



中国科学院大学
University of Chinese Academy of Sciences



ICTP-AP
International Centre
for Theoretical Physics Asia-Pacific
国际理论物理中心-亚太地区

Dissipative Effects as New Observables for Cosmological Phase Transitions

郭怀珂

2024年5月8日

第三届地下和空间粒子物理与宇宙物理前沿问题研讨会

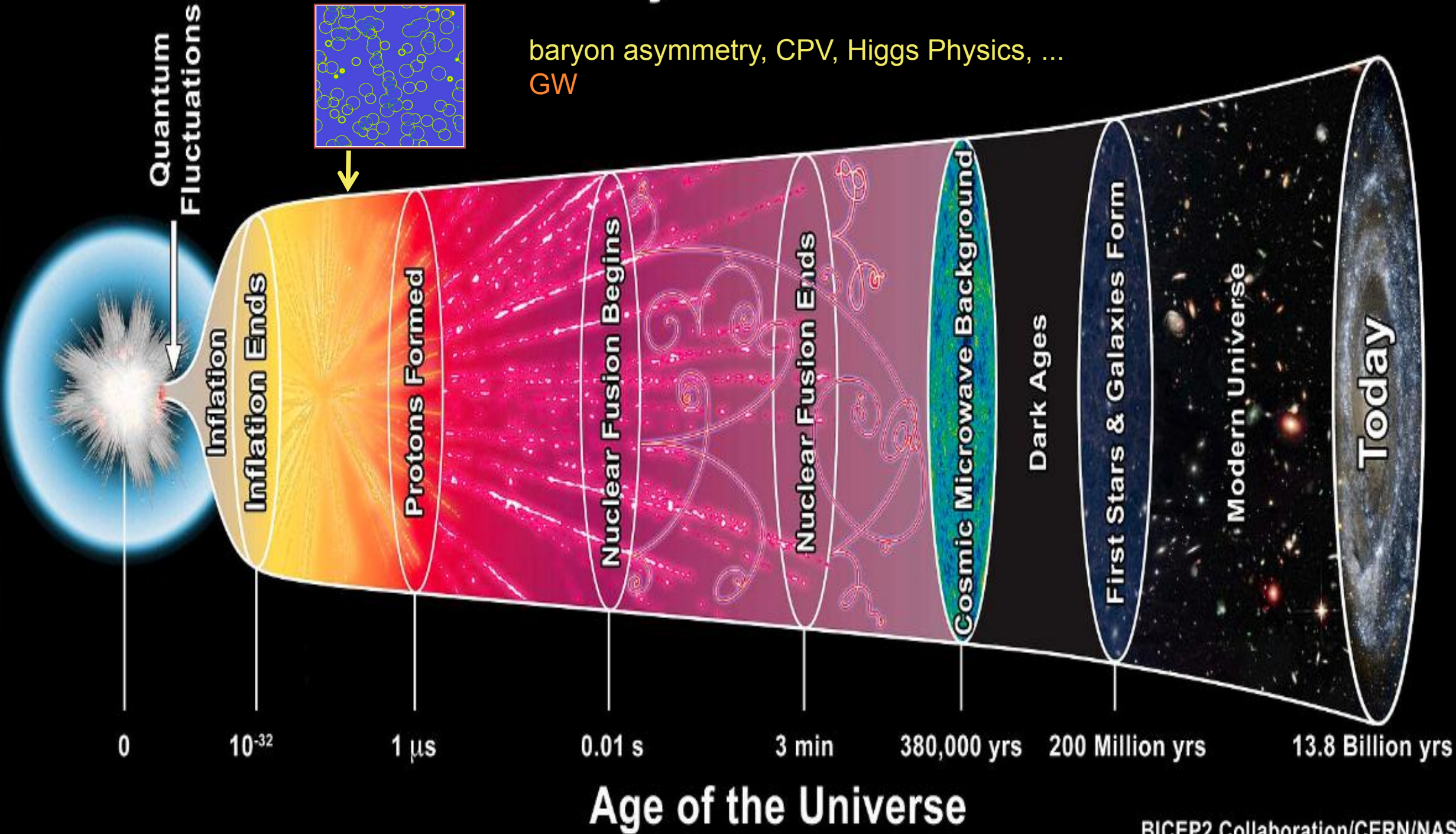
Conference on frontiers of underground and space particle physics and cosmophysics

2024年5月7日-11日，四川西昌



HG [2310.10927]

Radius of the Visible Universe

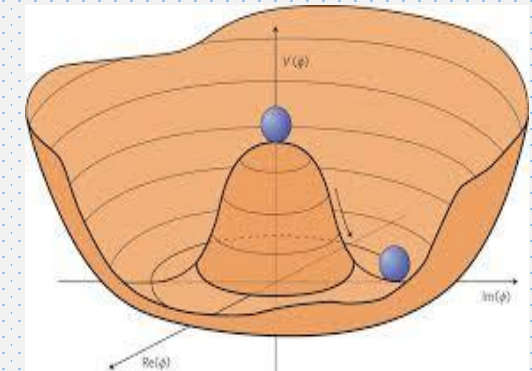
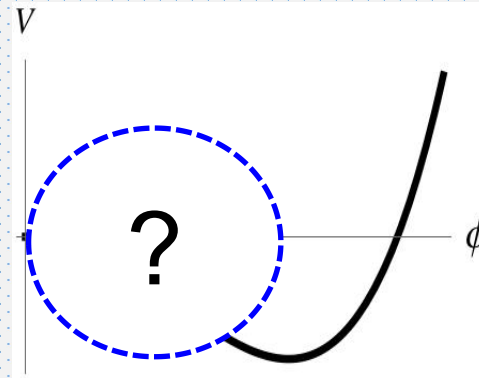
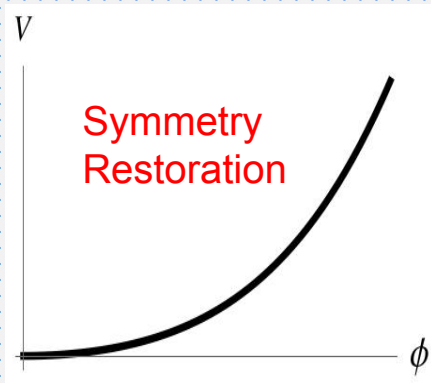




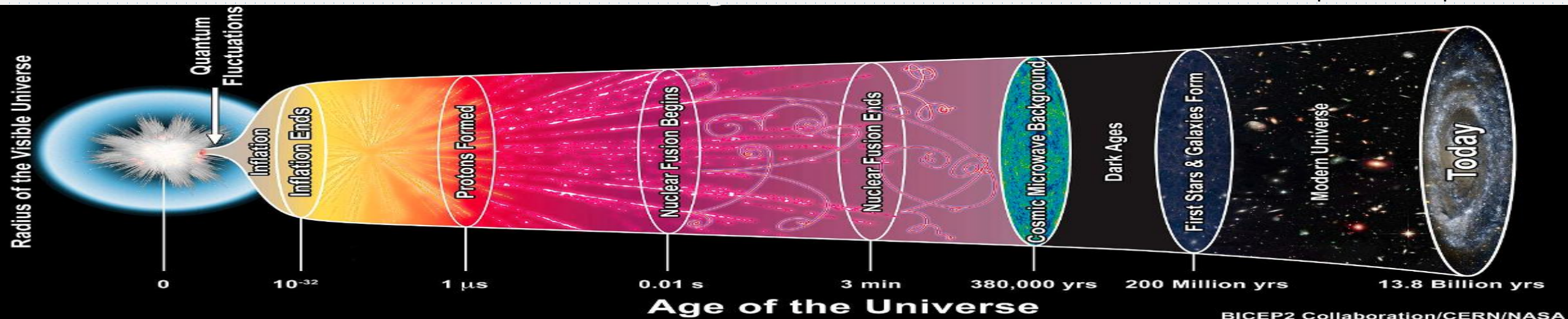
© Nobel Media AB. Photo: A. Mahmoud
 François Englert Prize share: 1/2
 Peter W. Higgs Prize share: 1/2
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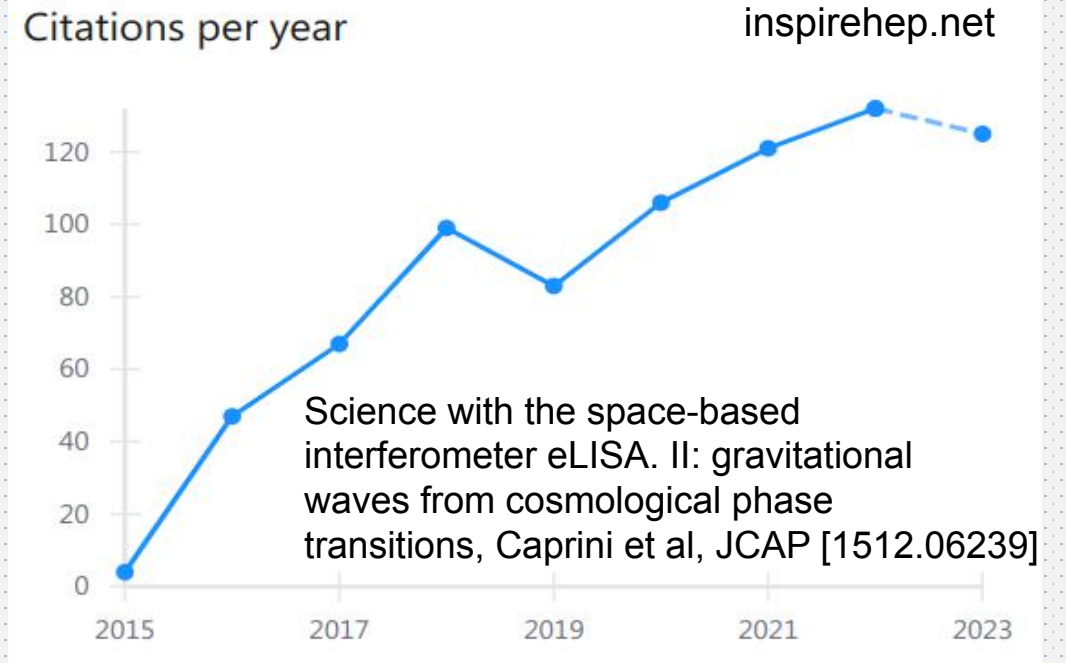
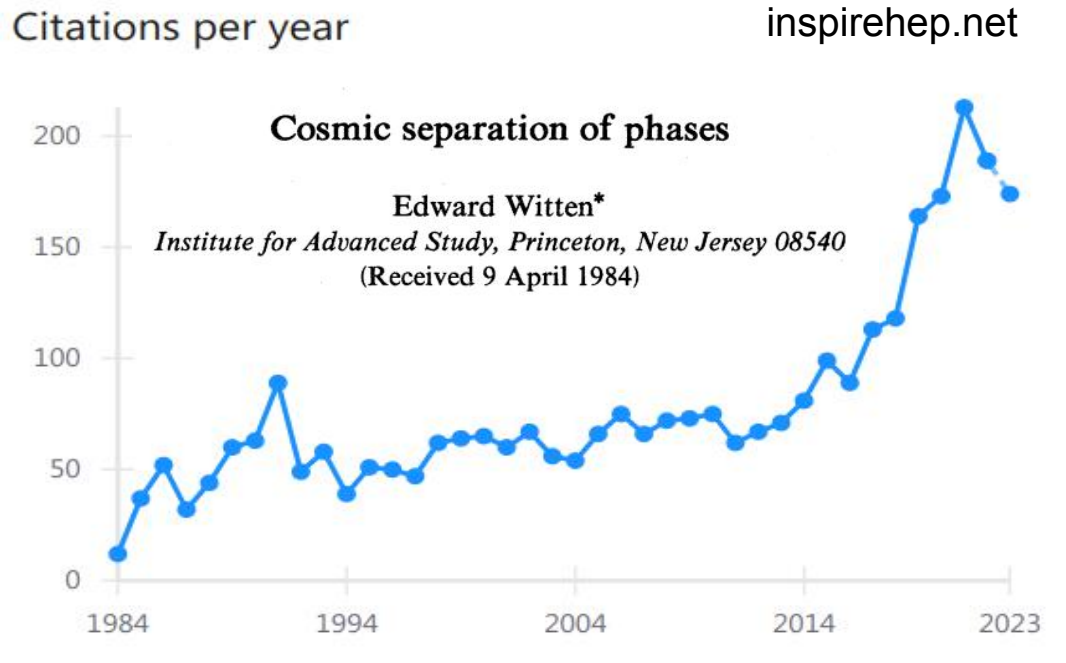
Electroweak Phase Transition

$$SU(3)_C \times SU(2)_L \times U(1)_Y \rightarrow SU(3)_C \times U(1)_{EM}$$

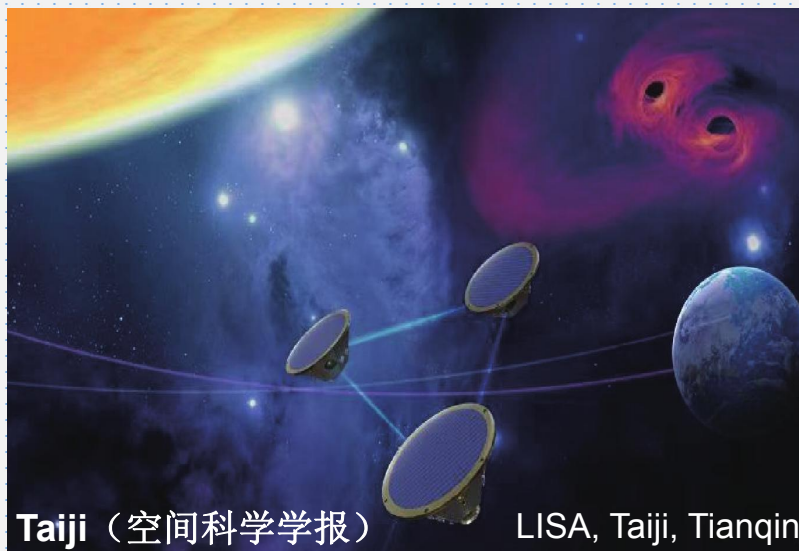


Temperature drops





中国脉冲星测时阵列 (CPTA)

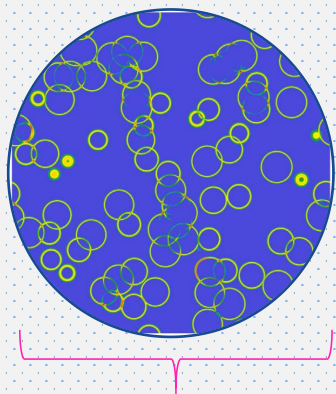


Taiji (空间科学学报) LISA, Taiji, Tianqin



ligo.caltech.edu

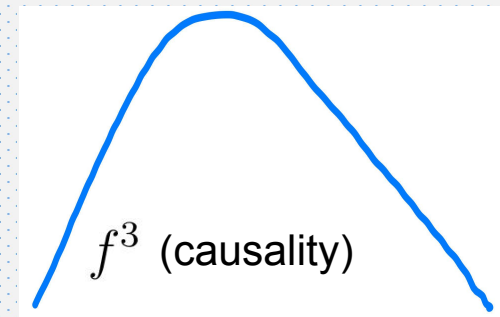
Properties



Horizon size: $1/H^*$

$$f_{\text{now}} = 1.65 \times 10^{-5} \left(\frac{f_{\text{PT}}}{\beta} \right) \left(\frac{\beta}{H_*} \right) \left(\frac{T_*}{100\text{GeV}} \right) \left(\frac{g_*}{100} \right)^{1/6} \text{ Hz}$$

~100-1000



Cai, Pi, Sasak, PRD [1909.13728]

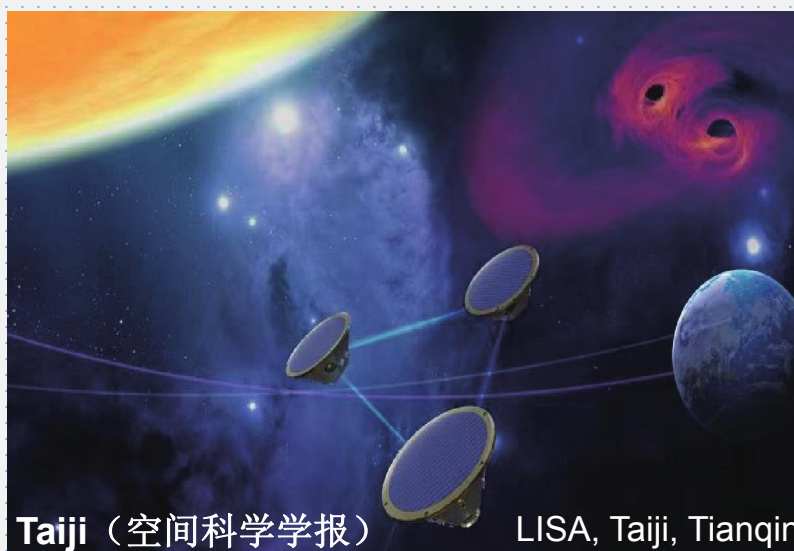
nHz (~100MeV) QCD scale

~mHz : (~100GeV) weak scale

~100Hz (~PeV - EeV) high scale



中国脉冲星测时阵列 (CPTA)



Taiji (空间科学学报)

LISA, Taiji, Tianqin



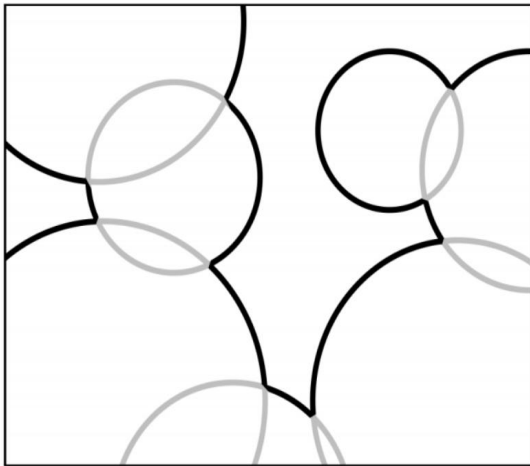
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Gravitational Wave Sources

The current understanding:

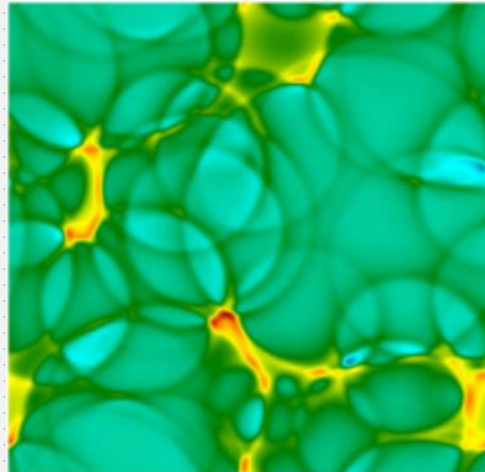
$$\square \bar{h}_{\mu\nu} = -\frac{16\pi G}{c^4} T_{\mu\nu}$$

energy near the wall



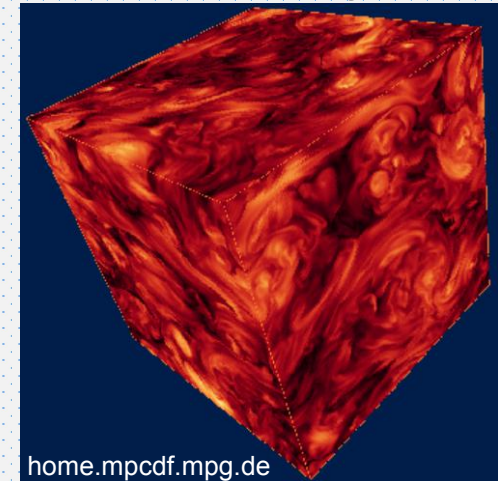
Bubble Collisions

fluid kinetic energy



Sound Waves

turbulent fluid + magnetic field



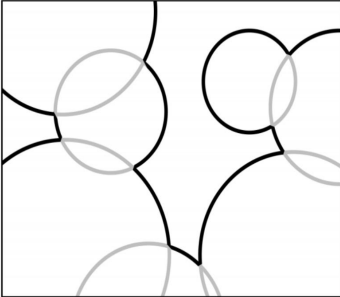
Magnetohydrodynamic Turbulence

GW Spectra

Energy density Spectrum

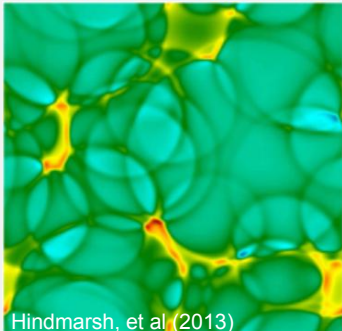
$$\Omega_{\text{GW}}(f) = \frac{d\rho_{\text{GW}}}{\rho_c d \log f}$$

bubble collision



$$\Omega_{\text{coll}}(f)h^2 = 1.67 \times 10^{-5} \Delta \left(\frac{H_{\text{pt}}}{\beta} \right)^2 \left(\frac{\kappa_{\phi} \alpha}{1 + \alpha} \right)^2 \times \left(\frac{100}{g_*} \right)^{1/3} S_{\text{env}}(f),$$

sound waves

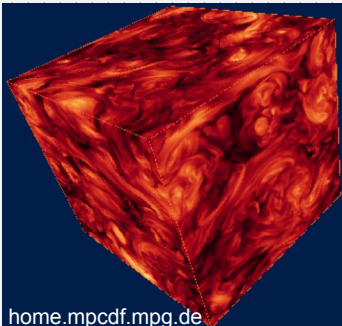


$$\Omega_{\text{sw}}(f)h^2 = 2.65 \times 10^{-6} \left(\frac{H_{\text{pt}}}{\beta} \right) \left(\frac{\kappa_{\text{sw}} \alpha}{1 + \alpha} \right)^2 \left(\frac{100}{g_*} \right)^{1/3} \times v_w \left(\frac{f}{f_{\text{sw}}} \right)^3 \left(\frac{7}{4 + 3(f/f_{\text{sw}})^2} \right)^{7/2} \Upsilon(\tau_{\text{sw}}),$$

$$\Upsilon = 1 - (1 + 2\tau_{\text{sw}} H_{\text{pt}})^{-1/2} \quad (\text{RD})$$

HG, Sinha, Vagie, White, JCAP [2007.08537]

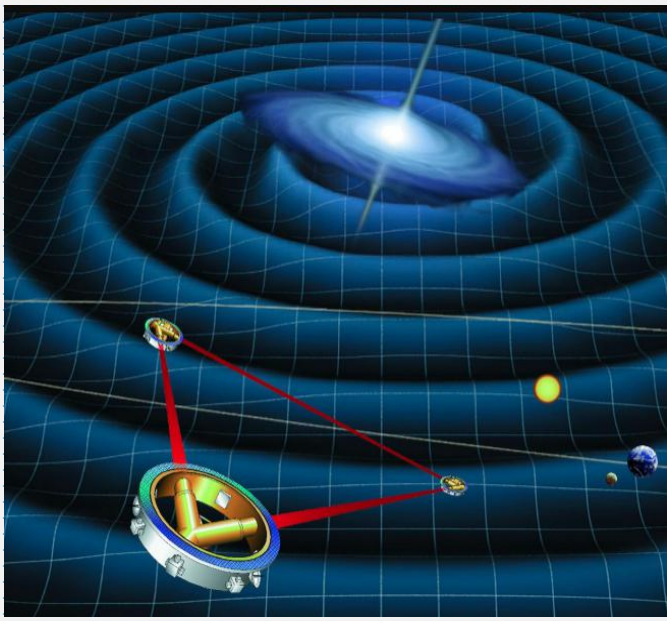
MHD



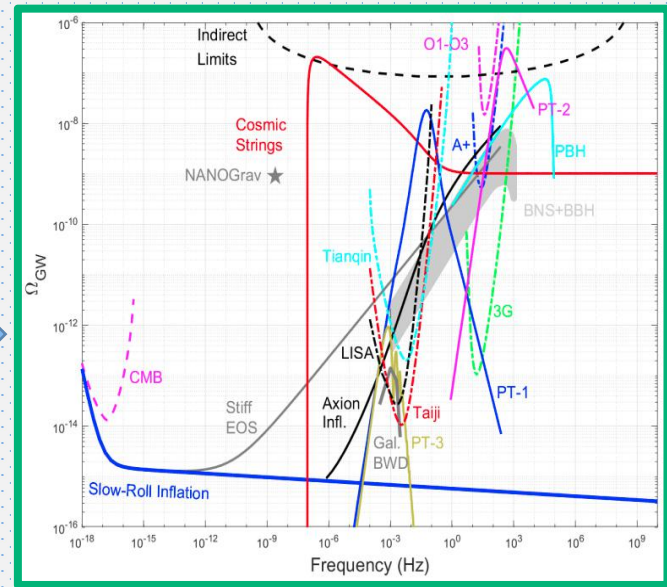
$$h^2 \Omega_{\text{turb}}(f) = 3.35 \times 10^{-4} \left(\frac{H_*}{\beta} \right) \left(\frac{\kappa_{\text{turb}} \alpha}{1 + \alpha} \right)^{\frac{3}{2}} \left(\frac{100}{g_*} \right)^{1/3} v_w S_{\text{turb}}(f)$$

Chiara Caprini et al, JCAP [1512.06239]

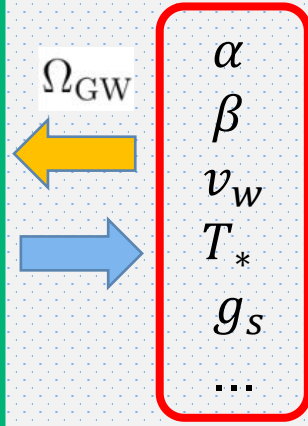
From Theory to Experiment



LIGO, LISA/Taiji/Tianqin, PTA, ...



Gravitational Wave Spectrum



Phase Transition Parameters

Standard Model of Elementary Particles

	three generations of matter (fermions)			interactions / force carriers (bosons)	
	I	II	III		
mass	$\approx 2.2 \text{ MeV}/c^2$	$\approx 1.28 \text{ GeV}/c^2$	$\approx 173.1 \text{ GeV}/c^2$	0	$\approx 124.97 \text{ GeV}/c^2$
charge	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0
QUARKS	u up	c charm	t top	g gluon	H higgs
	$\approx 4.7 \text{ MeV}/c^2$	$\approx 96 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$	0	
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
	d down	s strange	b bottom	γ photon	BSM
	$\approx 0.511 \text{ MeV}/c^2$	$\approx 105.66 \text{ MeV}/c^2$	$\approx 1.7768 \text{ GeV}/c^2$	0	$\approx 91.19 \text{ GeV}/c^2$
	-1	-1	-1	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
LEPTONS	e electron	μ muon	τ tau	Z Z boson	GAUGE BOSONS
	$< 1.0 \text{ eV}/c^2$	$< 0.17 \text{ MeV}/c^2$	$< 18.2 \text{ MeV}/c^2$	$\approx 80.39 \text{ GeV}/c^2$	VECTOR BOSONS
	0	0	0	± 1	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson	SCALAR BOSONS

Particle Physics Model



Problem: parameter degeneracy

Models	Strong 1 st order phase transition	GW signal	Cold DM	Dark Radiation and small scale structure
SM charged				
Triplet [20–22]	✓	✓	✓	✗
complex and real Triplet [23] (Georgi-Machacek model)	✓	✓	✓	✗
Multiplet [24]	✓	✓	✓	
2HDM [25–30]	✓	✓		✗
MLRSM [31]	✓	✓	✗	✗
NMSSM [32–36]	✓	✓	✓	✗
SM uncharged				
S_ν (xSM) [37–49]	✓	✓	✗	✗
2 S_ν 's [50]	✓	✓	✓	✗
S_c (cxSM) [49, 51–54]	✓	✓	✓	✗
$U(1)_D$ (no interaction with SM) [55]	✓	✓	✓	✗
$U(1)_D$ (Higgs Portal) [56]	✓	✓	✓	
$U(1)_D$ (Kinetic Mixing) [57]	✓	✓	✓	
Composite $SU(7)/SU(6)$ [58]	✓	✓	✓	
$U(1)_L$ [59]	✓	✓	✓	✗
$SU(2)_D \rightarrow$ global $SO(3)$ by a doublet [60–62]			✓	✗
$SU(2)_D \rightarrow U(1)_D$ by a triplet [63–65]			✓	✓
$SU(2)_D \rightarrow Z_2$ by two triplets [66]			✓	✗
$SU(2)_D \rightarrow Z_3$ by a quadruplet [67, 68]			✓	✗
$SU(2)_D \times U(1)_{B-L} \rightarrow Z_2 \times Z_2$ by a quintuplet and a S_c [69]			✓	✗
$SU(2)_D$ with two dark Higgs doublets [70]	✓	✓	✗	✗
$SU(3)_D \rightarrow Z_2 \times Z_2$ by two triplets [62, 71]			✓	✗
$SU(3)_D$ (dark QCD) (Higgs Portal) [72, 73]	✓	✓	✓	
$G_{SM} \times G_{D,SM} \times Z_2$ [74]	✓	✓	✓	
$G_{SM} \times G_{D,SM} \times G_{D,SM} \dots$ [75]	✓	✓	✓	
Current work				
$SU(2)_D \rightarrow U(1)_D$ (see the text)	✓	✓	✓	✓

Ghosh, HG, Han, Liu, JHEP [2012.09758]

Many models can lead to the same PT parameter values

Solutions: New Observables

- Anisotropy
Geller, Hook, Sundrum, Yuhsin Tsai, PRL [1803.10780]
Li, Huang, Wang, Zhang, PRD [2112.01409]
Li, Yan, Huang, PRD [2211.03368]
- Primordial magnetic field
Di, Wang, Zhou, Bian, Cai, PRL [2012.15625]
Yang, Bian, PRD [2102.01398], ...
- Primordial black holes and solitons
Hong, Jung, Xie, PRD [2008.04430]
Kawana, Xie, PLB [2106.00111]
Liu, Bian, Cai, Guo, Wang, PRD [2106.05637]
Lu, Kawana, Xie, PRD [2202.03439]
- Curvature perturbations
Liu, Bian, Cai, Guo, Wang, PRL [2208.14086]
Jiang, Liu, Sun, Wang, PLB [1512.07538]

Anything directly readable from the isotropic GW spectrum?

Dissipative Effects as New Observables

GW depends on (large) bulk velocity of the system

$$h \sim 10^{-22} \frac{M/M_{\odot}}{r/100\text{Mpc}} \left(\frac{v}{c}\right)^2$$

Dissipative effects dissipate away the bulk kinetic energy (leaves imprint)

$$\rho \left(\frac{\partial \mathbf{v}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{v} \right) = -\nabla p + \mu \nabla^2 \mathbf{v} + \left(\zeta + \frac{1}{3} \mu \right) \nabla (\nabla \cdot \mathbf{v})$$

Navier–Stokes equations (Newtonian fluid mechanics)



GW calculation requires: relativistic (magneto-)hydrodynamics

Sound Waves

Usually the dominant source (Hindmarsh, Huber, Rummukainen, Weir, PRL [1304.2433])

$$T^{ij} \propto (p + e)v^i v^j$$

$$h^2 \Omega_{\text{sw}}(f) = 2.65 \times 10^{-6} \left(\frac{100}{g_*}\right)^{\frac{1}{3}} \left(\frac{H_*}{\beta}\right) \left(\frac{\kappa_{\text{sw}} \alpha}{1 + \alpha}\right)^2 v_w S_{\text{sw}}(f) \Upsilon(\tau_{\text{sw}})$$

$$S_{\text{sw}}(f) = \left(\frac{f}{f_{\text{sw}}}\right)^3 \left[\frac{7}{4 + 3(f/f_{\text{sw}})^2}\right]^{7/2} \quad f_* = \frac{2\beta}{\sqrt{3}v_w} \approx \frac{3.4}{R_*}$$

Hindmarsh, Huber, Rummukainen, Weir, PRD [1504.03291]

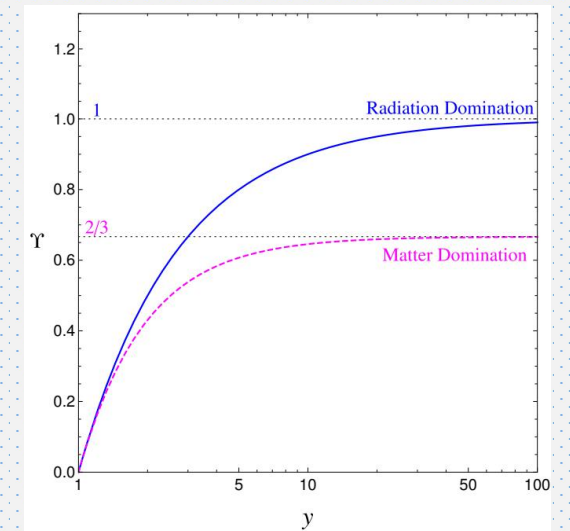
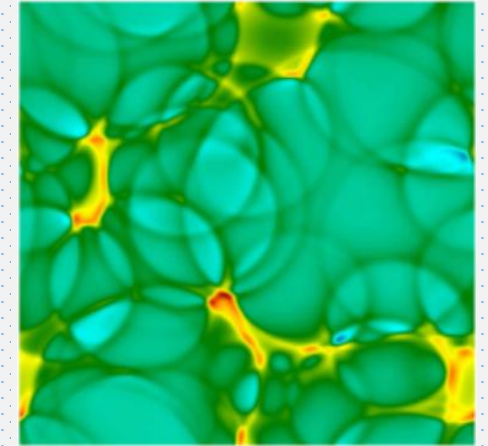
Slight different fit obtained by the same group, PRD [1704.05871]

$$\Upsilon = 1 - (1 + 2\tau_{\text{sw}} H_{\text{pt}})^{-1/2} \quad (\text{radiation domination})$$

HG, Sinha, Vagie, White, JCAP [2007.08537]

$$\Omega_{\text{sw}}(f \gtrsim f_{\text{peak}}) \propto f^{-4}$$

$$\Omega_{\text{sw}}(f \lesssim f_{\text{peak}}) \propto f^3$$



Sound Waves: Recent Development

Analytical Modelling

- Refine the sound shell model
- Synergy with simulations

Sound Shell Model

Hindmarsh, PRL [1608.04735]

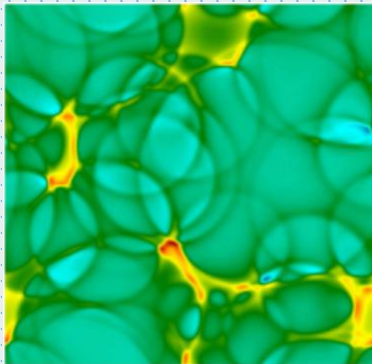
Hindmarsh, Hijazi, JCAP [1909.10040]

HG, Sinha, Vagie, White, JCAP [2007.08537]

Cai, Wang, Yuwen, PRD Letter [2305.00074]

Pol, Procacci, Caprini [2308.12943]

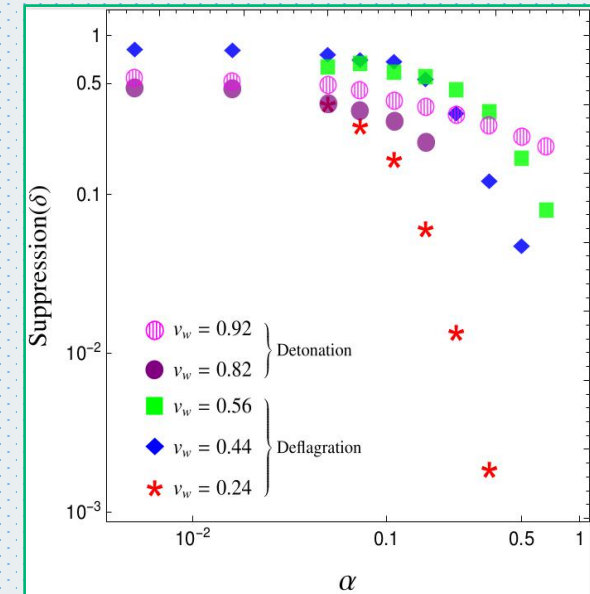
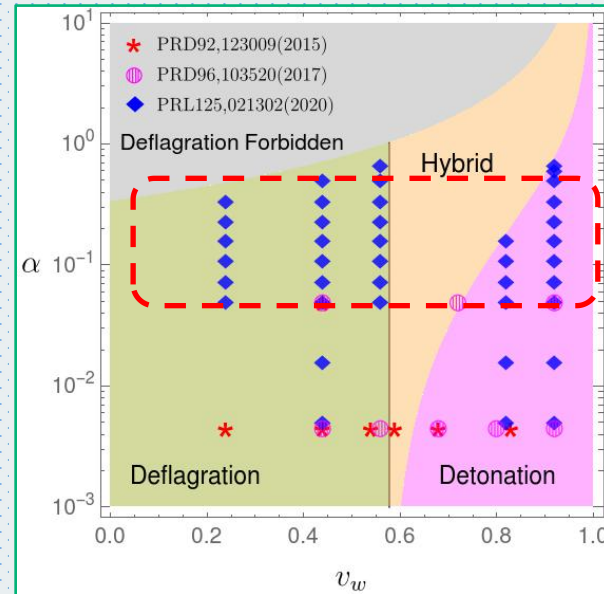
$$v_{\mathbf{q}}^i = \sum_{n=1}^{N_b} v_{\mathbf{q}}^{i(n)}$$



Numerical Simulation

- Suppression found for strong transitions with small v_w
- Need to cover more parameter space (very strong PT)

$$h^2 \Omega_{\text{sw}}(f) = 2.65 \times 10^{-6} \left(\frac{100}{g_*} \right)^{\frac{1}{3}} \left(\frac{H_*}{\beta} \right) \left(\frac{\kappa_{\text{sw}} \alpha}{1 + \alpha} \right)^2 v_w S_{\text{sw}}(f) \Upsilon(\tau_{\text{sw}})$$

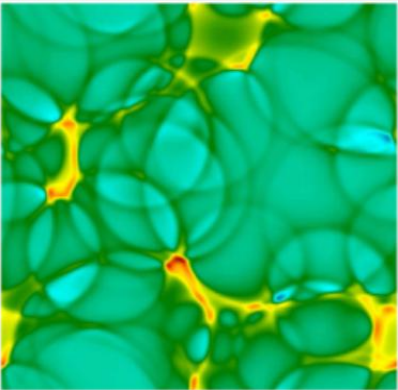


Cutting, Hindmarsh, Weir, PRL [1906.00480]

Effects of Dissipation

- Disturbed fluid comes into rest eventually

$$v^i(\eta, \mathbf{x}) = \int \frac{d^3q}{(2\pi)^3} [v_{\mathbf{q}}^i e^{-i\omega\eta + i\mathbf{q}\cdot\mathbf{x}} + c.c.]$$



$$v_{\mathbf{q}}^i(\eta) \propto \exp \left[- \int \Gamma(\mu, \zeta, \xi) d\eta \right]$$

$$\Gamma \propto q^2$$

shear viscosity bulk viscosity

$$\Delta T^{ij} = -\mu \left(\frac{\partial U_i}{\partial x^j} + \frac{\partial U_j}{\partial x^i} - \frac{2}{3} \delta_{ij} \nabla \cdot \mathbf{U} \right) - \zeta \delta_{ij} \nabla \cdot \mathbf{U},$$

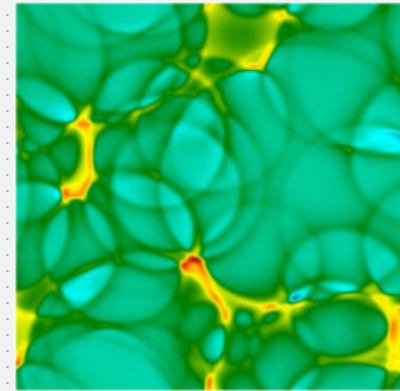
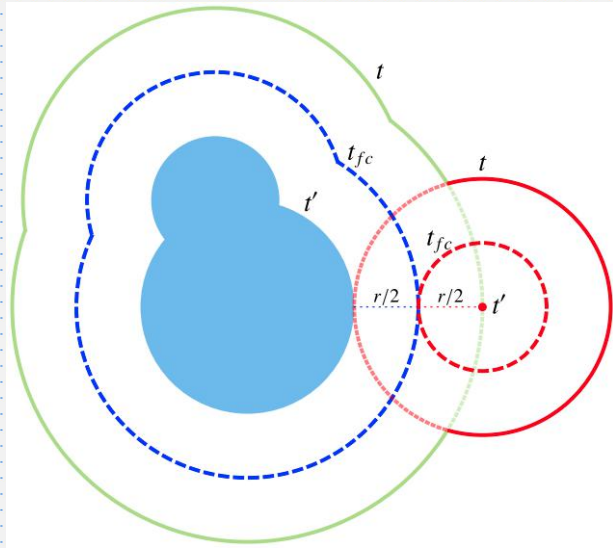
$$\Delta T^{i0} = -\chi \left(\frac{\partial T}{\partial x^i} + T \dot{U}_i \right). \tag{1}$$

thermal conduction

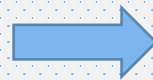
Weinberg, ApJ, 1971

Euler equation -> Navier–Stokes equations
 -> Relativistic hydrodynamics

Sound Shell Model with Dissipation



$$v_{\mathbf{q}}^i = \sum_{n=1}^{N_b} v_{\mathbf{q}}^{i(n)}$$

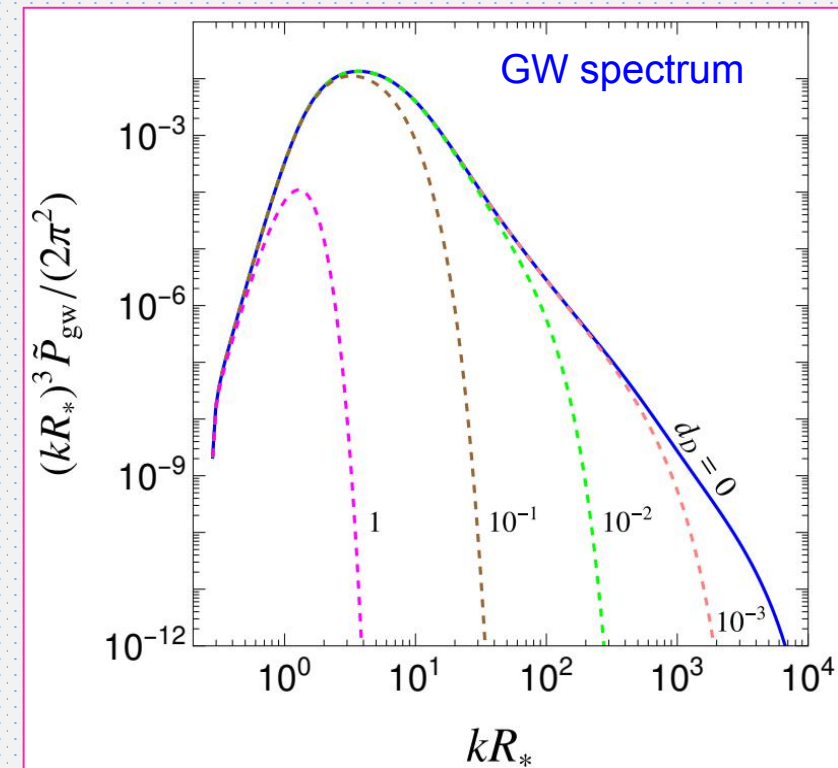
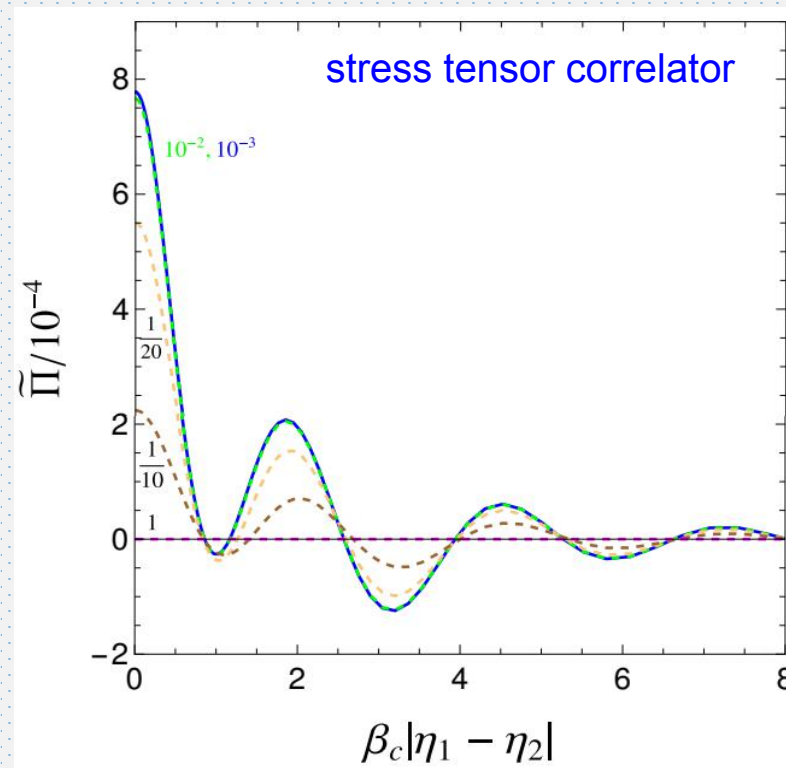
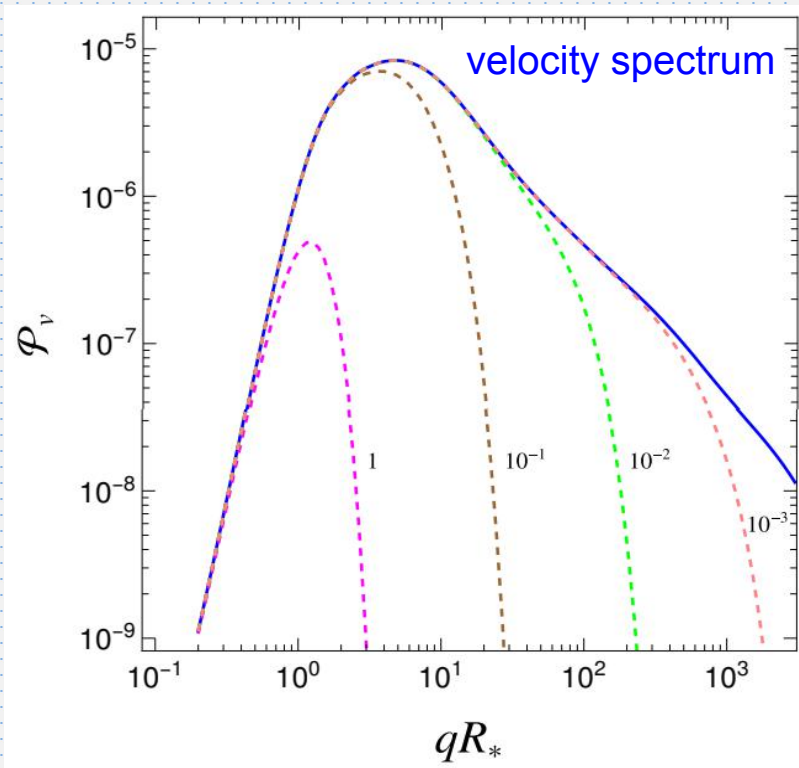


$$v_{\mathbf{q}}^i(\eta) = \sum_{n=1}^{N_b} v_{\mathbf{q}}^{i(n)} \exp \left[- \int_{\eta_d^{(n)}}^{\eta} \Gamma d\bar{\eta} \right] \theta(\eta - \eta_d^{(n)})$$

bubble destruction time
(when SW forms)

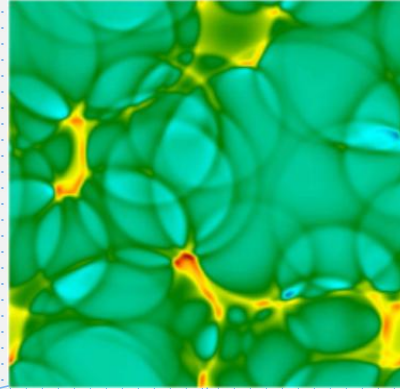
Dampings due to Dissipation

- Velocity power spectrum and stress tensor correlator are generally **non-stationary** (unequal time correlator depends not just on time difference)
- Damping at large frequencies (small scales)



All plots assuming constant effective damping length for illustration (leads to stationary spectrum)

Lifetime of Sound Waves



expansion of the Universe
(dilution)

dissipation
(damping)

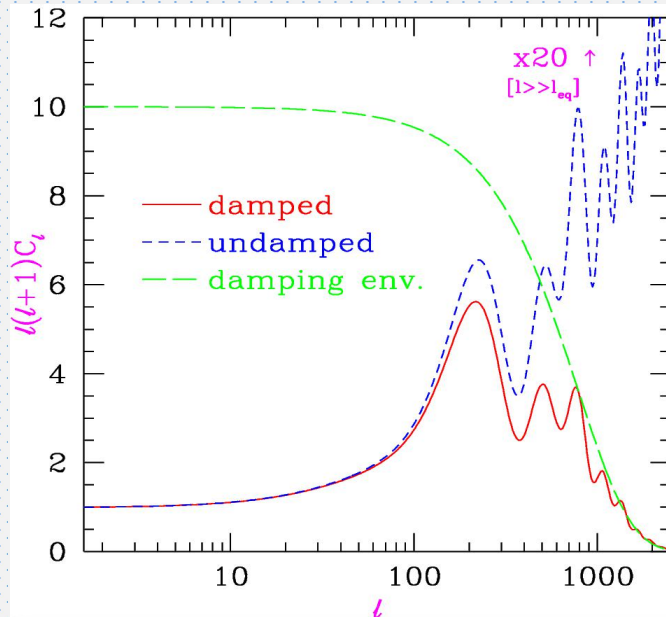
onset of MHD turbulence
(abrupt turnoff)

- Realistic cases: intertwining of these effects (makes GW spectrum **model dependent**)
- GW spectrum carries information about each model (**break parameter degeneracy**)
- Upsilon factor becomes frequency and model dependent

Microscopic Origin

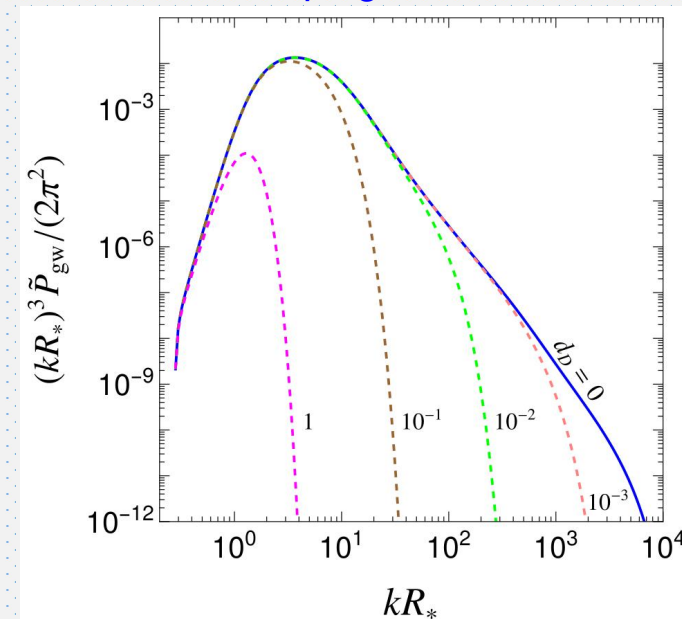
- Viscosity can be strong for phase transitions in the dark sector
- Can also be stronger when BSM physics are included
- Calculable from semi-classical kinetic theory or Green-Kubo relations

Analogy: Silk damping of CMB Anisotropy



Hu, White, ApJ [9609079]

damping of GW

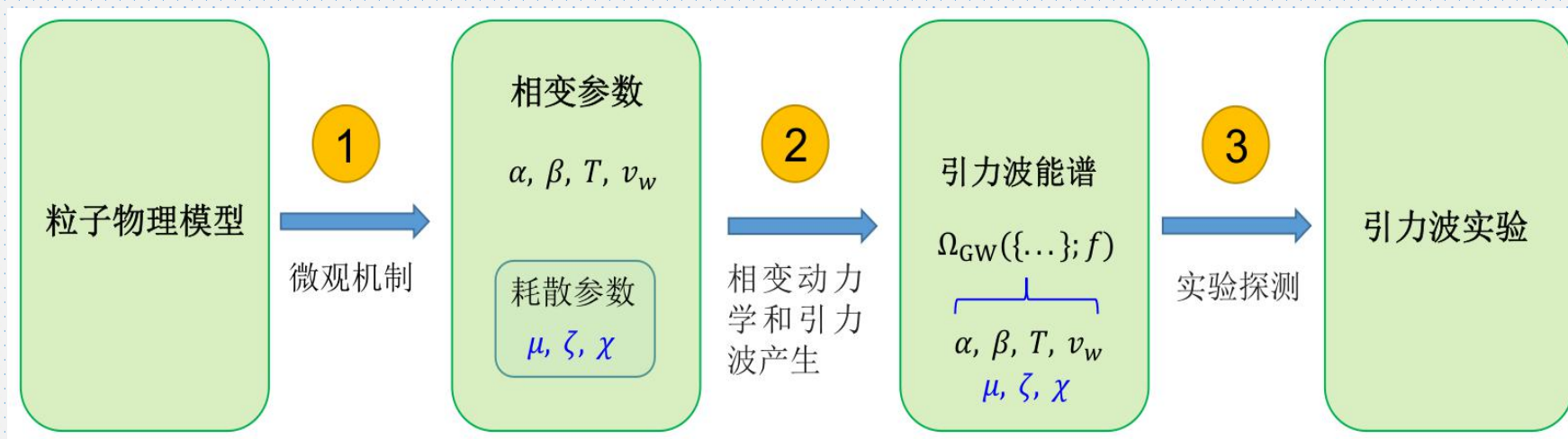


HG [2310.10927]

similar damping for scalar induced GWs: Yu, Wang [2405.02960]

Future Directions

- Microscopic origin (classifications of BSM)
- Dynamics and spectra calculation (simulation and modelling)
- Experimental detection (LIGO, LISA/Taiji/Tianqin, PTA)



Summary

- Dissipative effects can serve as new observables
- New portals to probe microscopic particle (very weak) interactions
- Experimental searches of new spectrum are desired

Thanks!