

# Application of the bateman equation to analyze disequilibrium in the $^{232}\text{Th}$ and $^{238}\text{U}$ chains in low-background detector materials

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## ABSTRACT

In rare-event search experiments such as AMoRE and COSINE, estimating background radioactivity levels and identifying background sources are crucial for background reduction. Typically, isotopes in the  $^{238}\text{U}$  and  $^{232}\text{Th}$  decay chains with relatively short half-lives are grouped together, and secular equilibrium is assumed during background measurements and estimations. During our material screening process, we observed that the  $^{228}\text{Ac}$ - $^{228}\text{Th}$ , and  $^{238}\text{U}$ - $^{226}\text{Ra}$  secular equilibrium was disrupted in several candidate materials. These measurements were conducted using a single HPGe detector at Y2L before 2023, and at Yemilab from 2024 onward.

In one notable case, an aluminum sample showed a significant increase in  $^{226}\text{Ra}$  activity—from below the detection limit (22 mBq/kg) in 2021 to  $893 \pm 48$  mBq/kg in 2025—despite the fact that there was no treatment or exposure that could have lead to radium contamination of the sample. Interestingly, the  $^{234}\text{Th}$  activity remained nearly constant at around 60 Bq/kg, indicating that the  $^{238}\text{U}$  parent activity did not change. Moreover, the  $^{228}\text{Th}/^{228}\text{Ac}$  activity ratio decreased significantly over time. In 2021, the activity values were  $^{228}\text{Ac} = 155 \pm 19$  mBq/kg and  $^{228}\text{Th} = 4030 \pm 206$  mBq/kg, resulting in a ratio of approximately 27. By 2025, the measured values had shifted to  $^{228}\text{Ac} = 421 \pm 30$  mBq/kg and  $^{228}\text{Th} = 1273 \pm 67$  mBq/kg, corresponding to a reduced ratio of around 3.

This behavior suggests that prior radium purification influenced the relative amounts of isotopes in both the  $^{238}\text{U}$  and  $^{232}\text{Th}$  decay chains, resulting in a significant disruption of secular equilibrium.

A clear correlation was observed between the buildup of  $^{226}\text{Ra}$  and the imbalance in the  $^{228}\text{Th}/^{228}\text{Ac}$  activity ratio, highlighting the interconnected nature of these decay series.

These findings underscore the need for time-dependent modeling using the Bateman equation, which can account for such disequilibrium and provide accurate predictions of future activity levels.

By applying this method, we aim to predict the time-dependent activity of long-lived isotopes and enhance the accuracy of background level estimation in upcoming rare-event search experiments, including AMoRE-II and COSINE.

## Collaboration you are representing

AMoRE, COSINE

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