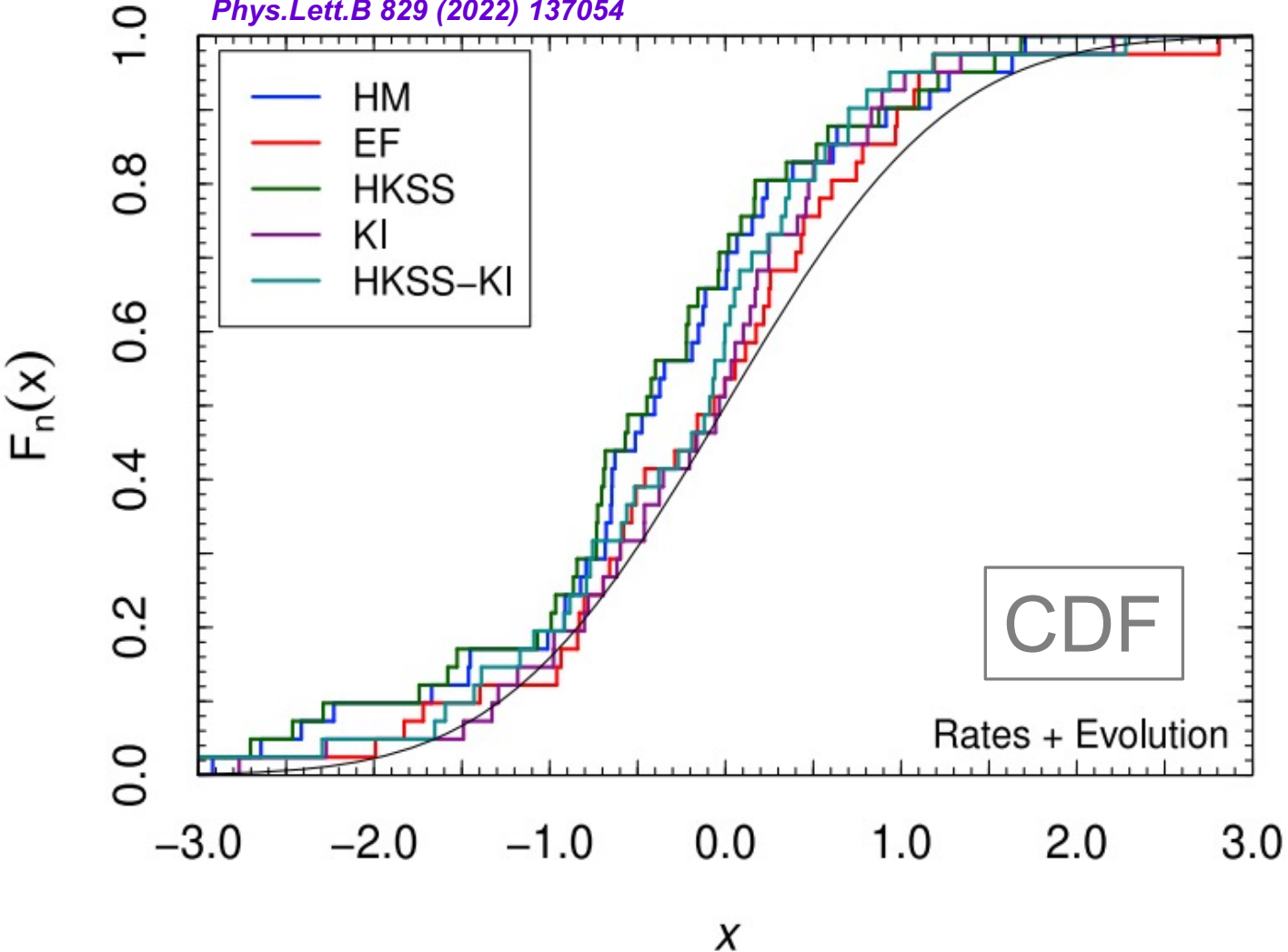
- EF, KI and HKSS-KI agree with evolution data
 - 3.5 σ for HM model
 - 3.6 σ for HKSS model
- HM and HKSS are disfavored.**

RENO evolution data \rightarrow similar results



Statistic test

C. Giunti, Y. F. Li, C. A. Ternes, ZX,
Phys.Lett.B 829 (2022) 137054

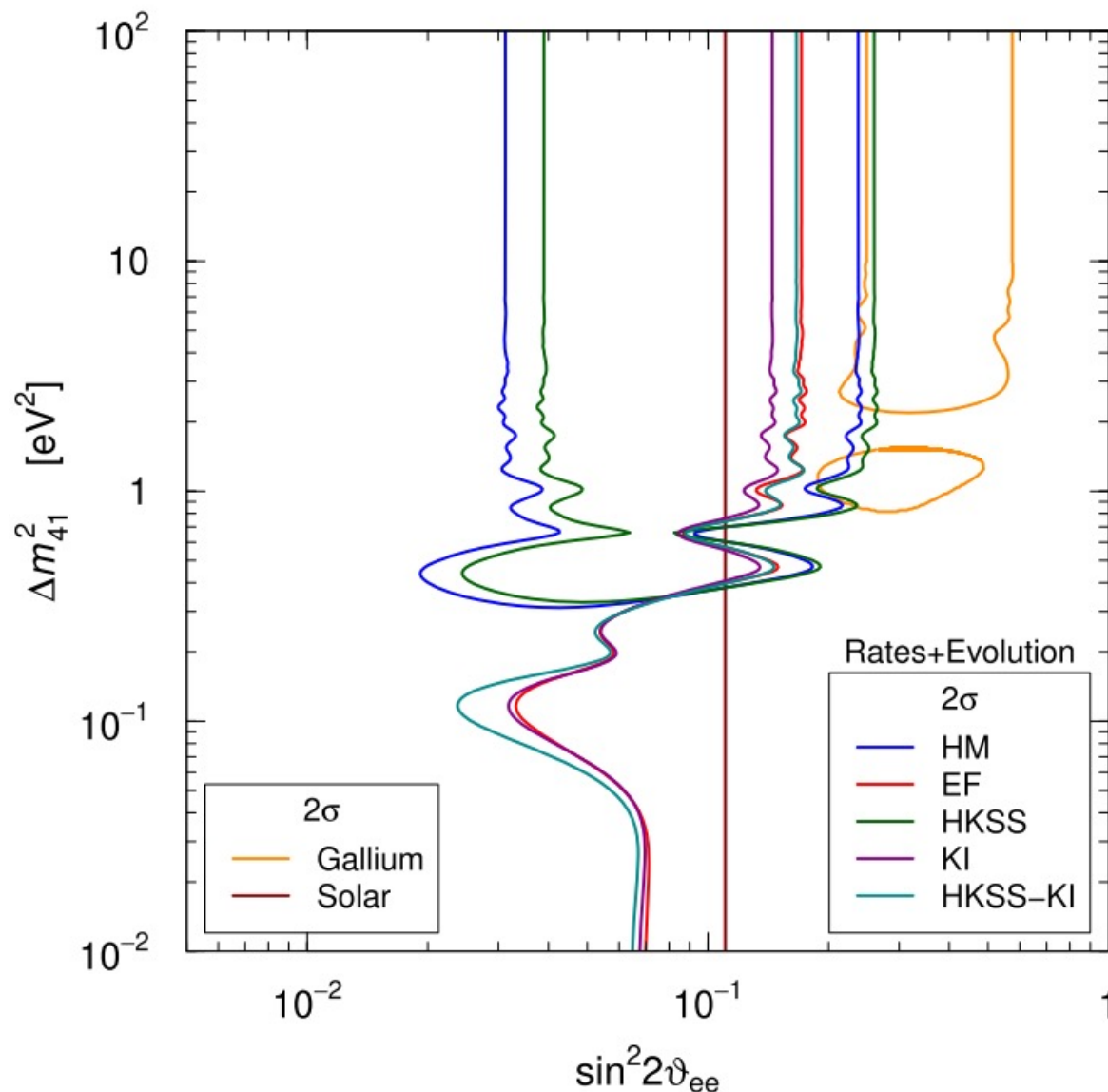


Rates + Evolution data

Test	HM	EF	HKSS	KI	HKSS-KI
χ^2	0.13	0.22	0.08	0.68	0.44
SW	0.32	0.13	0.35	0.59	0.41
sign	0.03	0.38	0.006	0.38	0.11
KS	0.04	0.84	0.02	0.39	0.20
CVM	0.02	0.67	0.006	0.38	0.14
AD	0.02	0.57	0.006	0.40	0.13
Z_K	$< 10^{-3}$	0.05	$< 10^{-3}$	0.05	0.008
Z_C	0.02	0.11	0.005	0.55	0.15
Z_A	0.03	0.20	0.01	0.41	0.12
weighted average	0.05	0.35	0.03	0.42	0.16


EF model is the best summation model
 KI model is the best conversion model

Implications for neutrino oscillations

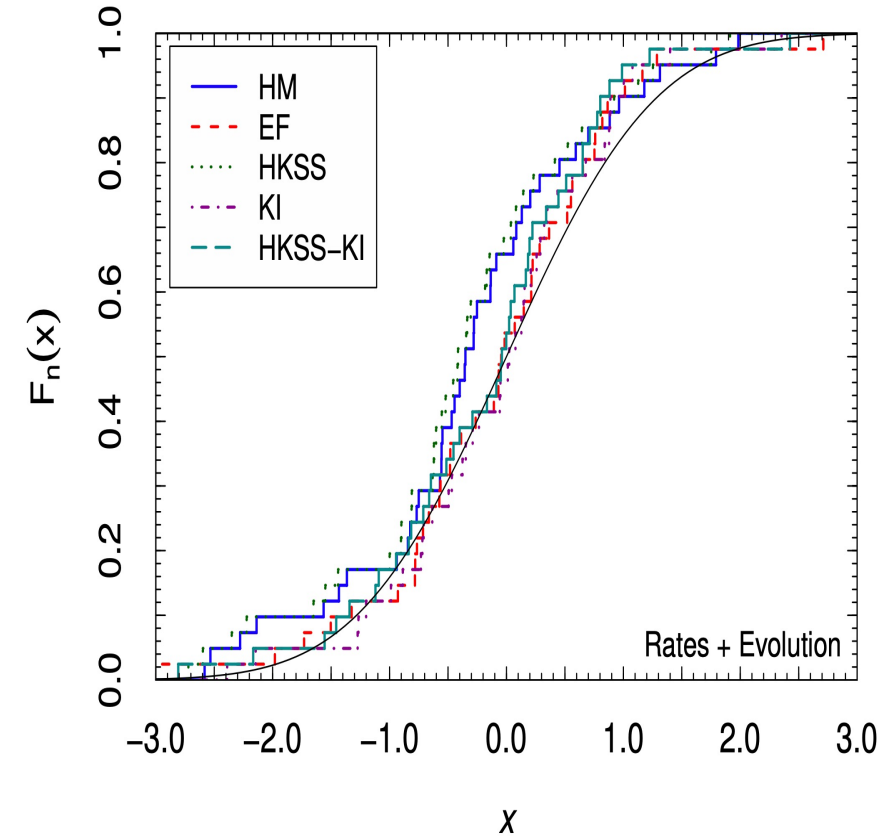
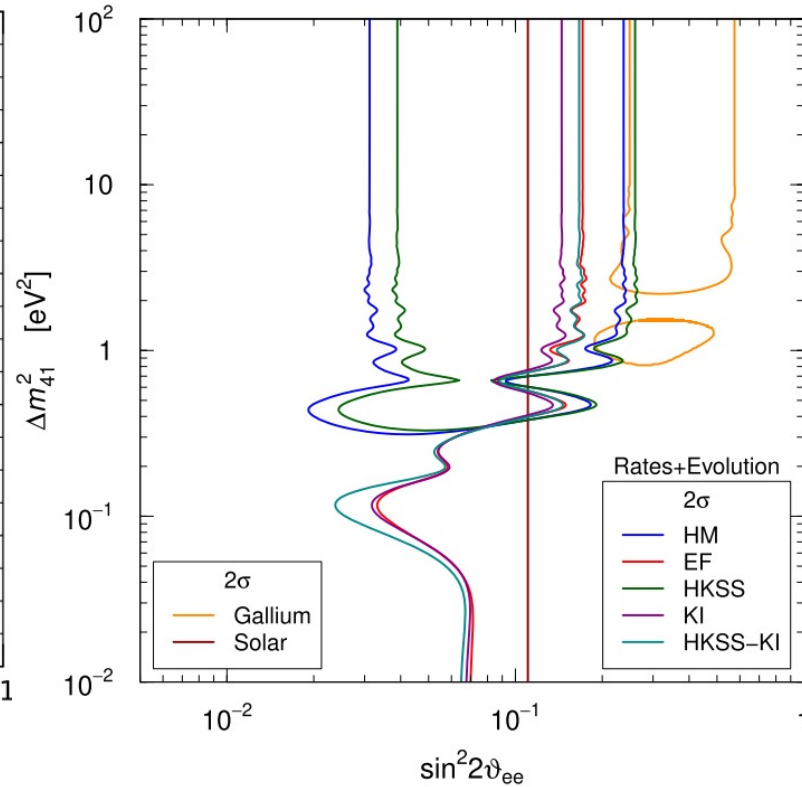
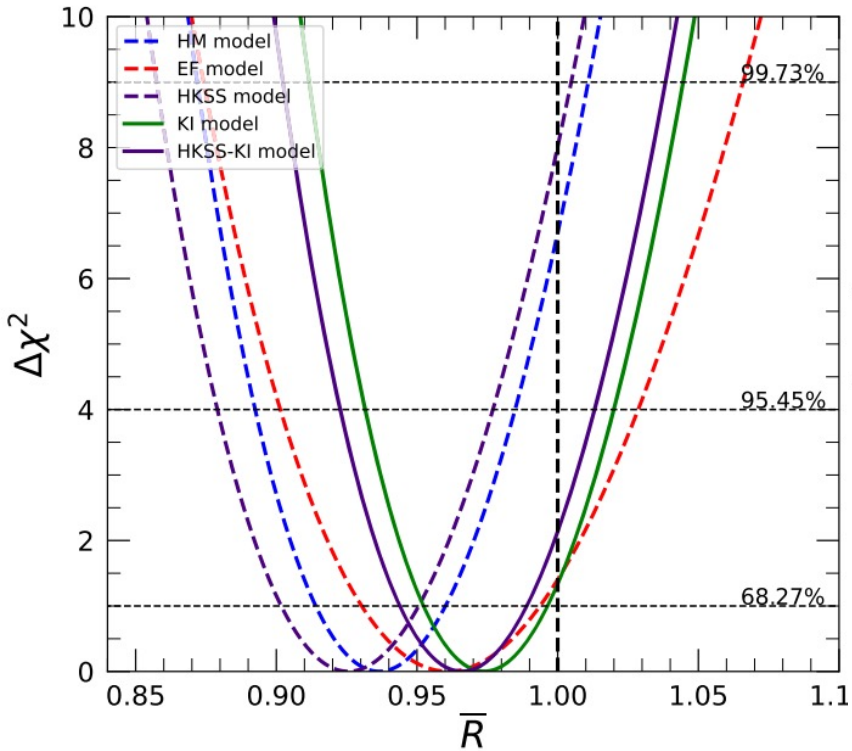
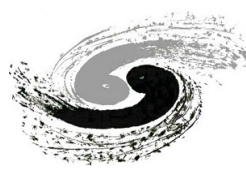


C. Giunti, Y. F. Li, C. A. Ternes, ZX,
Phys.Lett.B 829 (2022) 137054

$$P_{ee} \simeq 1 - \sin^2 2\theta_{ee} \sin^2 \left(\frac{\Delta m_{41}^2 L}{4E} \right)$$

- EF and KI models 
 No short-baseline oscillations
- Reactor data upper limits
 - $\sin^2 2\theta_{ee} \lesssim 0.14 \sim 0.25$ at 2σ
 - disfavor Gallium anomaly allowed region
- Gallium anomaly allowed region is also in tension with solar upper bound.

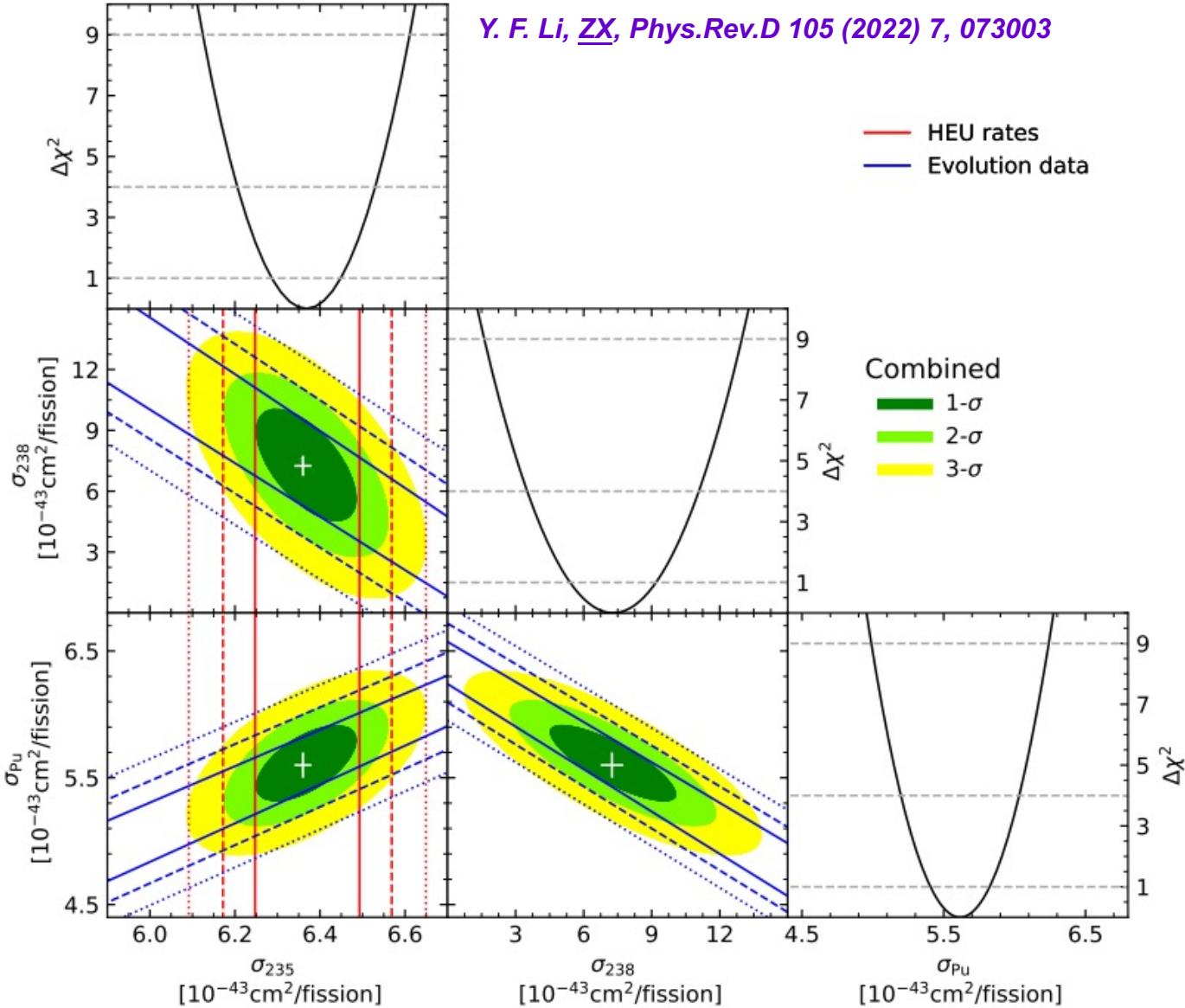
What more can reactor data provide ?



- Flux models still have a (small) deviation compared with reactor data.
- **Can reactor data offer a data-driven flux model?**

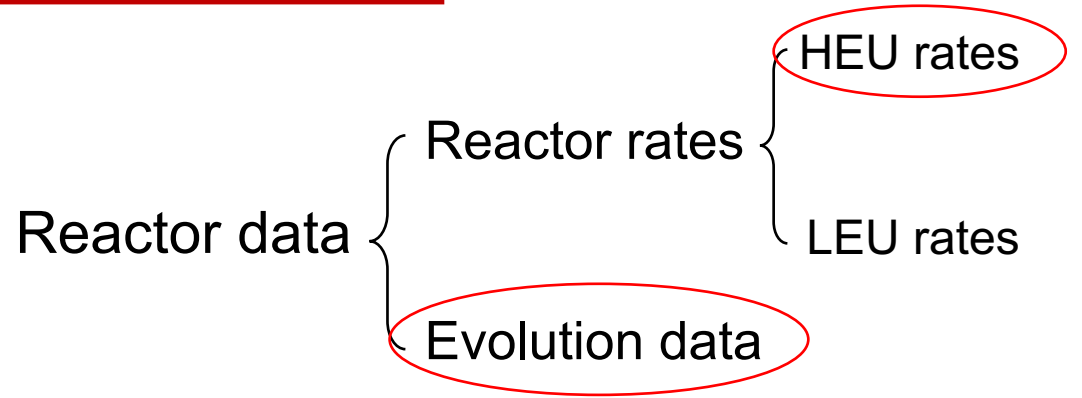
Rate: Model independent fluxes

Y. F. Li, *ZX*, *Phys.Rev.D* 105 (2022) 7, 073003



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- Combined Pu component (**LEU data**)

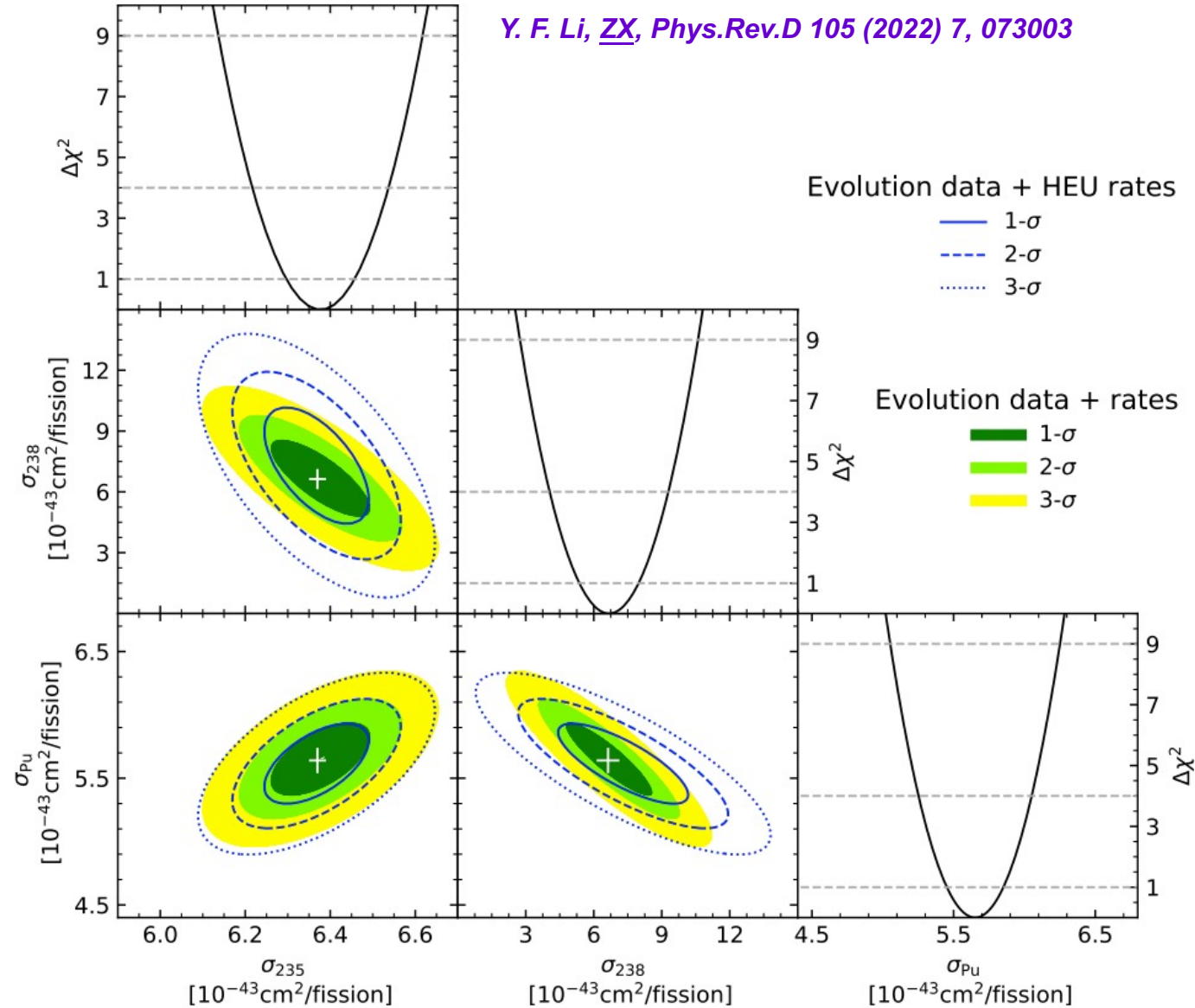
$$f_{241} = k \cdot f_{239}$$

$$\sigma_{\text{Pu}} = \sigma_{239} + k \cdot \sigma_{241}$$

- The **HEU rates** constrain σ_{235}
- The **evolution data** constrain the linear combination of σ_i 's
- The **LEU rates data** constrain σ_{238} and σ_{Pu}

Rate: Model independent fluxes

Y. F. Li, *ZX*, *Phys.Rev.D* 105 (2022) 7, 073003



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Reactor data

Reactor rates

HEU rates

LEU rates

Evolution data

- Combined Pu component (**LEU data**)

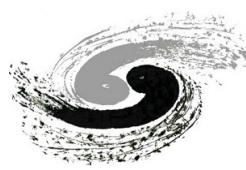
$$f_{241} = k \cdot f_{239}$$

$$\sigma_{\text{Pu}} = \sigma_{239} + k \cdot \sigma_{241}$$

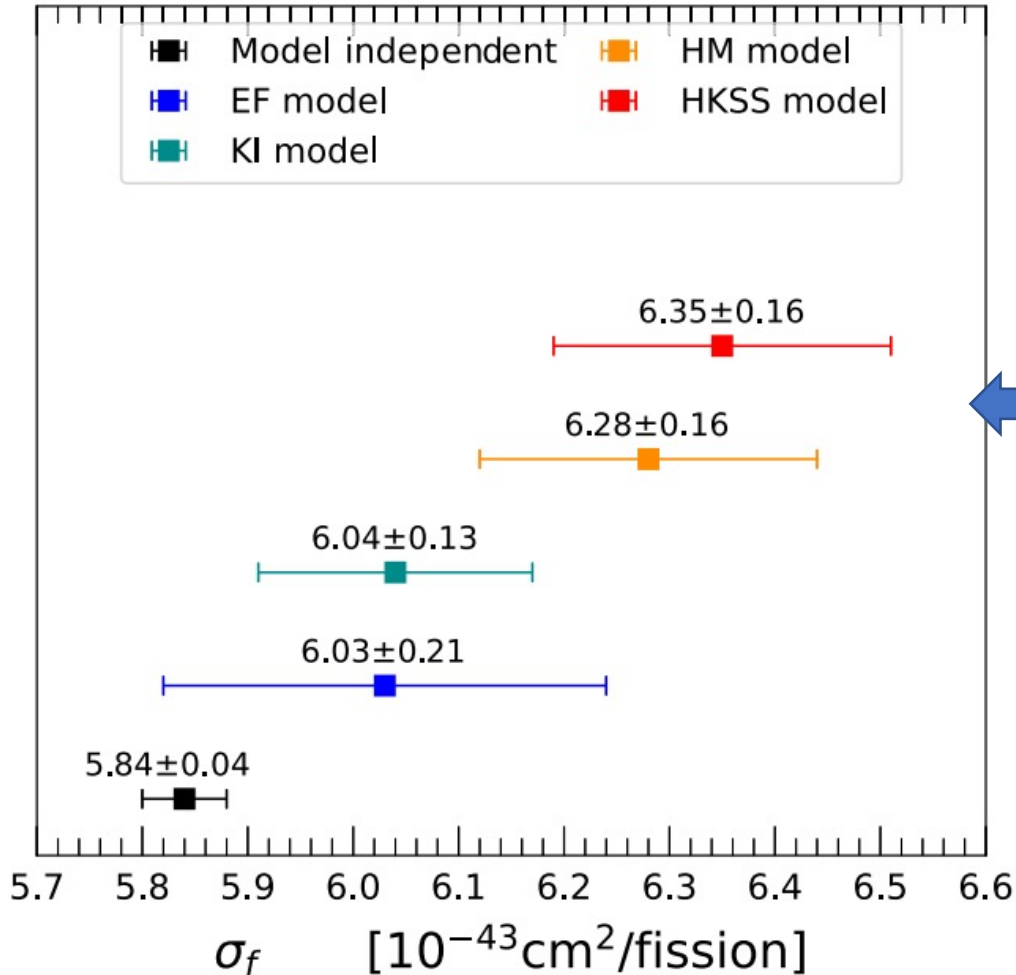
- The **LEU rates** constrain σ_{238} and σ_{Pu} further
- Model independent fluxes

$$\begin{cases} \sigma_{235} = (6.37 \pm 0.08) \times 10^{-43} \text{ cm}^2/\text{fission}, \\ \sigma_{238} = (6.63 \pm 1.30) \times 10^{-43} \text{ cm}^2/\text{fission}, \\ \sigma_{\text{Pu}} = (5.64 \pm 0.20) \times 10^{-43} \text{ cm}^2/\text{fission}, \end{cases}$$

Rate: Prediction of a future experiment



$$f_{241} = k \cdot f_{239} \text{ (LEU data)}$$



- How to predict the IBD yield for a certain experiment:

$$\sigma_A = f_{235}^A \sigma_{235} + f_{238}^A \sigma_{238} + f_{239}^A \sigma_{Pu} + \Delta f^A \sigma_{241}^{HM}$$

- A LEU reactor with typical fission fractions

(0.577: 0.076: 0.295: 0.052)

$$\sigma^{\text{pre}} = 5.84 \pm (0.04)_{\text{MI}} \pm (0.0004)_{\text{HM}} \quad (0.7\%)$$

- Another European reactors with mixed oxide technology with typical fission fractions

(0.000: 0.080: 0.708: 0.212)

$$\sigma^{\text{pre}} = 5.05 \pm (0.07)_{\text{MI}} \pm (0.01)_{\text{HM}} \quad (1.4\%)$$



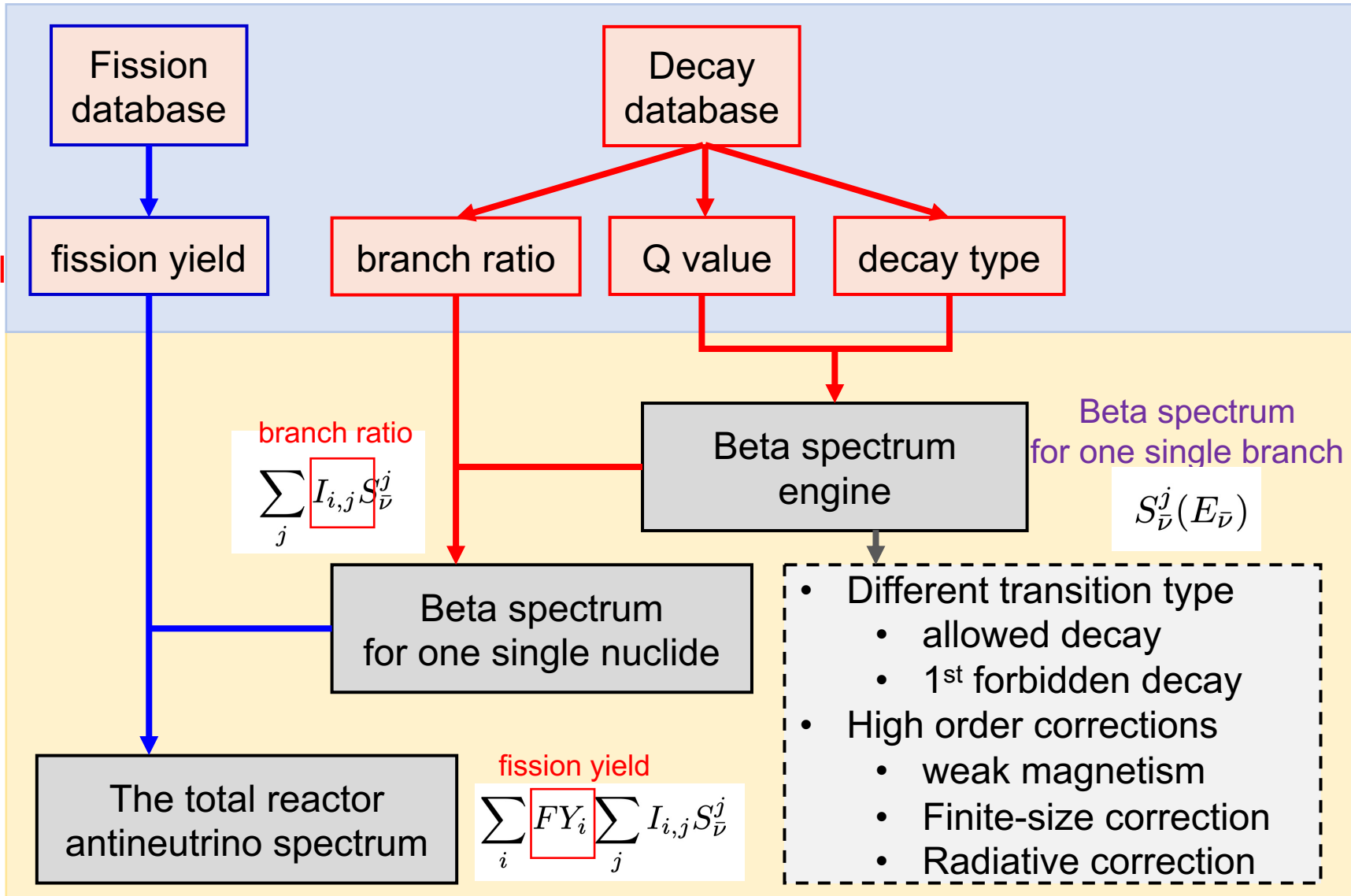
Shape: Summation model

Nuclear database inputs

The fundamental of summation model

Spectra calculation

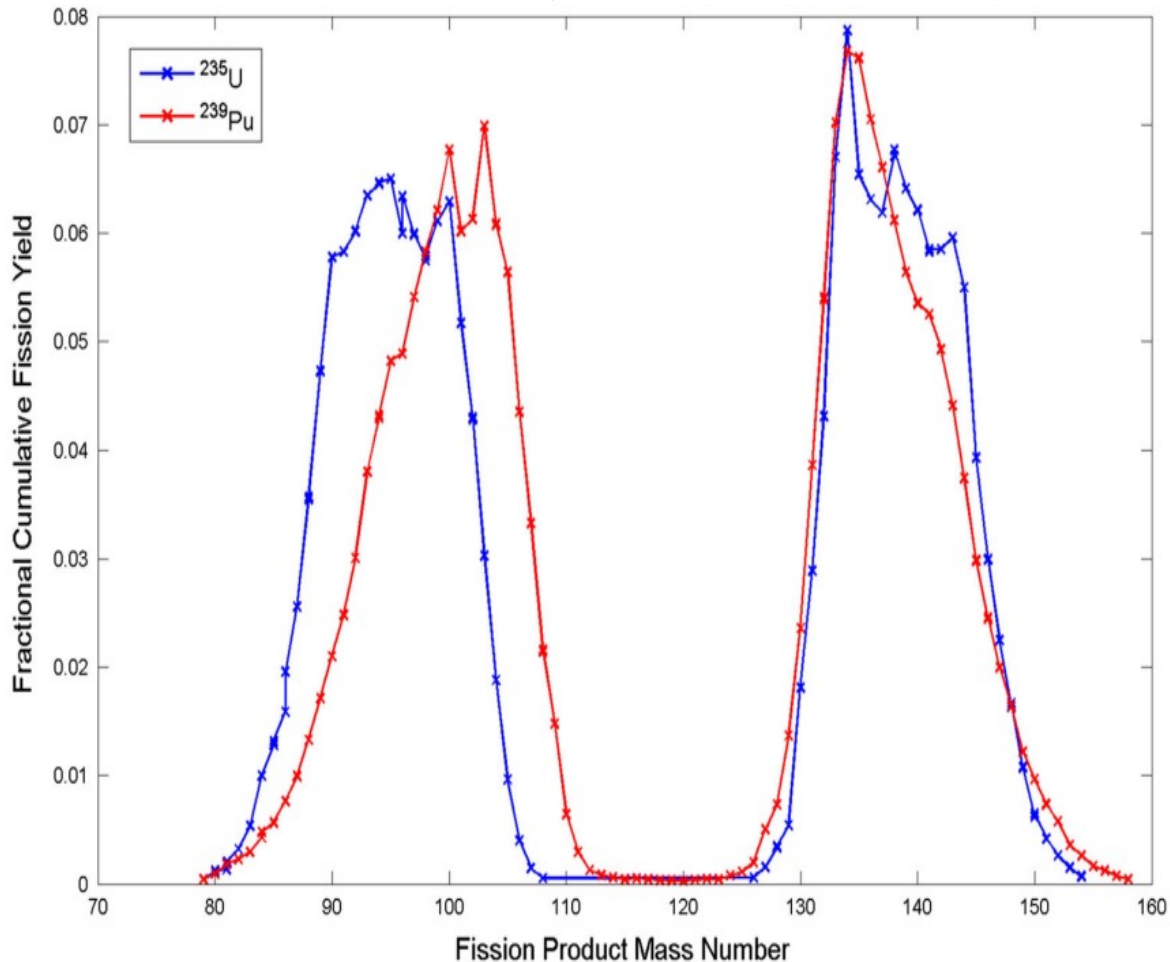
Follow the calculation in
Phys.Rev.D 100 (2019) 5, 053005
Yufeng Li, Di Zhang



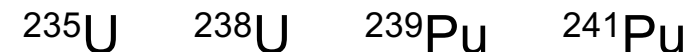
Summation model: fission database



Cumulative fission product yield from thermal neutron-induced fission



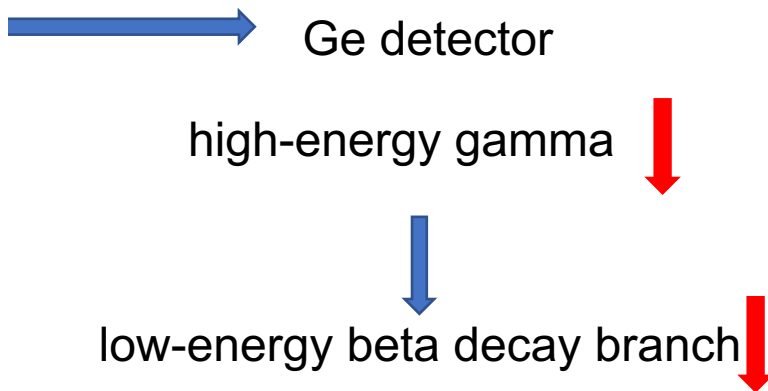
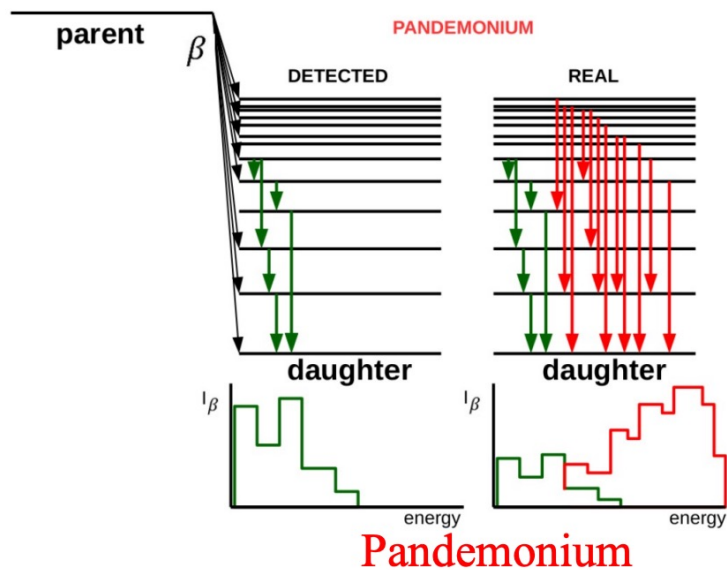
Reactor antineutrinos flux produced by beta decays of fission products of



The fission data are taken in the following order of priority

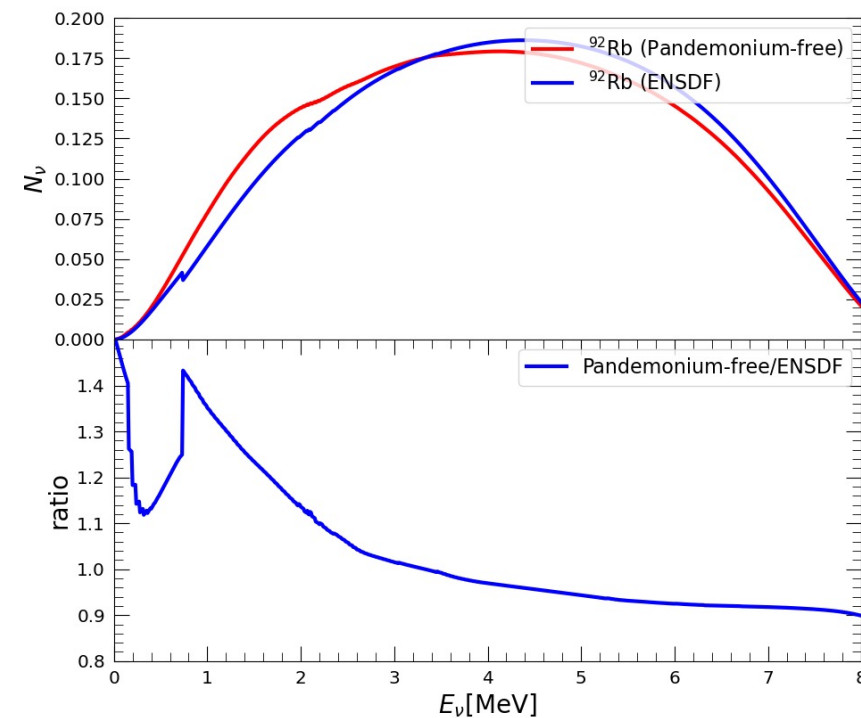
Nuclear database	^{235}U	^{238}U	^{239}Pu	^{241}Pu
JEFF	963 (963)	935 (935)	1093 (1093)	1071 (1071)
ENDF	195 (1158)	268 (1208)	198 (1226)	203 (1263)
JENDL	0 (1152)	6 (1139)	0 (1241)	7 (1241)
CENDL	0 (1158)	0 (1209)	0 (1226)	0 (1264)
Total	1158	1209	1291	1281

Summation model: decay database



Pandemonium effect

Overestimation of high-energy spectra



The decay data are taken in the following order of priority

Pandemonium-free data

~20%

More Pandemonium-free data urgently needed

ENSDF database

~60%

Gross theory

Phys. Rev. C 98, 041303(R) (2018).

~14%

Q-approximation

~6%

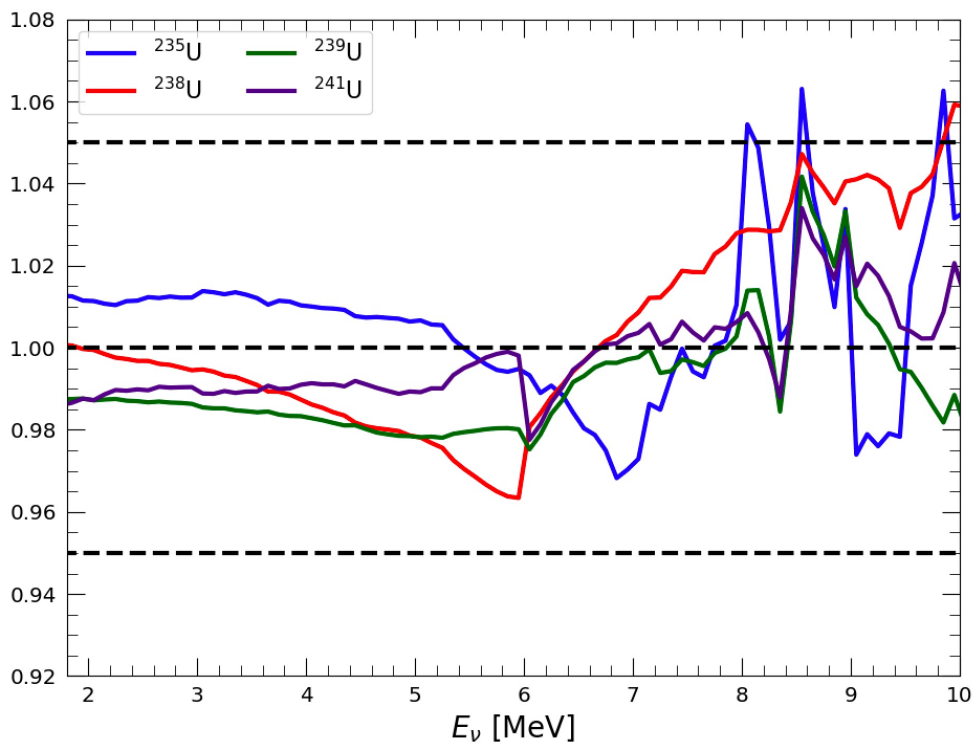
Phys. Rev. Lett. 123 (2 2019)

More Pandemonium-free data added comparing with EF model 2018

Summation model: decay database

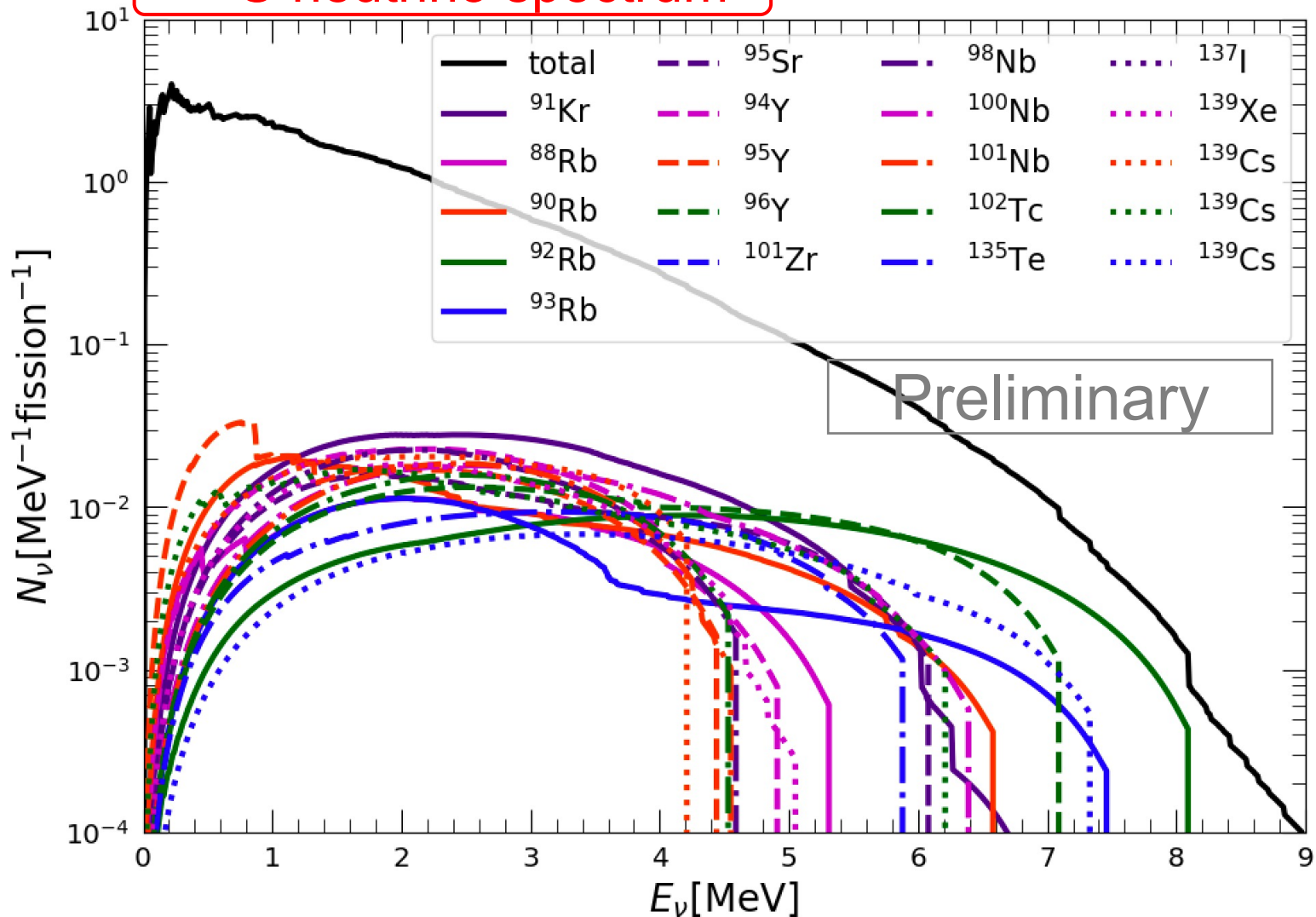


- Total summation spectrum and the main contributions for ^{235}U neutrino spectrum
- Consistent with SM 2018 within 5%



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^{235}U neutrino spectrum



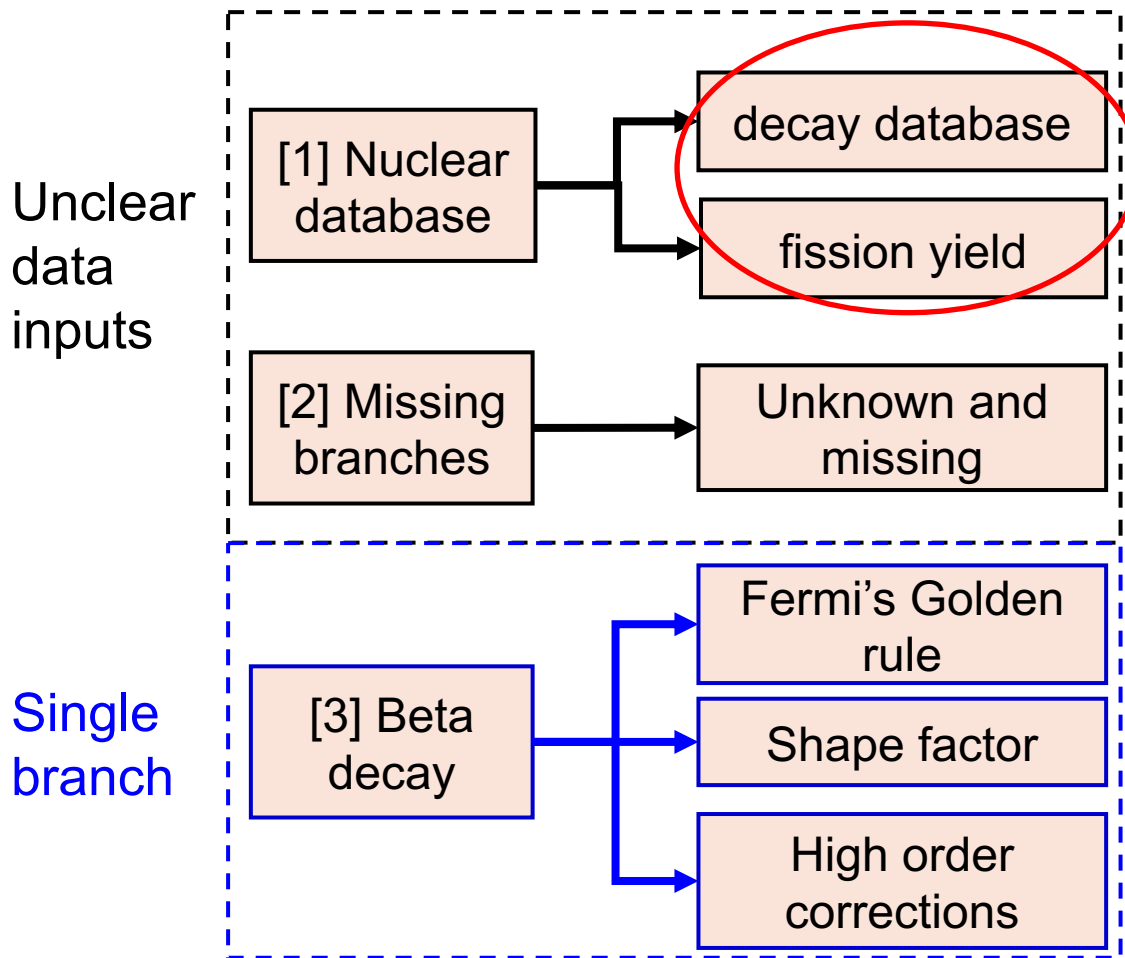
COUSP-2024

20

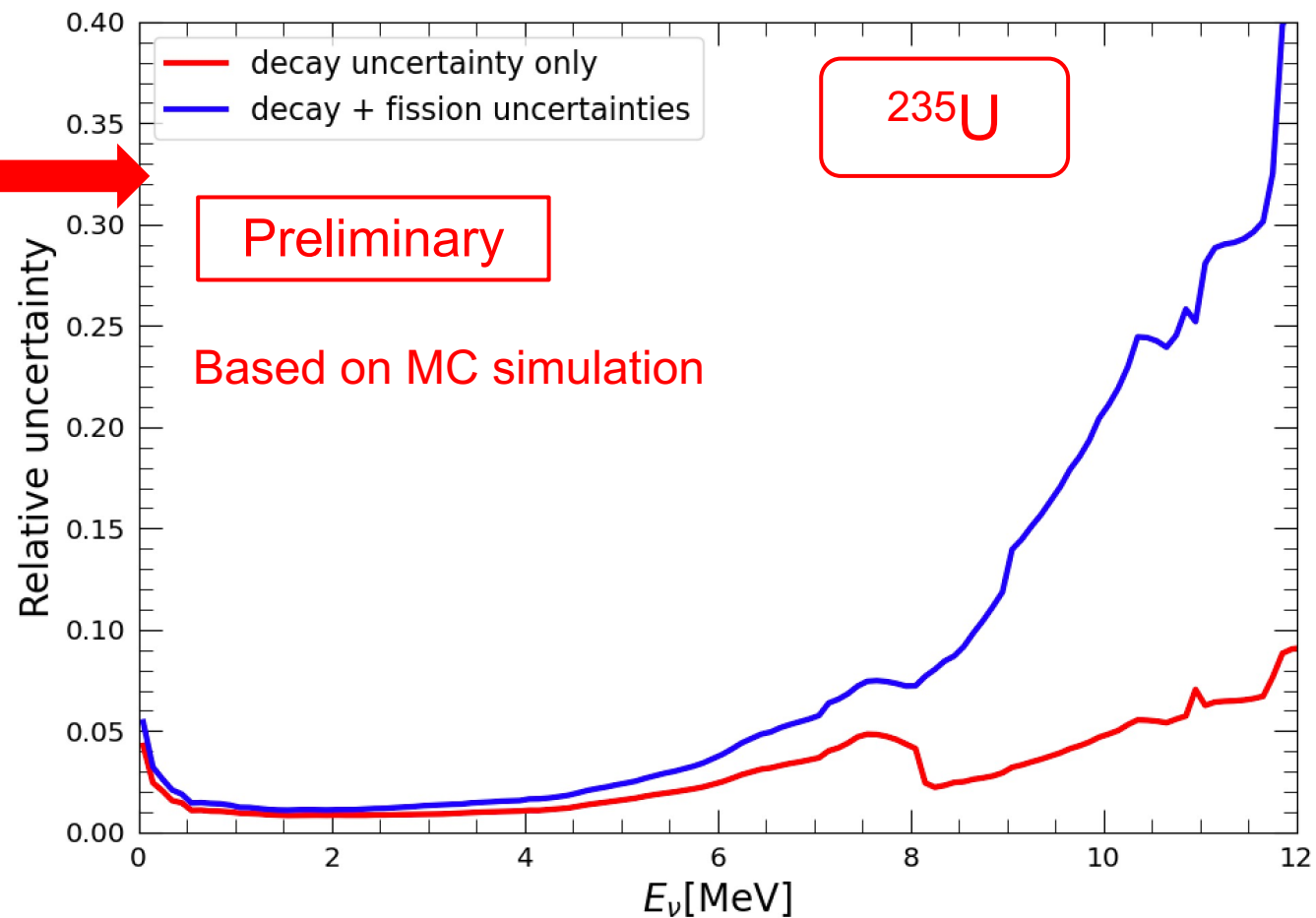
Summation model: uncertainty evaluation



Uncertainty source



The uncertainty evaluation caused by [1] nuclear database



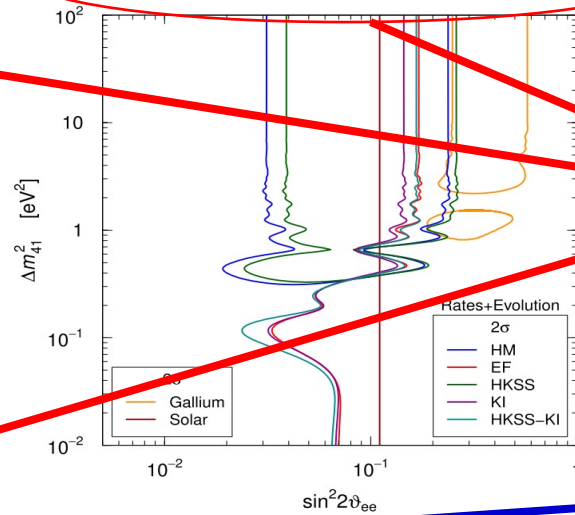
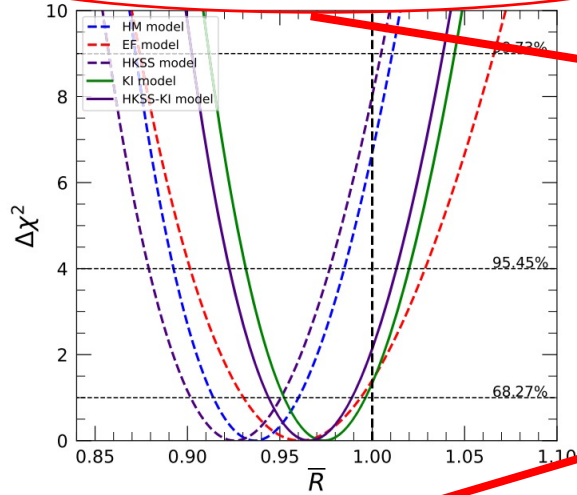
The correlation between fission yields is not included yet, which will be included. (will enlarge uncertainty)



Conclusion

Reactor Antineutrino Anomaly

Short-baseline oscillation



- RAA → recent flux model refinements

Best-fit models: EF and KI

- No RAA
- No short-baseline oscillations

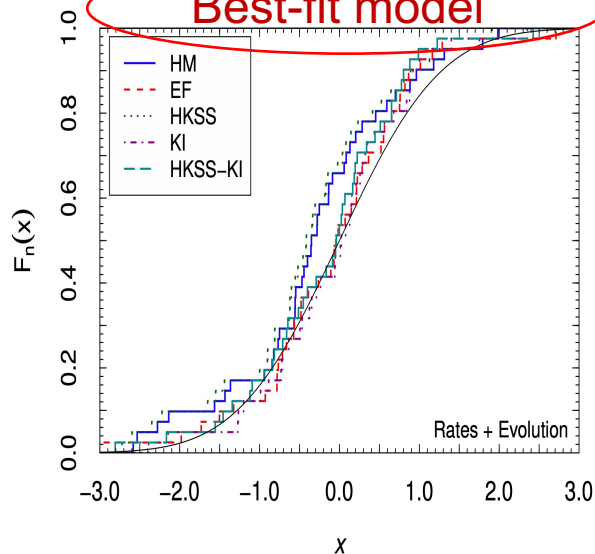
Global fits of reactor data

- Model independent isotopic fluxes
- High precision IBD yields

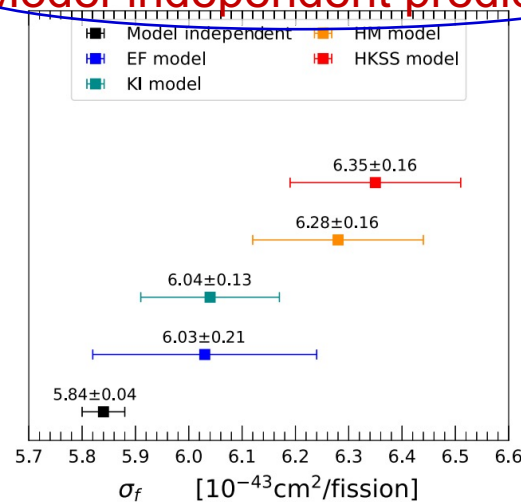
The bump anomaly needs more investigation.

Our summation model.

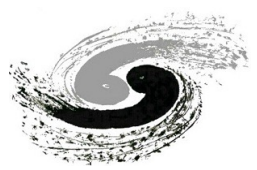
Best-fit model



Model-independent prediction



Thanks for your attention!



Backup



Updated IBD yields

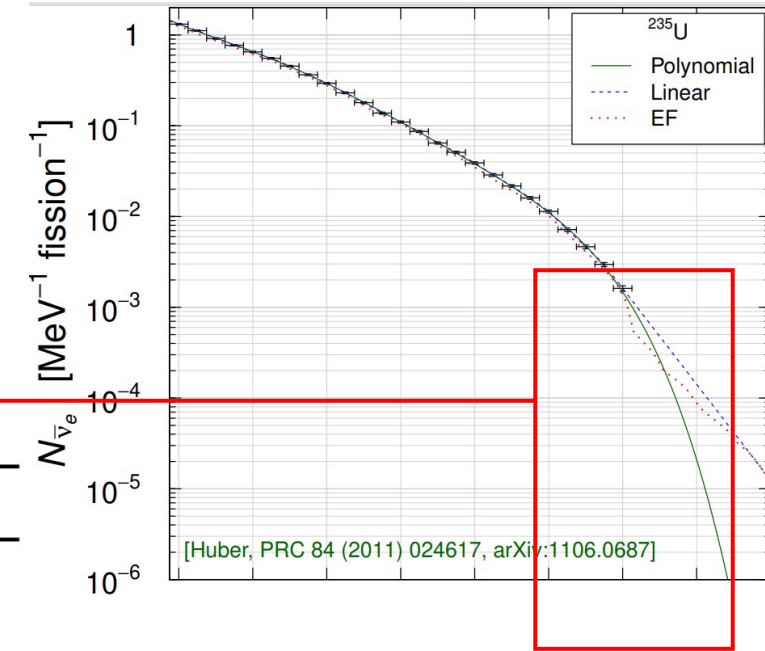
• The individual IBD yield σ_i

1. IBD cross section

2. Integral energy regions (1.8→10.0 MeV)

- Low energy region (1.8 → 8.0 MeV)
extrapolate and interpolate with the original spectra.
- High energy region approximation (8.0 → 10.0 MeV)

EF summation model spectra with a very conservative 100% uncertainty.



original IBD yields

Model	σ_{235}	σ_{238}	σ_{239}	σ_{241}
HM	6.69 ± 0.14	10.10 ± 0.82	4.40 ± 0.11	6.03 ± 0.13
EF	6.28 ± 0.31	10.14 ± 1.01	4.42 ± 0.22	6.07 ± 0.31
HKSS	6.74 ± 0.17	10.33 ± 0.85	4.43 ± 0.13	6.07 ± 0.16
KI	6.27 ± 0.13	9.34 ± 0.47	4.33 ± 0.11	6.01 ± 0.13

our updated results

Model	σ_{235}	σ_{238}	σ_{239}	σ_{241}
HM	6.74 ± 0.17	10.19 ± 0.83	4.40 ± 0.13	6.10 ± 0.16
EF	6.29 ± 0.31	10.16 ± 1.02	4.42 ± 0.22	6.23 ± 0.31
HKSS	6.82 ± 0.18	10.28 ± 0.84	4.42 ± 0.13	6.17 ± 0.16
KI	6.41 ± 0.14	9.53 ± 0.48	4.40 ± 0.13	6.10 ± 0.16
HKSS-KI	6.48 ± 0.14	10.28 ± 0.84	4.45 ± 0.13	6.17 ± 0.16

Small contribution above 8 MeV:
0.3% for ^{235}U , 0.9% for ^{238}U ,
0.2% for ^{239}Pu , 0.3% for ^{241}Pu .

Data Sets: reactor rates

- The data sets in our work are separated into **HEU rates** three categories:

- High-enriched uranium (HEU) reactor rates (8 rates)
 - As known as the research reactors, where ^{235}U is the main contributor to the neutrino spectra.
- Low-enriched uranium (LEU) reactor rates (18 rates)
 - As known as the commercial reactors, where the fission fraction of ^{235}U is only 0.5 ~ 0.6
- Fuel evolution data **LEU-like evolution data**
 - Daya Bay (8 data points)
 - RENO (8 data points)

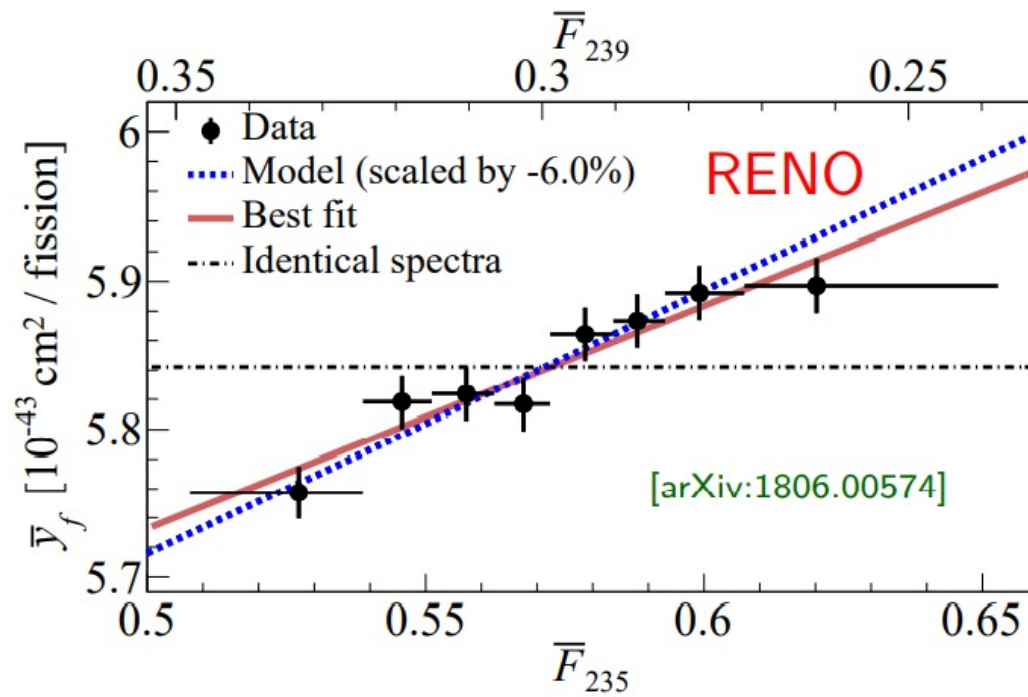
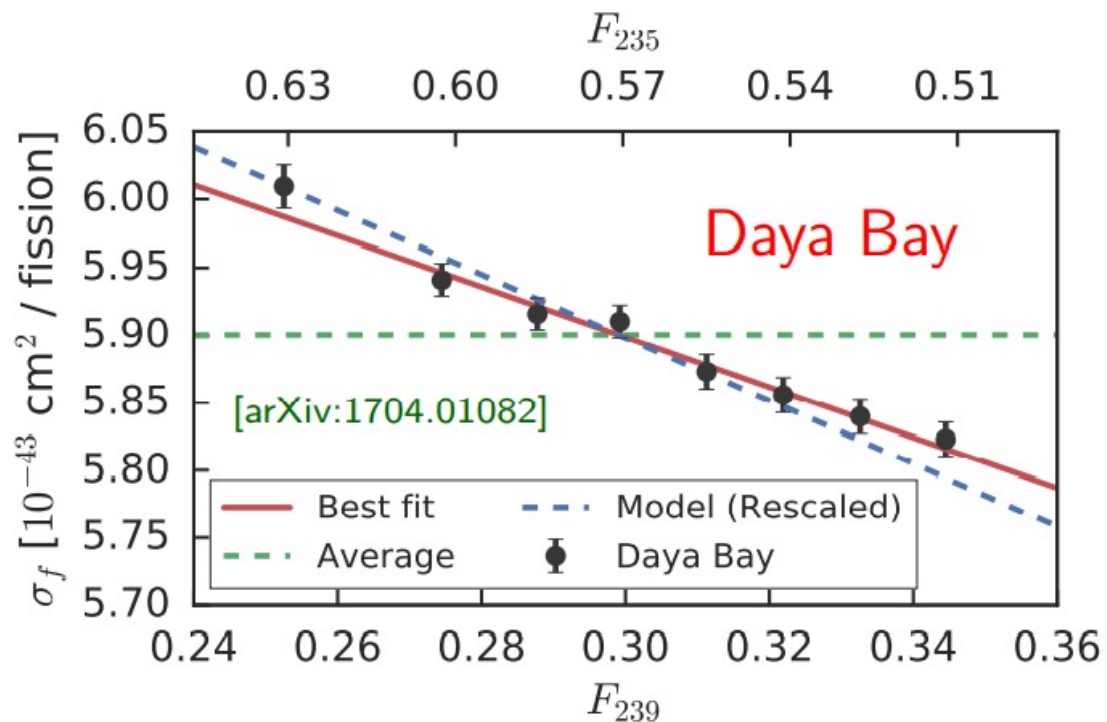
C. Giunti, Y. F. Li, C. A. Ternes, ZX, Phys.Lett.B 829 (2022) 137054

Y. F. Li, ZX, Phys.Rev.D 105 (2022) 7, 073003

Experiment	f_{235}^a	f_{238}^a	f_{239}^a	f_{241}^a	$\sigma_{f,a}^{\text{exp}}$	δ_a^{exp} [%]
ILL	1	0	0	0	5.30	9.1
Krasnoyarsk87-33	1	0	0	0	6.20	5.2
Krasnoyarsk87-92	1	0	0	0	6.30	20.5
Krasnoyarsk94-57	1	0	0	0	6.26	4.2
Krasnoyarsk99-34	1	0	0	0	6.39	3.0
SRP-18	1	0	0	0	6.29	2.8
SRP-24	1	0	0	0	6.73	2.9
STEREO	1	0	0	0	6.34	2.5

Experiment	f_{235}^a	f_{238}^a	f_{239}^a	f_{241}^a	$\sigma_{f,a}^{\text{exp}}$	δ_a^{exp} [%]
Chooz	0.496	0.087	0.351	0.066	6.12	3.2
Palo Verde	0.600	0.070	0.270	0.060	6.25	5.4
Daya Bay	0.564	0.076	0.304	0.056	5.94	1.5
RENO	0.571	0.073	0.300	0.056	5.85	2.1
Double Chooz	0.520	0.087	0.333	0.060	5.71	1.1
Bugey-4	0.538	0.078	0.328	0.056	5.75	1.4
Rovno91	0.614	0.074	0.274	0.038	5.85	2.8
Rovno88-11	0.607	0.074	0.277	0.042	5.70	6.4
Rovno88-2I	0.603	0.076	0.276	0.045	5.89	6.4
Rovno88-1S	0.606	0.074	0.277	0.043	6.04	7.3
Rovno88-2S	0.557	0.076	0.313	0.054	5.96	7.3
Rovno88-3S	0.606	0.074	0.274	0.046	5.83	6.8
Bugey-3-15	0.538	0.078	0.328	0.056	5.77	4.2
Bugey-3-40	0.538	0.078	0.328	0.056	5.81	4.3
Bugey-3-95	0.538	0.078	0.328	0.056	5.35	15.2
Gosgen-38	0.619	0.067	0.272	0.042	5.99	5.4
Gosgen-46	0.584	0.068	0.298	0.050	6.09	5.4
Gosgen-65	0.543	0.070	0.329	0.058	5.62	6.7

Data Sets: evolution data



LSM with Wilks' theorem



How to treat the **systematic theoretical uncertainties** in the least-squares function.

Method A *Phys. Rev. D83, 073006 (2011)*
JHEP 1706, 135 (2017)

A covariance matrix with experimental and theoretical uncertainties added in quadrature.

$$\chi^2 = \sum_{a,b} \left(\sigma_{f,a}^{\text{exp}} - R_{\text{NP}}^a \sigma_{f,a}^{\text{th}} \right) (V^{\text{tot}})^{-1}_{ab} \left(\sigma_{f,b}^{\text{exp}} - R_{\text{NP}}^b \sigma_{f,b}^{\text{th}} \right)$$

$$V^{\text{tot}} = V^{\text{exp}} + \underline{V^{\text{th}}} \quad \sigma_{f,a}^{\text{th}} = \sum_i f_i^a \sigma_i^{\text{mod.}}$$

A **strongly-correlated theoretical** matrix derived from the covariance matrix V_{ij}^{mod} among ^{235}U , ^{238}U , ^{239}Pu , and ^{241}Pu

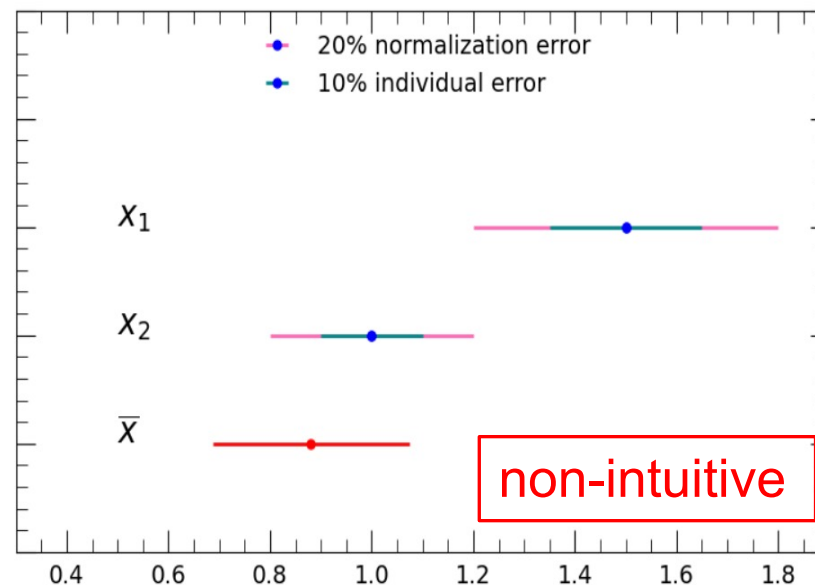
The method A will suffer the PPP!

Journal of Nuclear Science and Technology 31, 770 (1994).

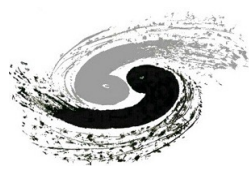
Peelle's Pertinent Puzzle

strongly correlated data

the best-fit average can be lower than most of the data



- improper combination of experimental and theoretical matrices
- truncation of data space.



LSM with Wilks' theorem

Method B *Phys. Rev. D87, 073018 (2013)*

Calculate the fit results considering only the experimental uncertainties and add by hand a global theoretical uncertainty to the final result.

hard to calculate

$$\chi^2 = \sum_{a,b} \left(\sigma_{f,a}^{\text{exp}} - R_{\text{NP}}^a \sigma_{f,a}^{\text{th}} \right) (V^{\text{exp}})_{ab}^{-1} \left(\sigma_{f,b}^{\text{exp}} - R_{\text{NP}}^b \sigma_{f,b}^{\text{th}} \right)$$

Method C

Method C is adopted in this work!

Phys.Rev.Lett. 120, 022503 (2018),

Phys.Rev. D99, 073005 (2019)

Consider the theoretical uncertainties with appropriate **pull terms**

$$\chi^2 = \sum_{a,b} \left(\sigma_{f,a}^{\text{exp}} - R_{\text{NP}}^a \sigma_{f,a}^{\text{th}} \right) (V^{\text{exp}})_{ab}^{-1} \left(\sigma_{f,b}^{\text{exp}} - R_{\text{NP}}^b \sigma_{f,b}^{\text{th}} \right)$$

$$+ \sum_{i,j \in \Omega} (r_i - 1) \left(\tilde{V}^{\text{mod}} \right)_{ij}^{-1} (r_j - 1),$$

PPP is avoided by decoupling the minimization of **physical parameters** from the minimization of **pull coefficients!**

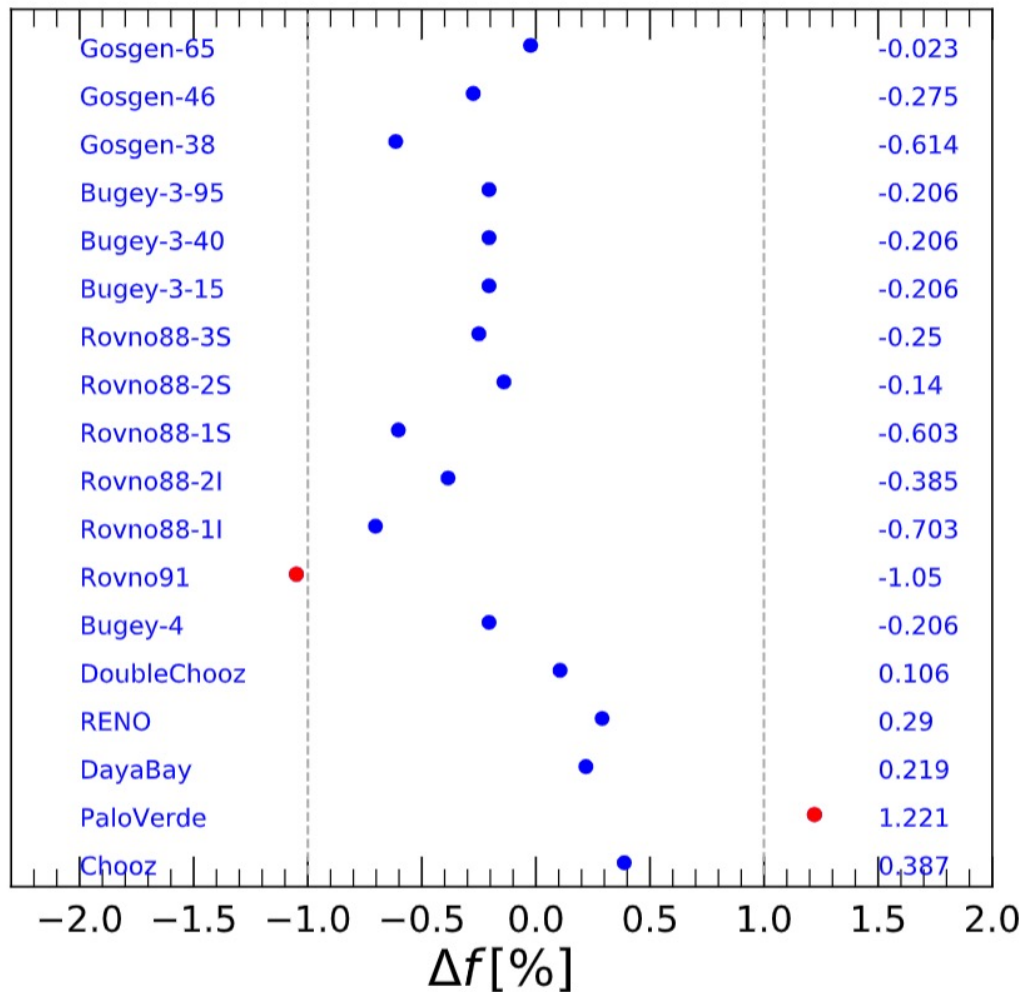
$$\sigma_{f,a}^{\text{th}} = \sum_i r_i f_i^a \sigma_i^{\text{mod}}. \quad \tilde{V}_{ij}^{\text{mod}} = V_{ij}^{\text{mod}} / (\sigma_i^{\text{mod}} \sigma_j^{\text{mod}})$$

V_{ij}^{mod} covariance matrix for these four isotopes

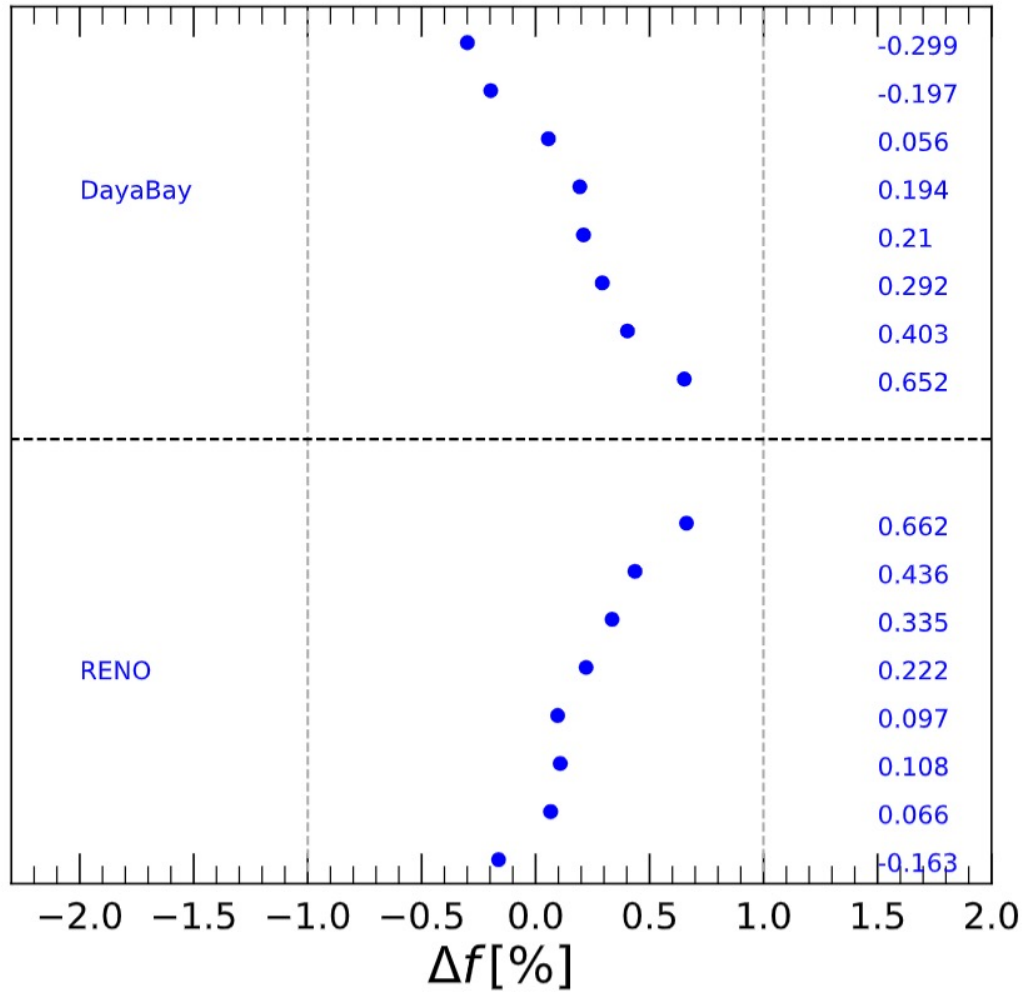


Pu's linearity

$$\Delta f = f_{241} - k \cdot f_{239} \text{ for LEU-like data sets}$$



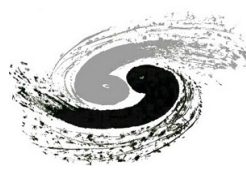
(a) LEU reactor data



(b) Reactor evolution data

The linearity between Pu's is well described, for most data points $\Delta f < 1\%$

χ^2 function in model-independent fit



• The χ^2 function

$$\chi^2 = \sum_{a,b} \left(\sigma_{f,a}^{\text{exp}} - \sigma_{f,a}^{\text{fit}} \right) (V^{\text{exp}})^{-1}_{ab} \left(\sigma_{f,b}^{\text{exp}} - \sigma_{f,b}^{\text{fit}} \right),$$

The direct extraction

$$\sigma_{f,a}^{\text{fit}} = f_{235}^a \cdot \sigma_{235}^{\text{fit}} + f_{238}^a \cdot \sigma_{238}^{\text{fit}} + f_{239}^a \cdot \sigma_{239}^{\text{fit}} + f_{241}^a \cdot \sigma_{241}^{\text{fit}}$$

all data

$$\begin{aligned} \sigma_{235} &= 6.37 \pm 0.08 \\ \sigma_{238} &= 8.97 \pm 2.62 \\ \sigma_{239} &= 2.98 \pm 1.54 \\ \sigma_{241} &= 11.62 \pm 5.33 \end{aligned}$$

Used in this work

The improved extraction

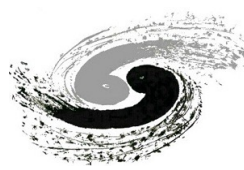
$$\sigma_{f,a}^{\text{fit}} = f_{235}^a \cdot \sigma_{235}^{\text{fit}} + f_{238}^a \cdot \sigma_{238}^{\text{fit}} + f_{239}^a \cdot \sigma_{\text{Pu}}^{\text{fit}} + \Delta f^a \cdot \sigma_{241}^{\text{HM}},$$

all data

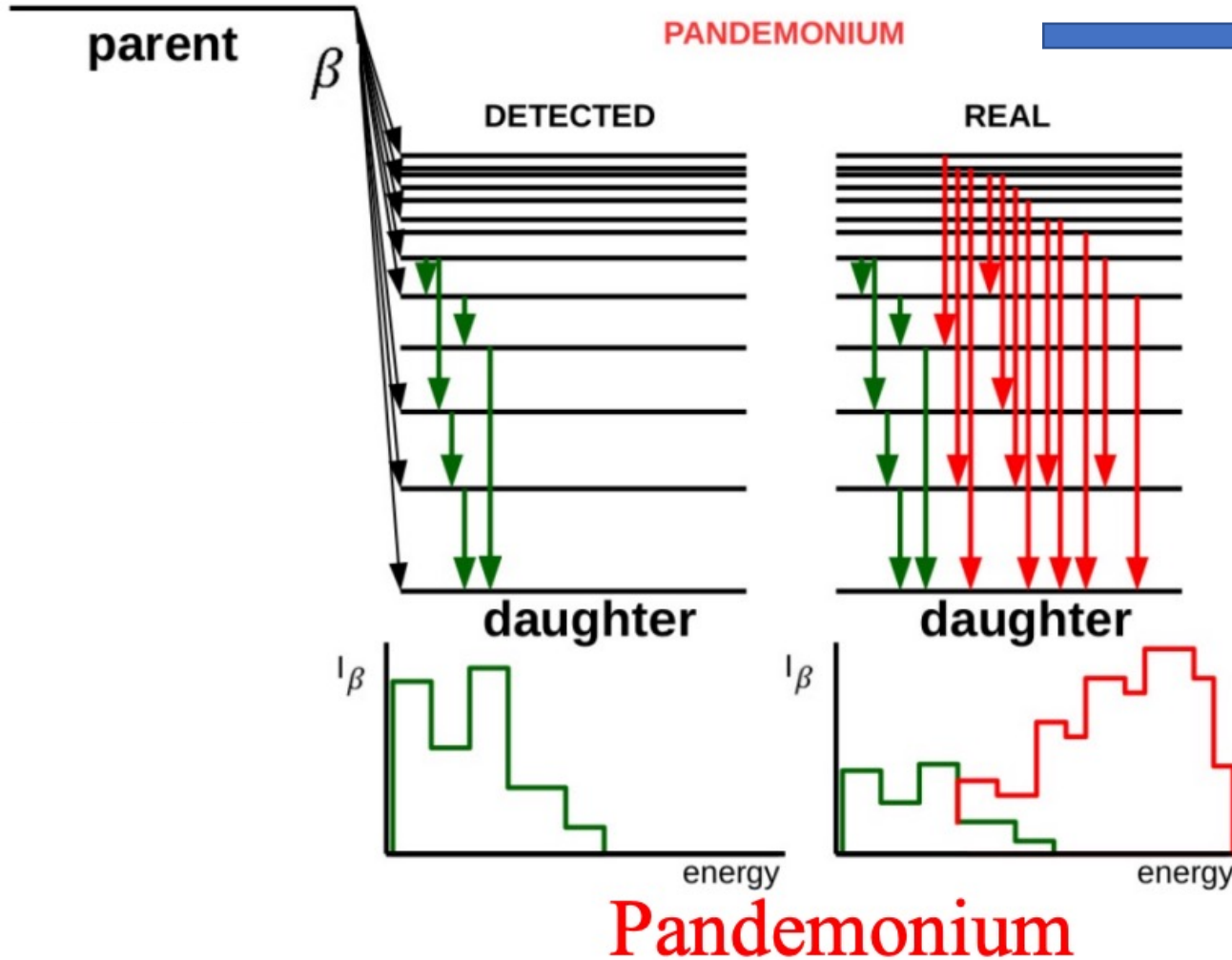
$$\begin{aligned} \sigma_{235} &= 6.37 \pm 0.08 \\ \sigma_{238} &= 6.63 \pm 1.30 \\ \sigma_{\text{Pu}} &= 5.64 \pm 0.20 \end{aligned}$$

- Reactor neutrino spectra models can offer referenced **Pu's IBD yields**
- The improved extraction can obtain **more precise IBD yields**

Model	σ_{235}	σ_{238}	σ_{239}	σ_{241}	$\sigma_{239} + 0.177\sigma_{241}$
HM	6.74 ± 0.17	10.19 ± 0.83	4.40 ± 0.13	6.10 ± 0.16	5.48 ± 0.13
EF	6.29 ± 0.31	10.16 ± 1.02	4.42 ± 0.22	6.23 ± 0.31	5.52 ± 0.23
HKSS	6.82 ± 0.18	10.28 ± 0.84	4.45 ± 0.13	6.17 ± 0.16	5.54 ± 0.13
KI	6.41 ± 0.14	9.53 ± 0.48	4.40 ± 0.13	6.10 ± 0.16	5.48 ± 0.13
HKSS-KI	6.48 ± 0.14	10.28 ± 0.84	4.45 ± 0.13	6.17 ± 0.16	5.54 ± 0.13



Pandemonium effect



Ge detector

high-energy gamma ↓



high-energy beta decay branch ↑

Pandemonium effect will enlarge the RAA



Statistic test

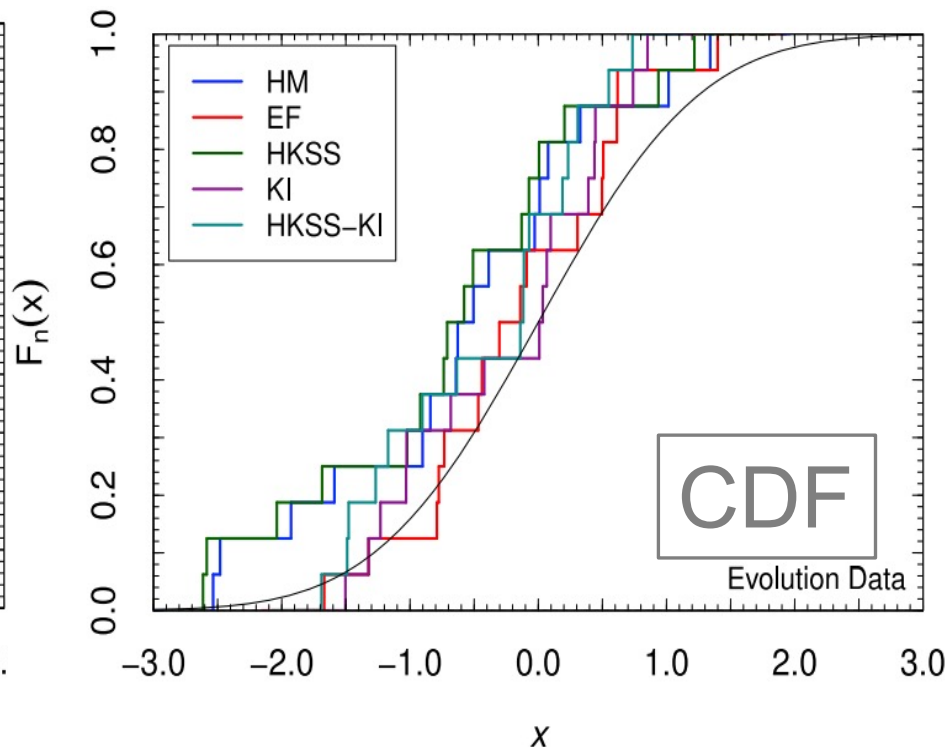
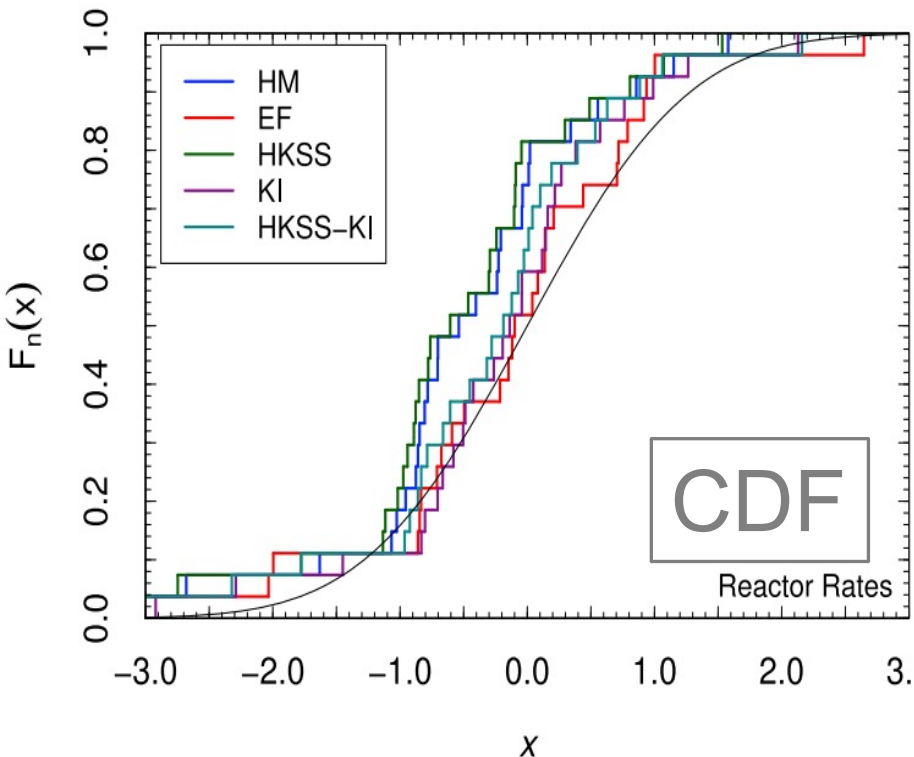
Statistic test

which model provides the best fit of reactor rates and the evolution data.

A normalized deviation of data and model

$$x_a^{\text{mod}} = \sum_b (V^{\text{tot}})_{ab}^{-1/2} (\sigma_{f,b}^{\text{exp}} - \sigma_{f,b}^{\text{mod}})$$

Shapiro-Wilk test



χ^2 test

size of deviation



Sign test

'+' or '-' deviation



Kolmogorov-Smirnov test

Cramer-von Mises test

Anderson-Darling test



Z_K, Z_C, Z_A test

*Journal of the Royal Statistical Society
Series B 64, 281 (2002).*

more powerful, based on
likelihood ratio