

Precision Neutrino Physics: Status and Outlook in the 3ν Paradigm

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Bari University

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Precision era in neutrino oscillation phenomenology

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Standard 3ν mass-mixing framework parameters

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What we known

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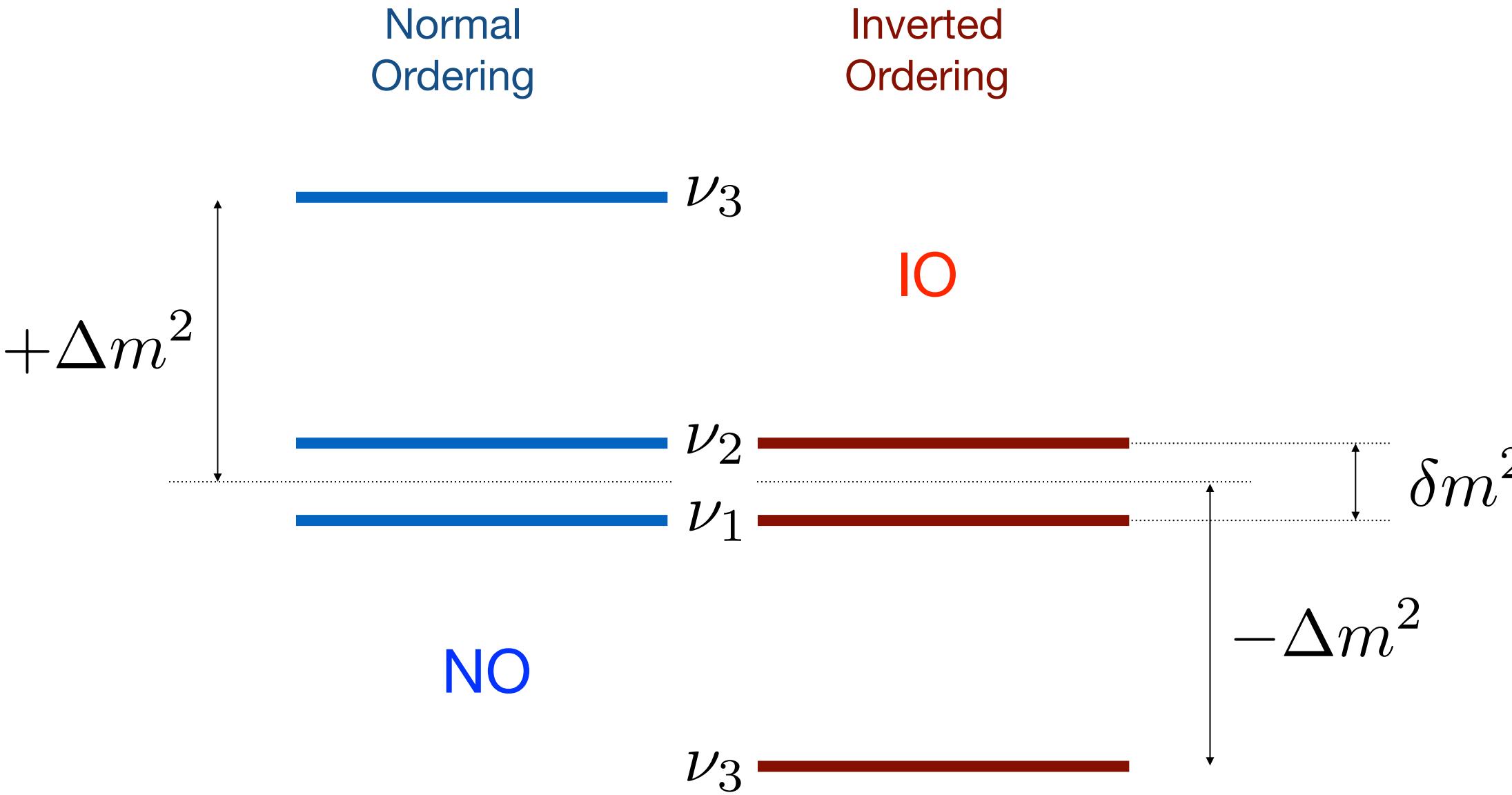
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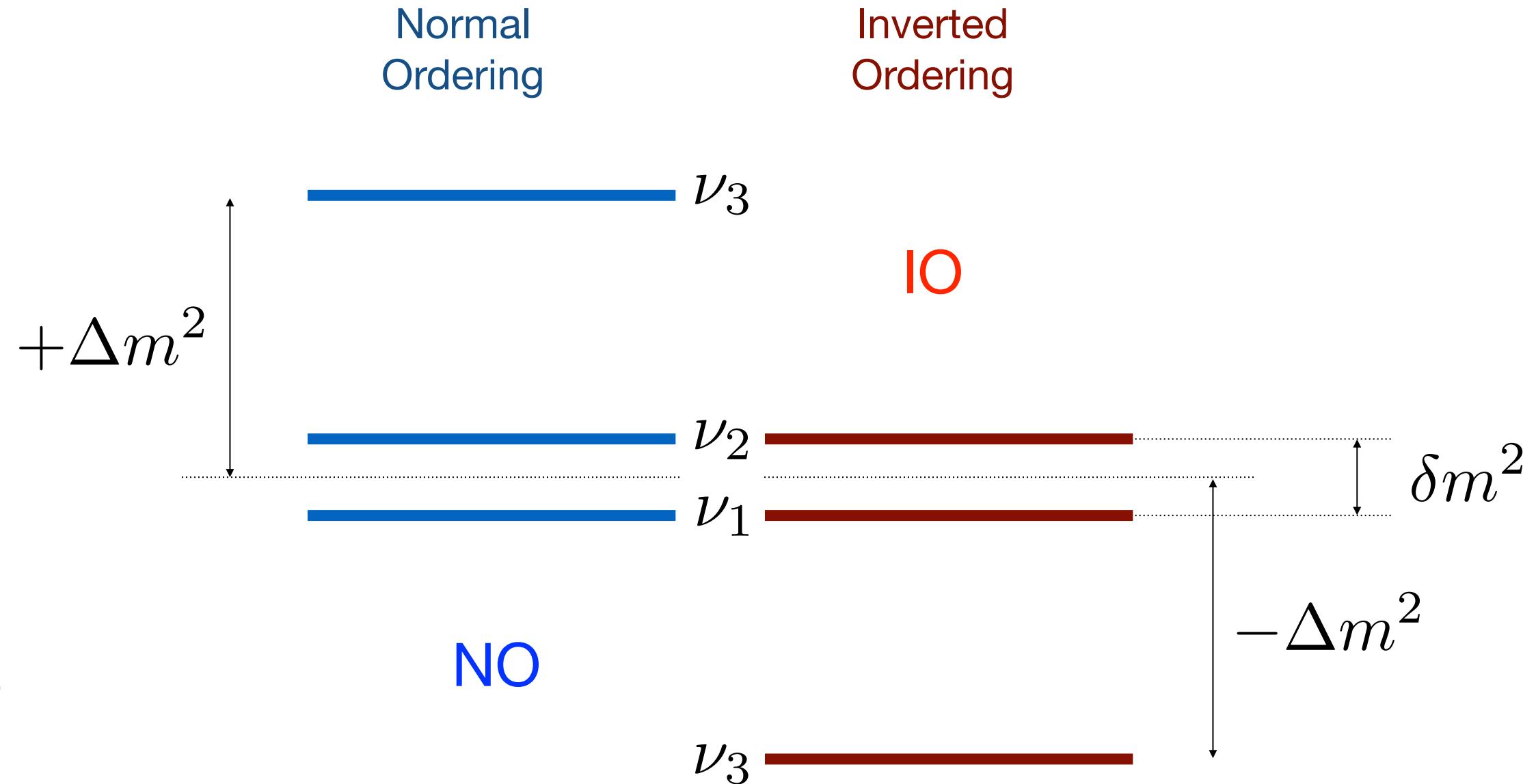
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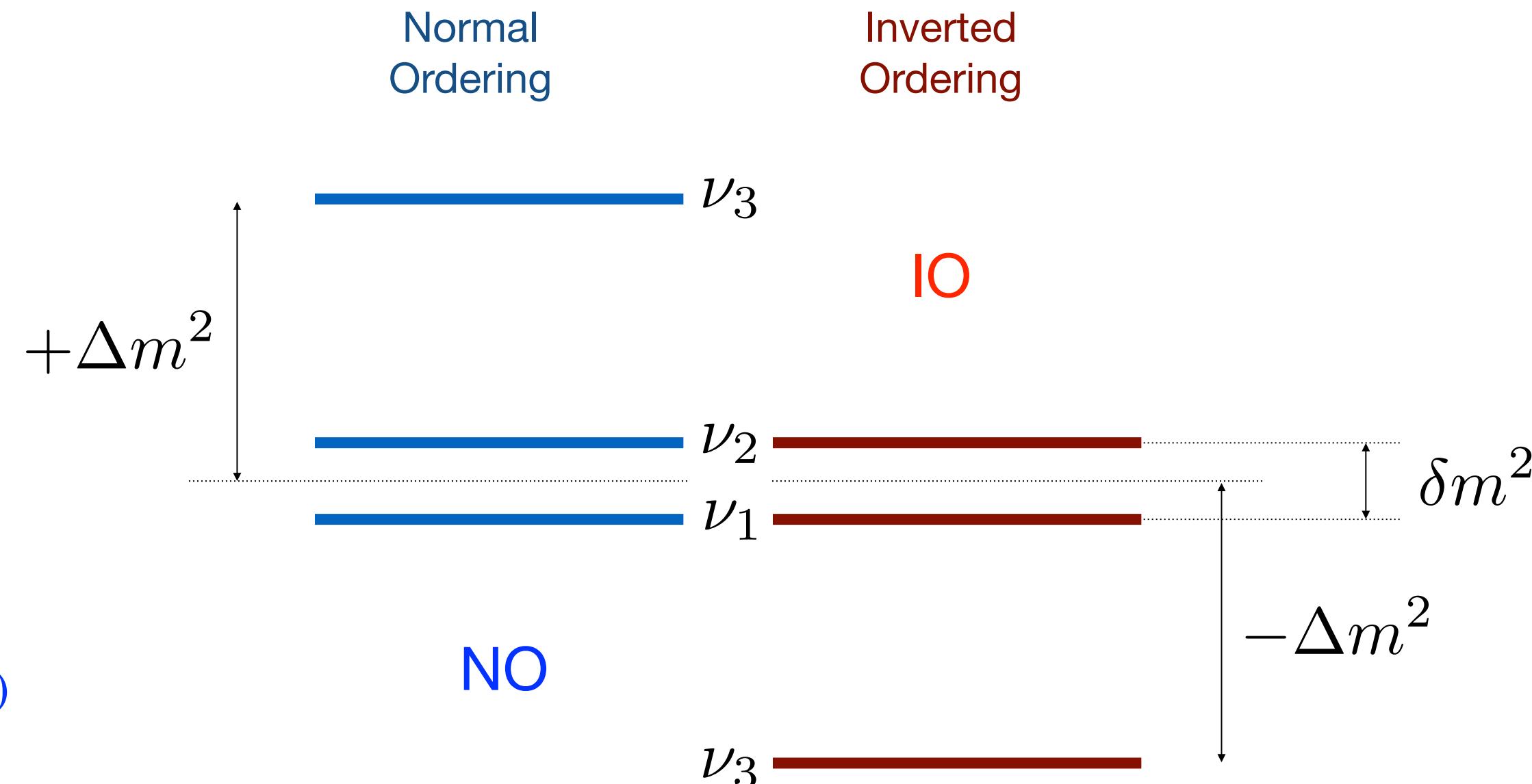
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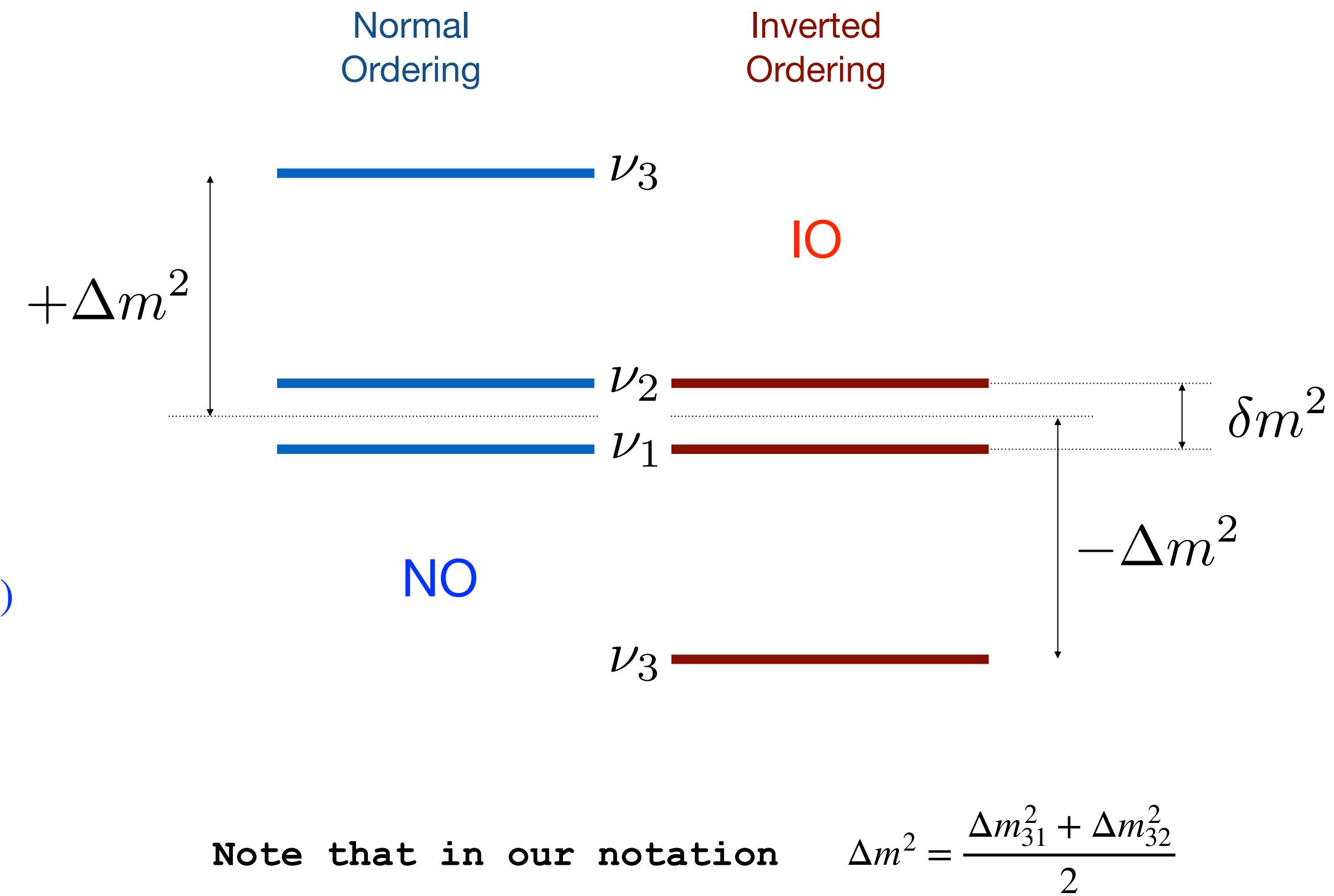
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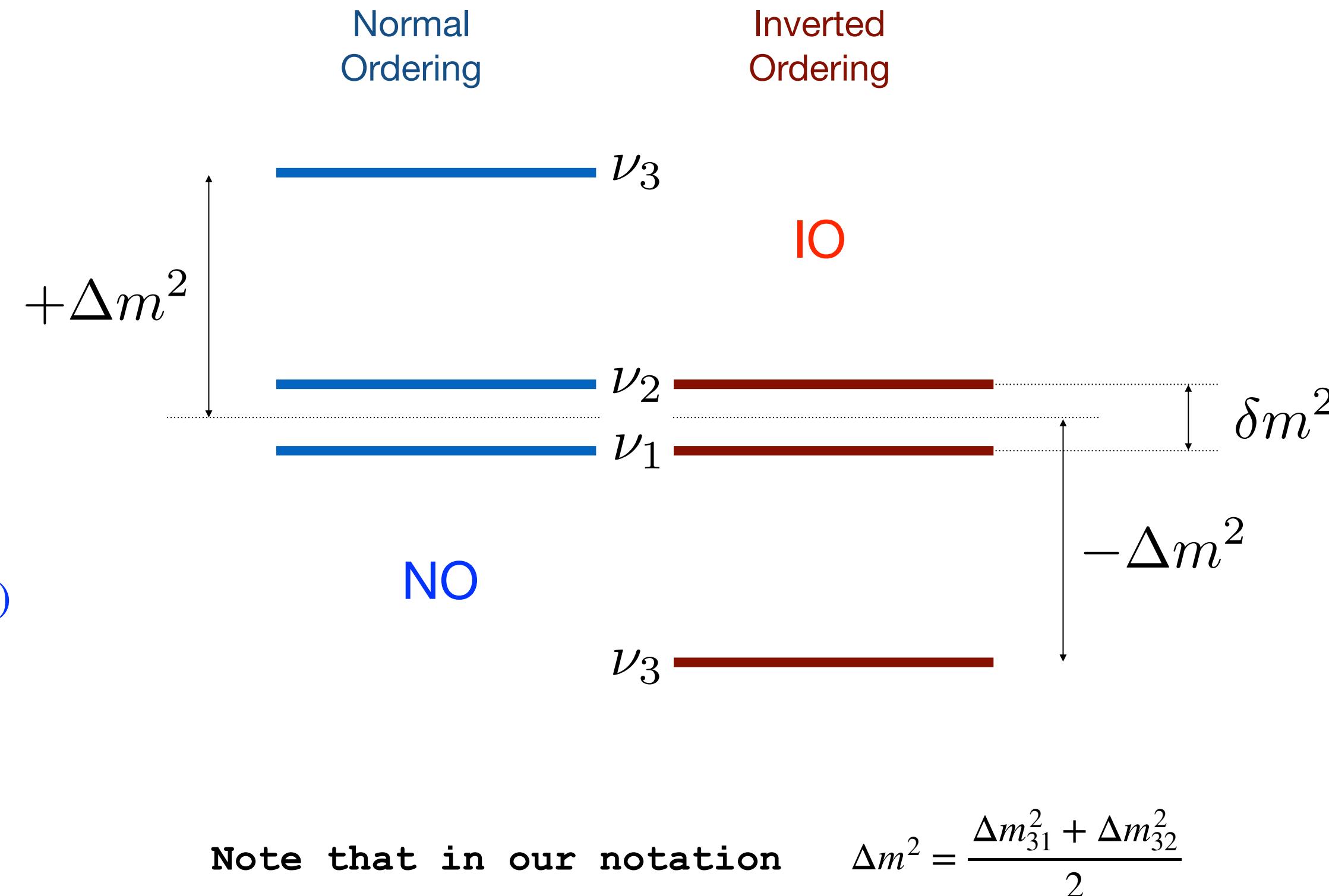
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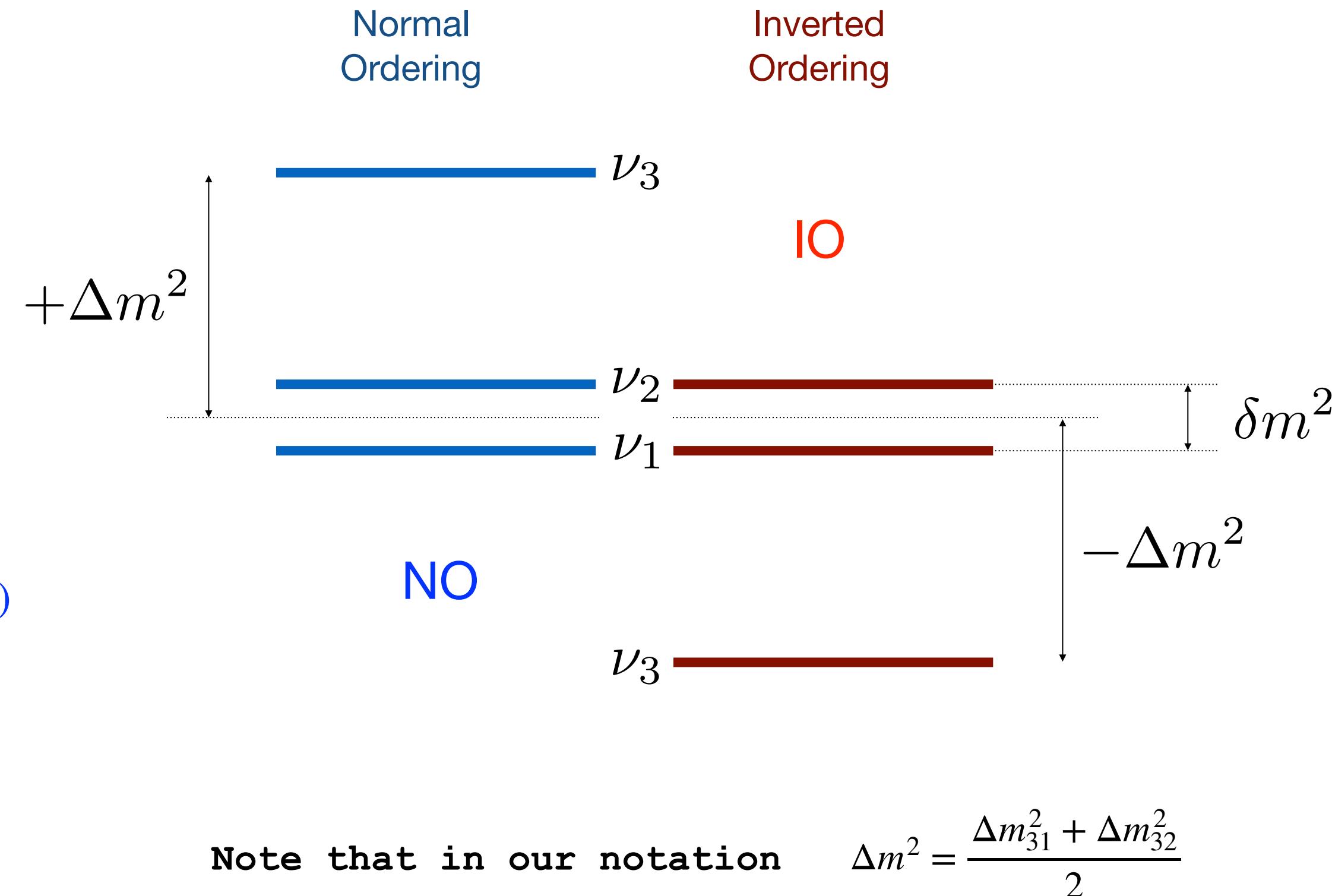
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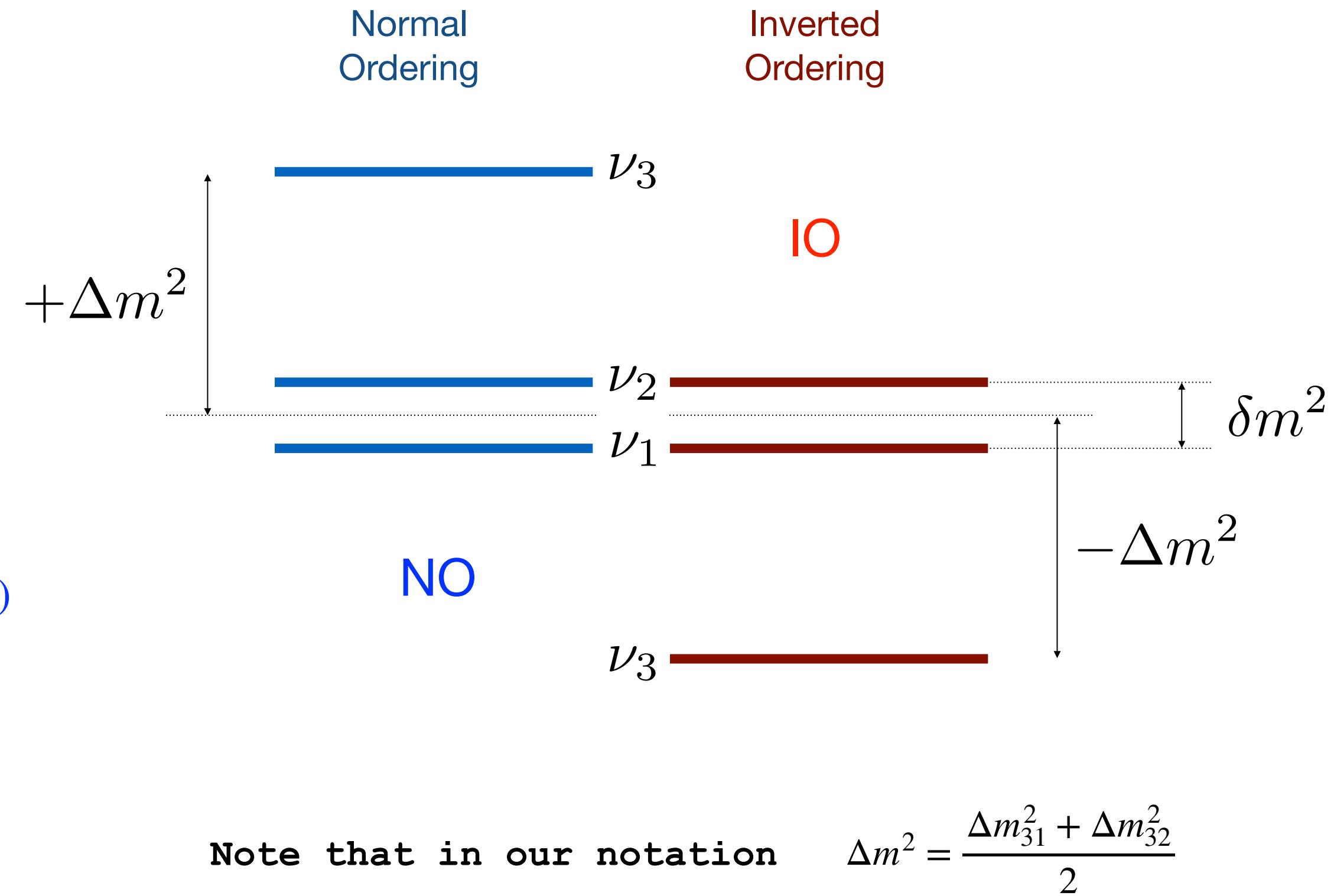
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- Octant of θ_{23}
- Absolute mass scale
- Nature of ν (Dirac/Majorana)

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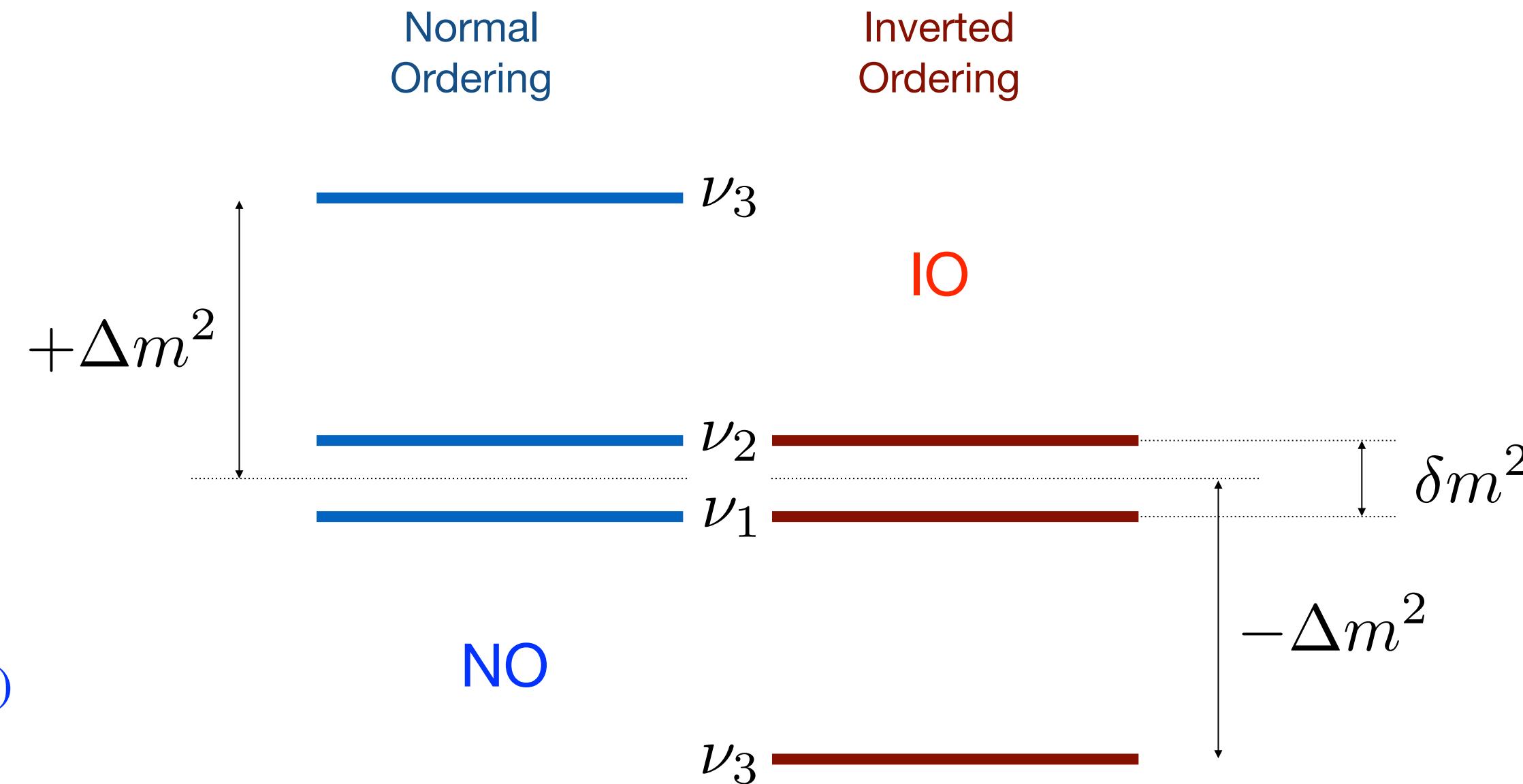
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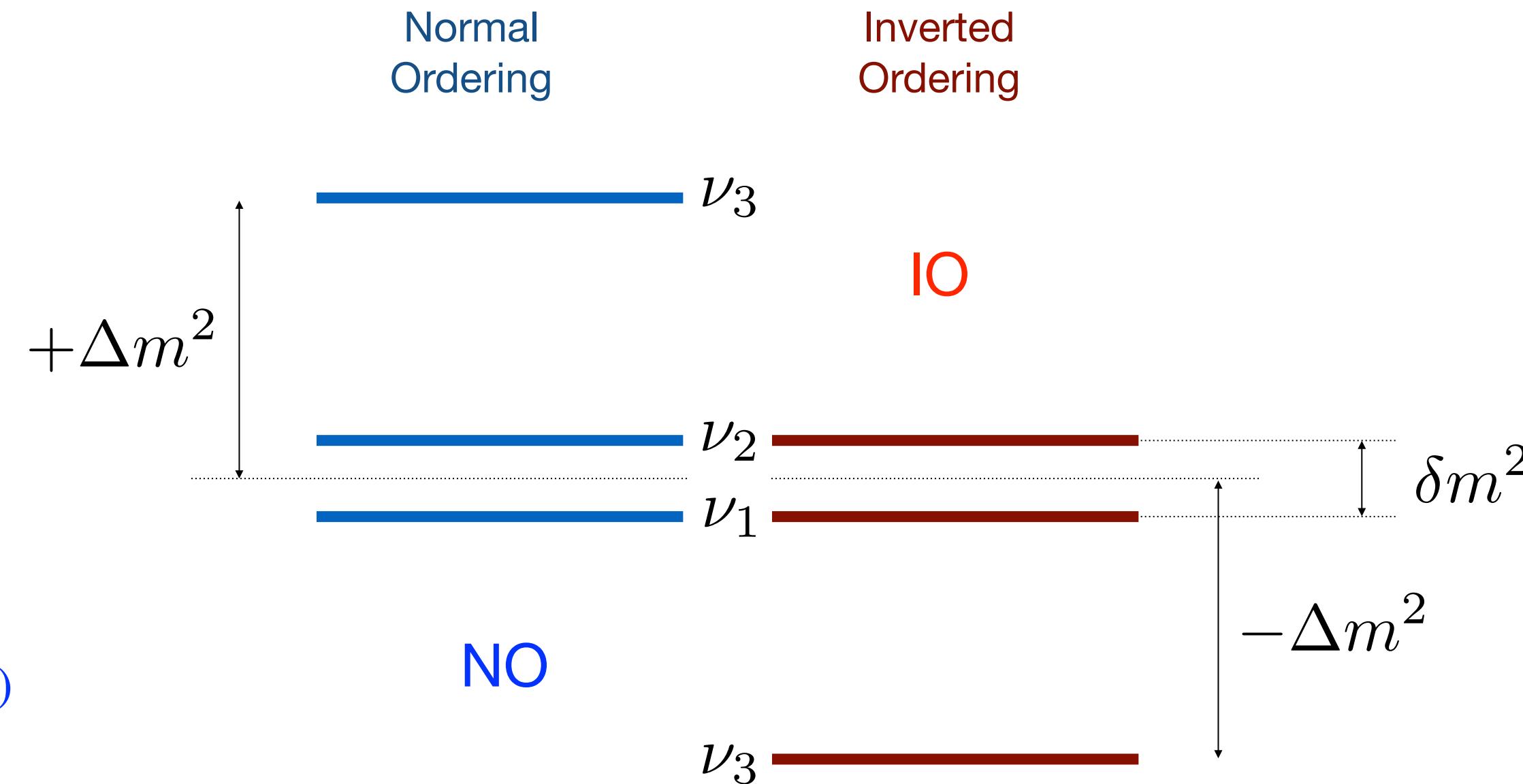
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In particular, JUNO will be sensitive to

$$\Delta m_{ee}^2 = |\Delta m^2| + \frac{1}{2}\alpha(\cos^2 \theta_{12} - \sin^2 \theta_{12})\delta m^2$$

NO: $\alpha = +1$ IO: $\alpha = -1$

Useful analysis sequence in the global analysis of oscillation data

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Long Baseline Accelerator + Solar + KamLAND

minimal set sensitive to all oscillation parameters (δm^2 , Δm^2 , θ_{12} , θ_{23} , θ_{13} , δ_{CP}) and to mass ordering

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Long Baseline Accelerator + Solar + KamLAND + Short Baseline Reactor

Add sensitivity to Δm^2 , θ_{13} + correlations

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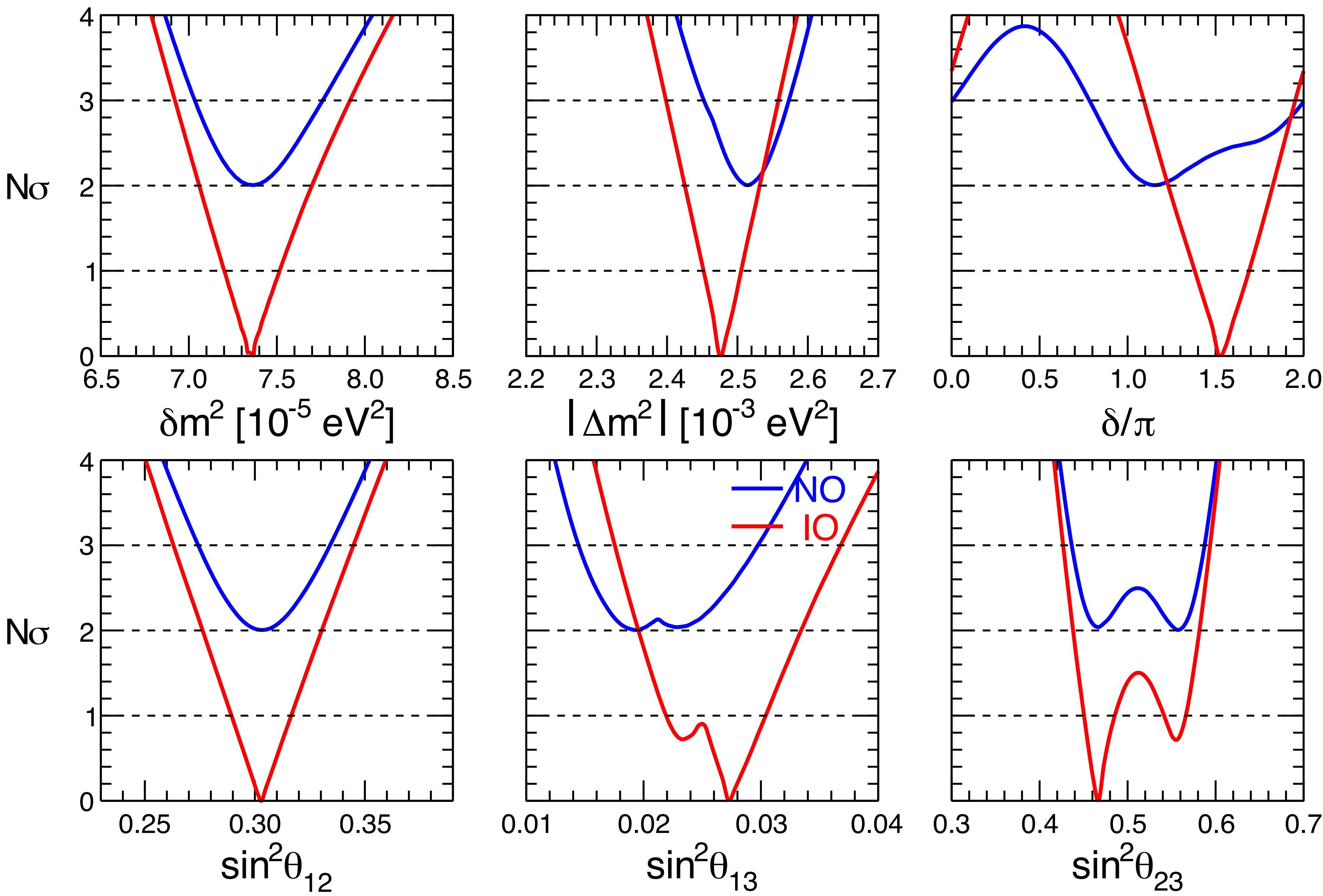
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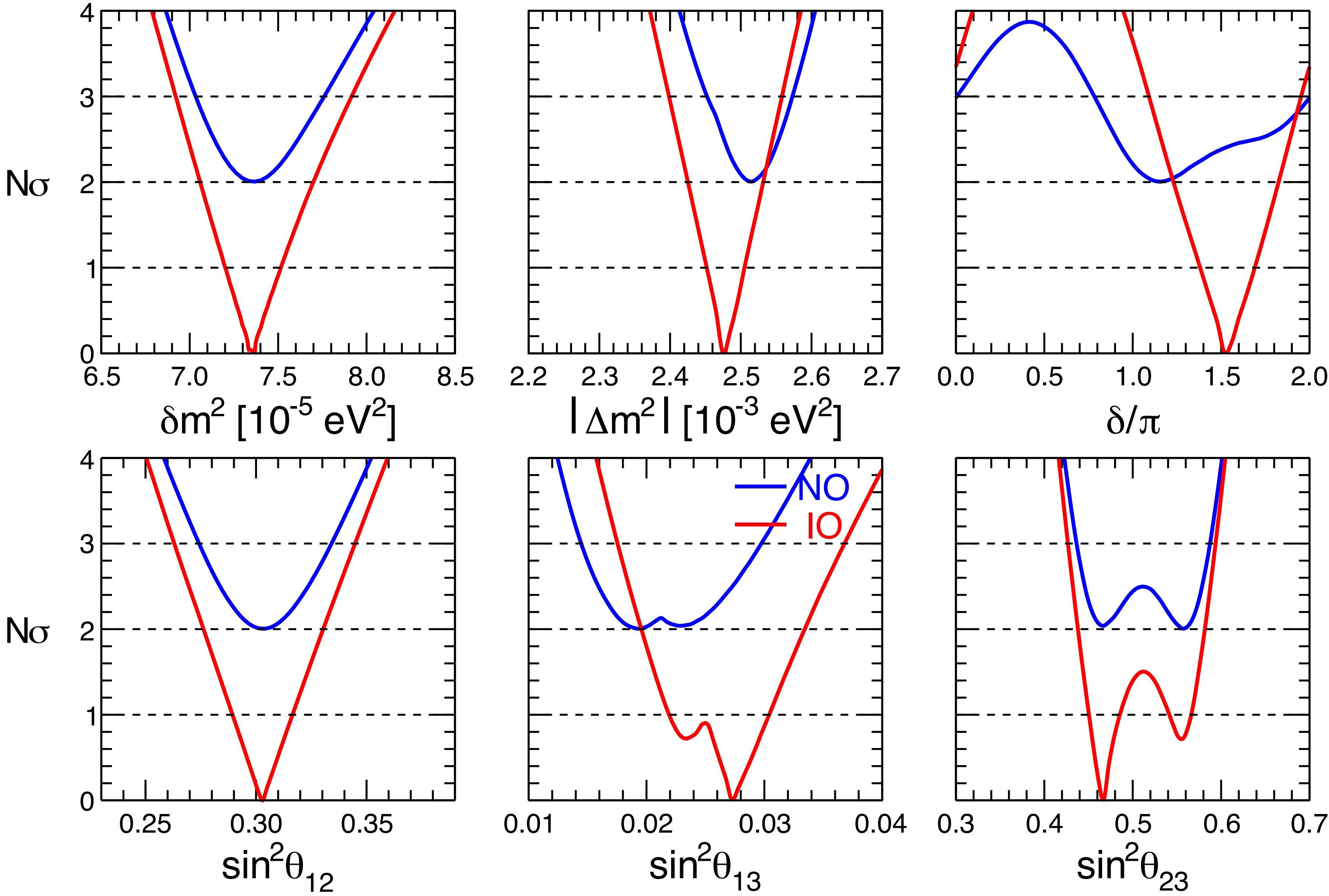
Long Baseline Acc. + Solar + KamLAND + Short Baseline Reactor + Atmospheric

Add sensitivity to Δm^2 , θ_{23} , δ_{CP} and mass ordering

LBL Acc + Solar + KamLAND

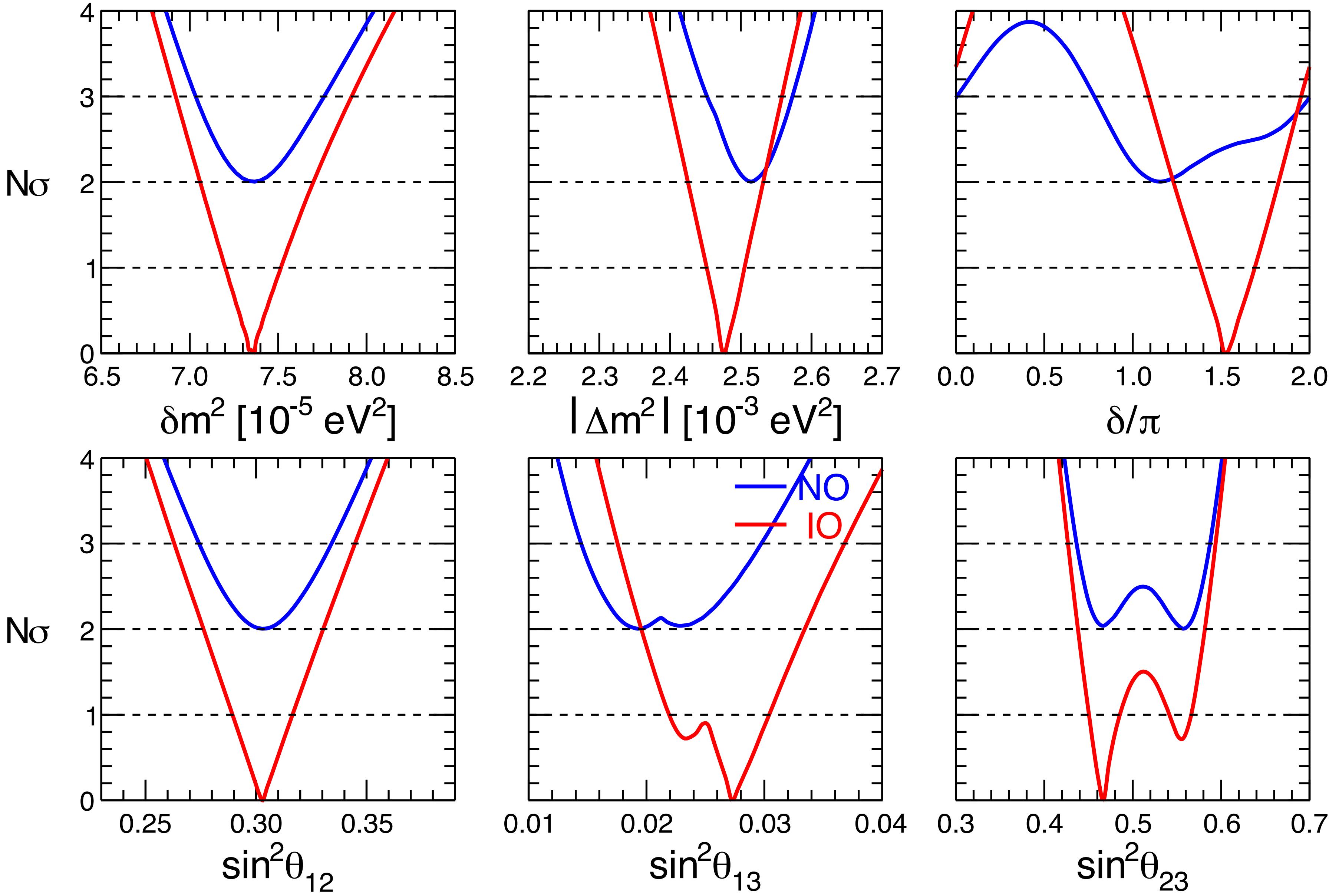


LBL Acc + Solar + KamLAND



T2K and NOvA prefer NO separately, and IO in combination (at 2σ).

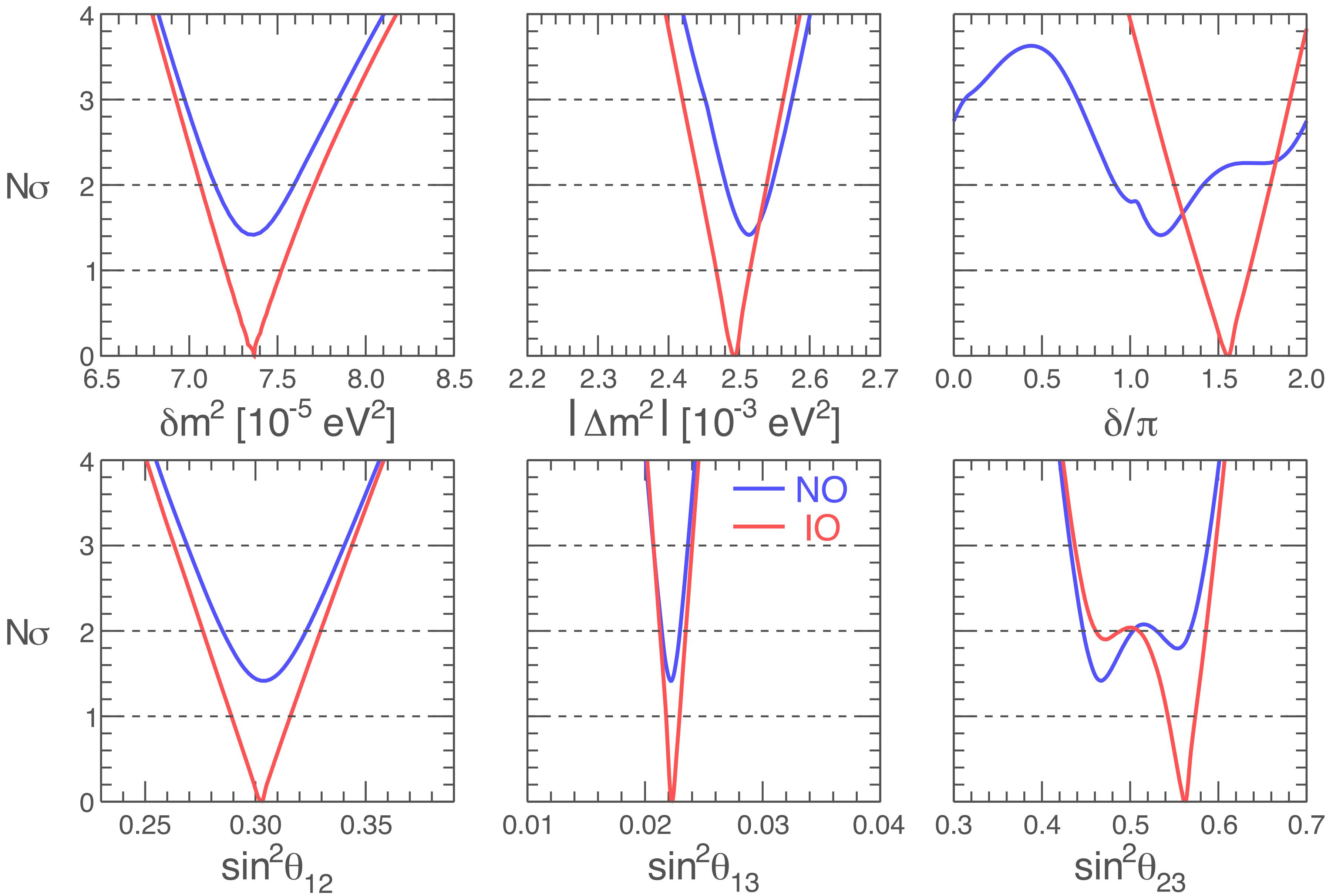
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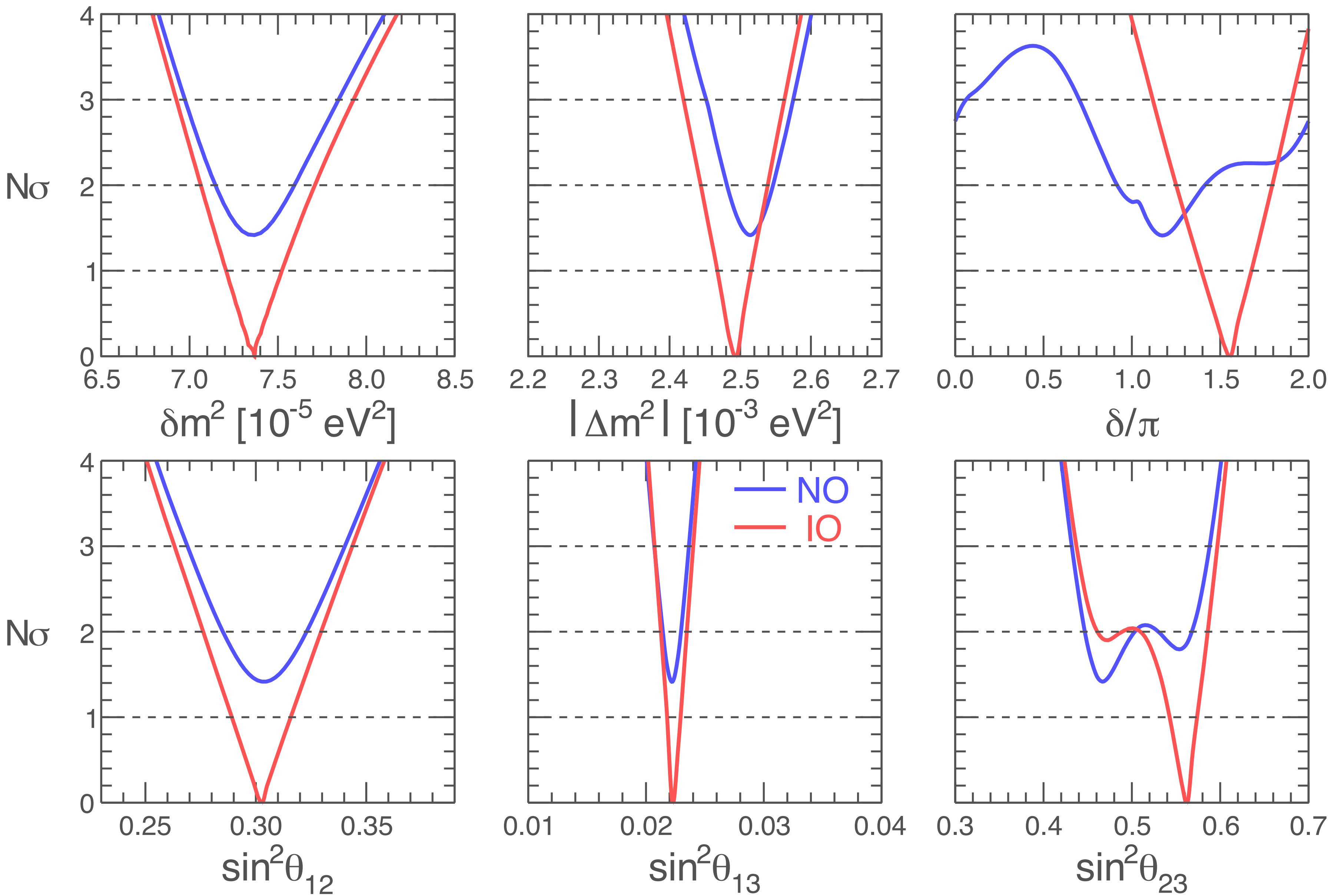
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Due to some tension, in IO, indications for CP violation $> 3\sigma$

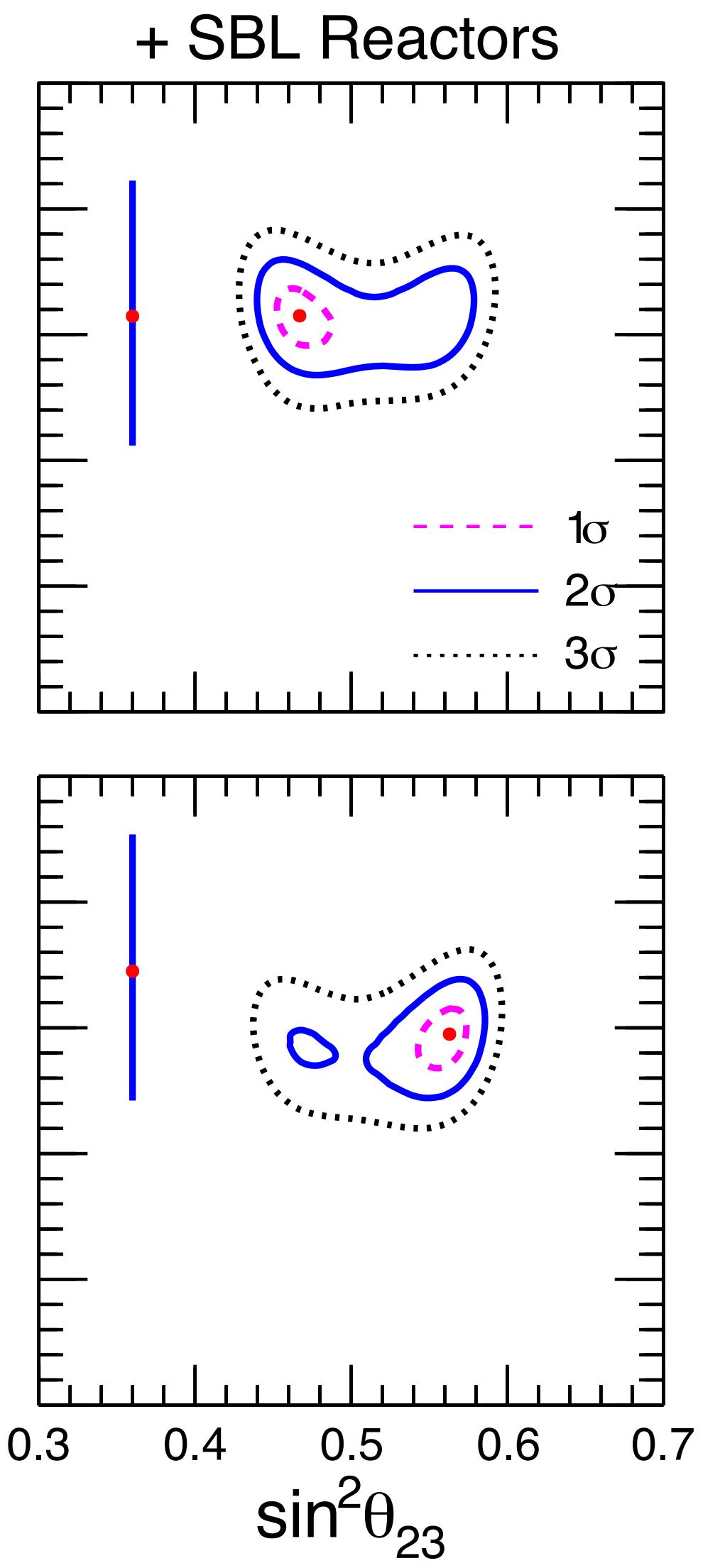
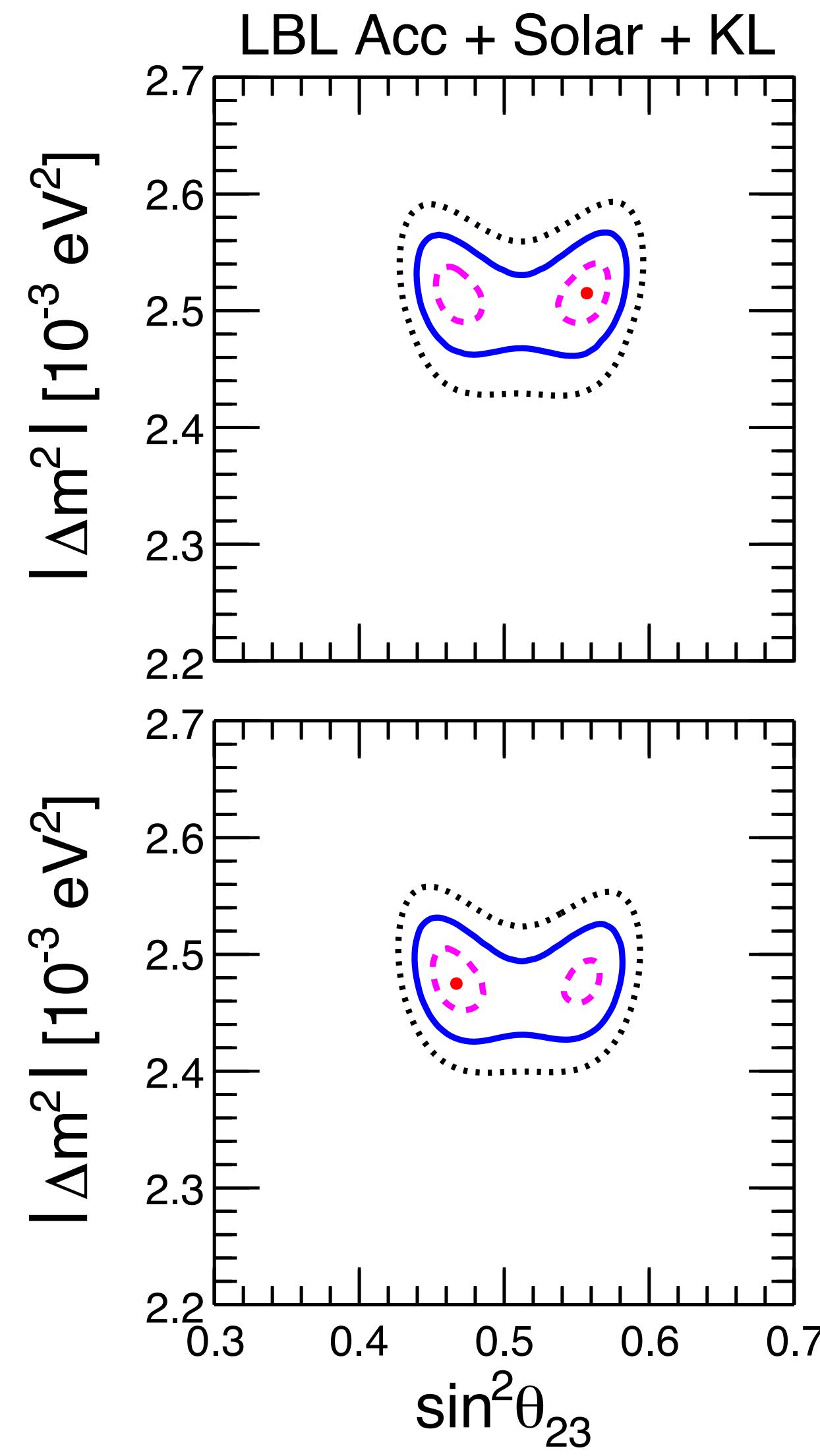
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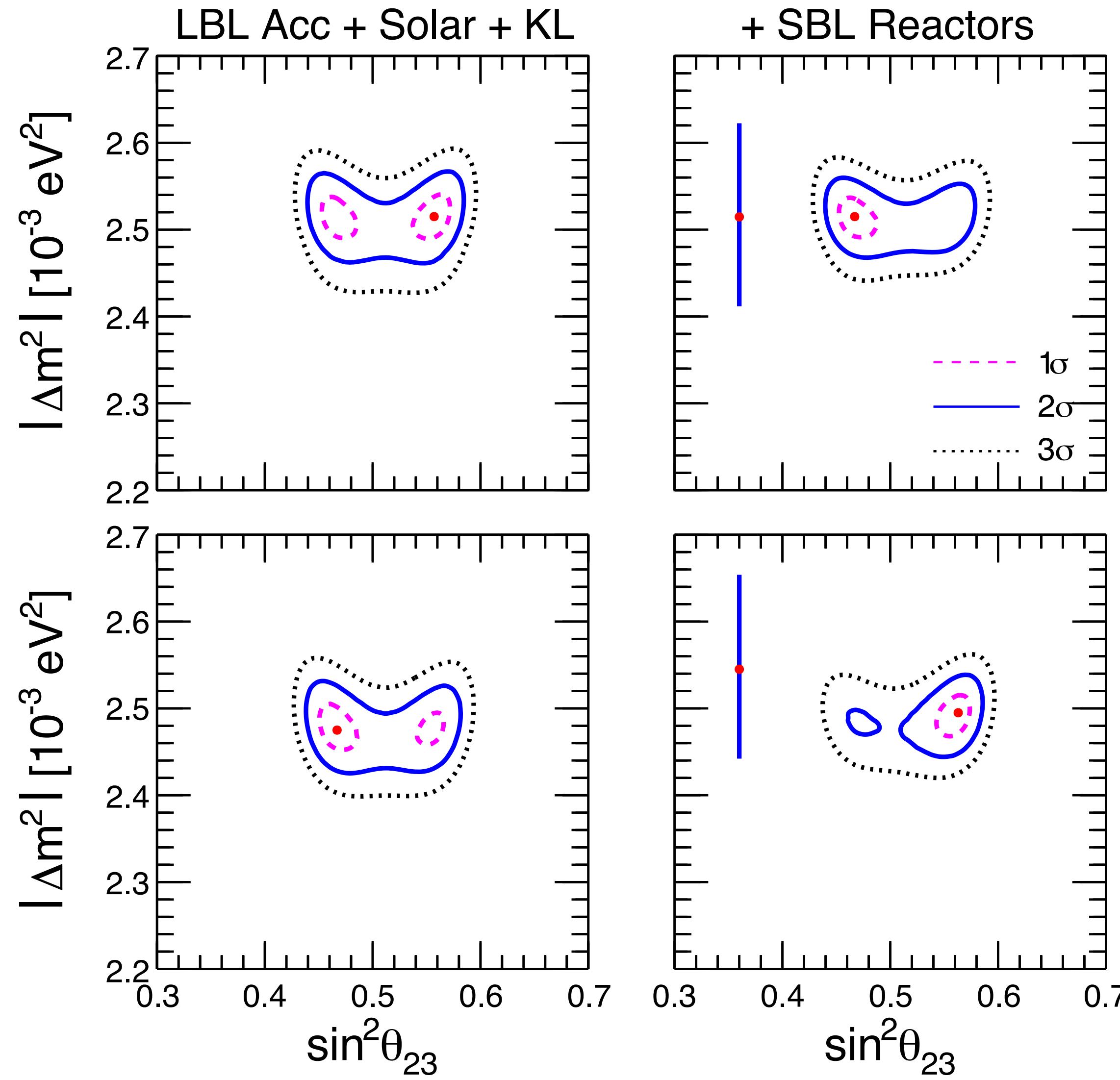
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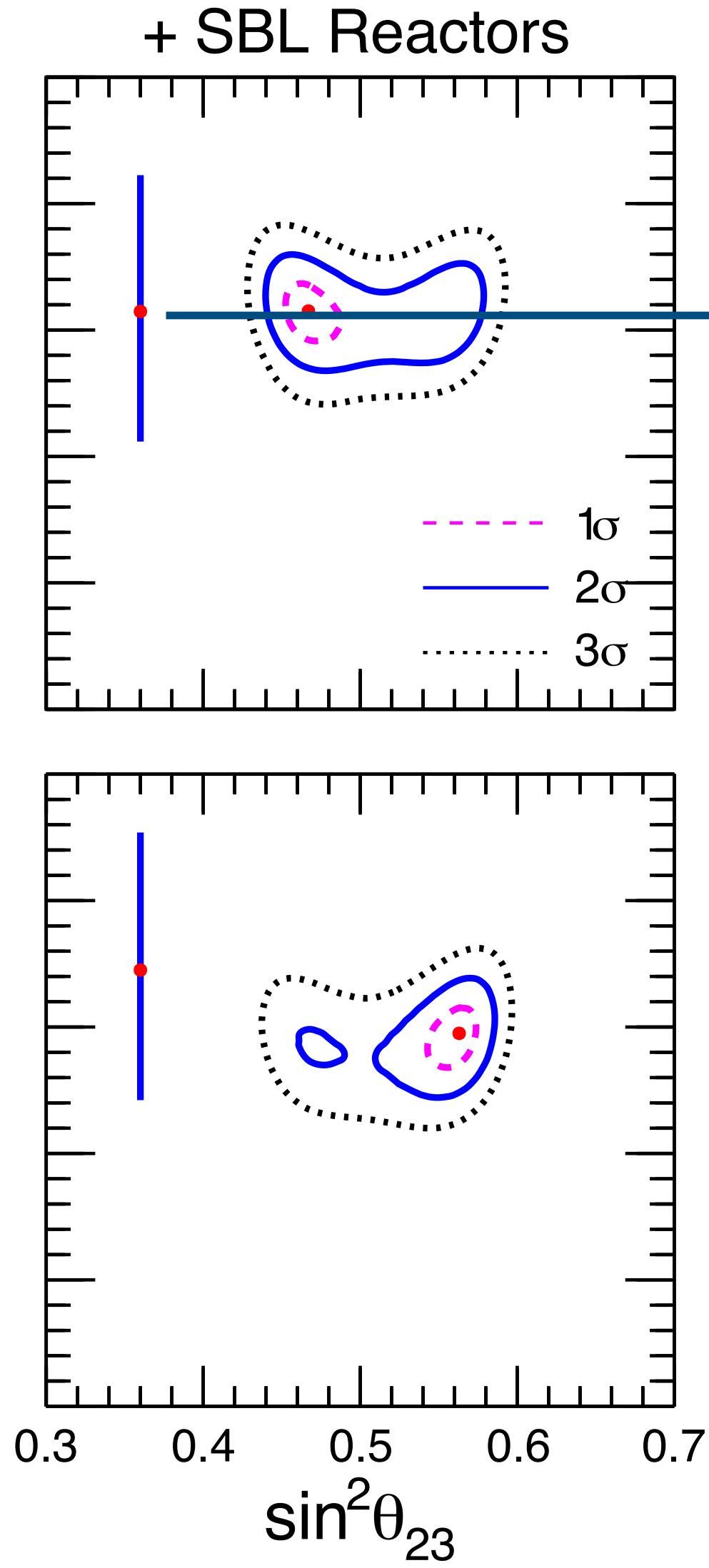
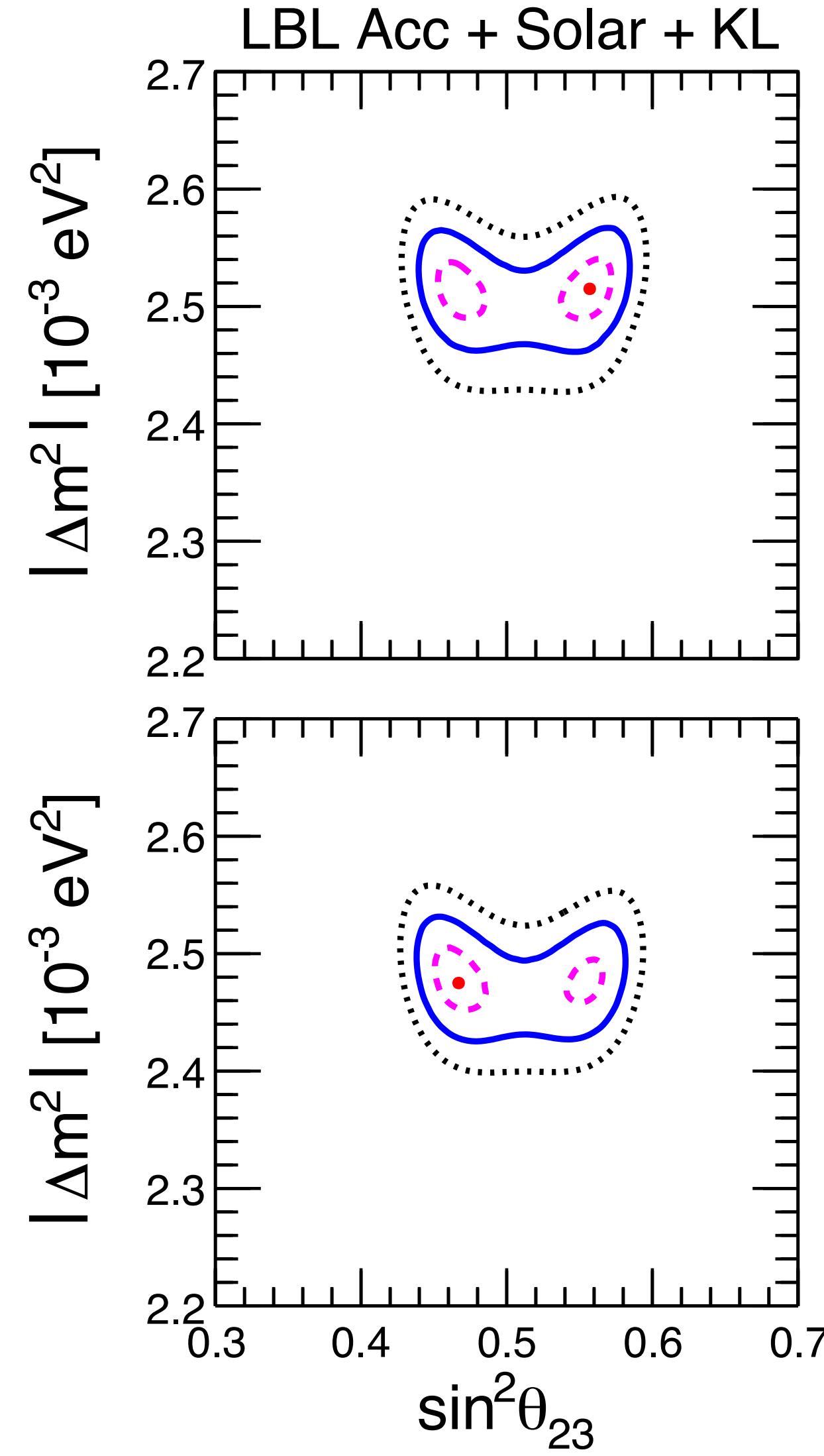


Adding SBL reactors:
 Still preference for IO, but
 at lower CL ($\sim 1.4\sigma$)



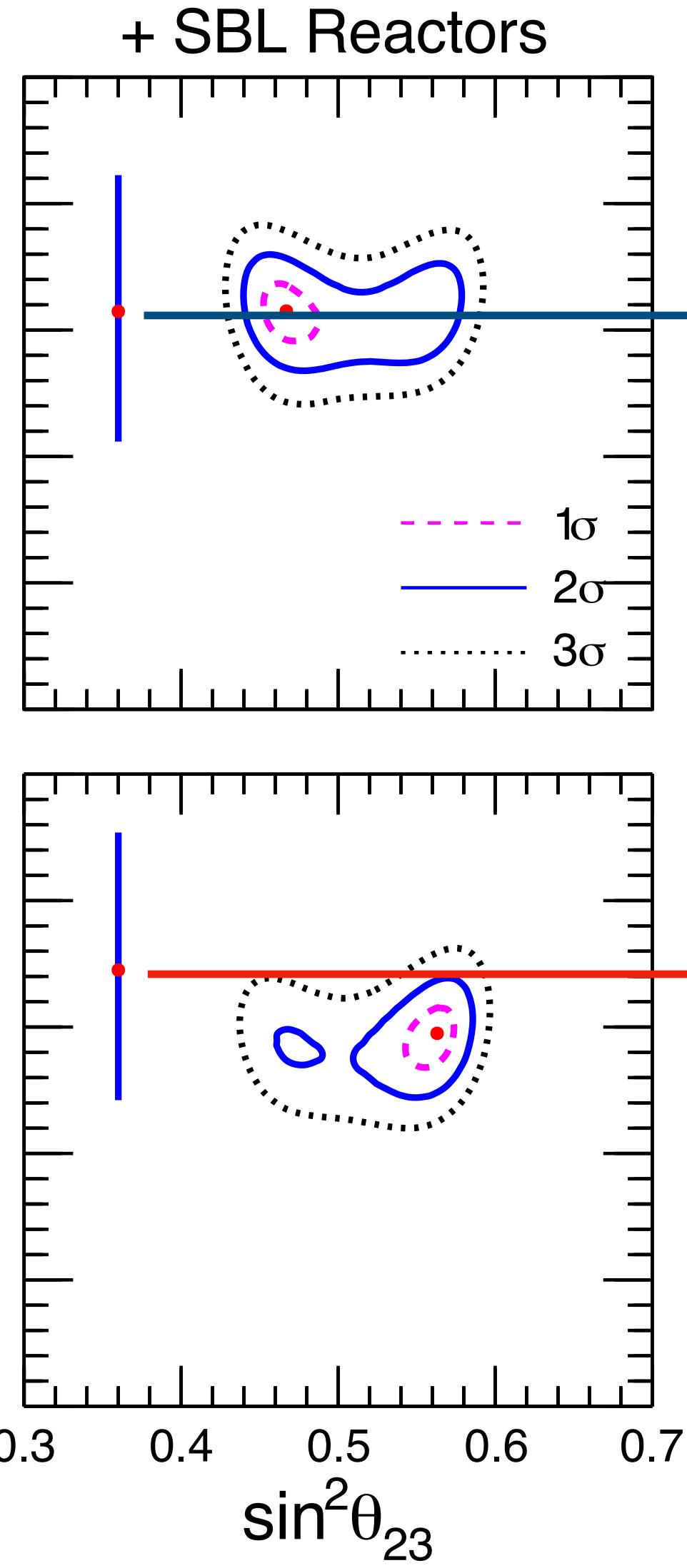
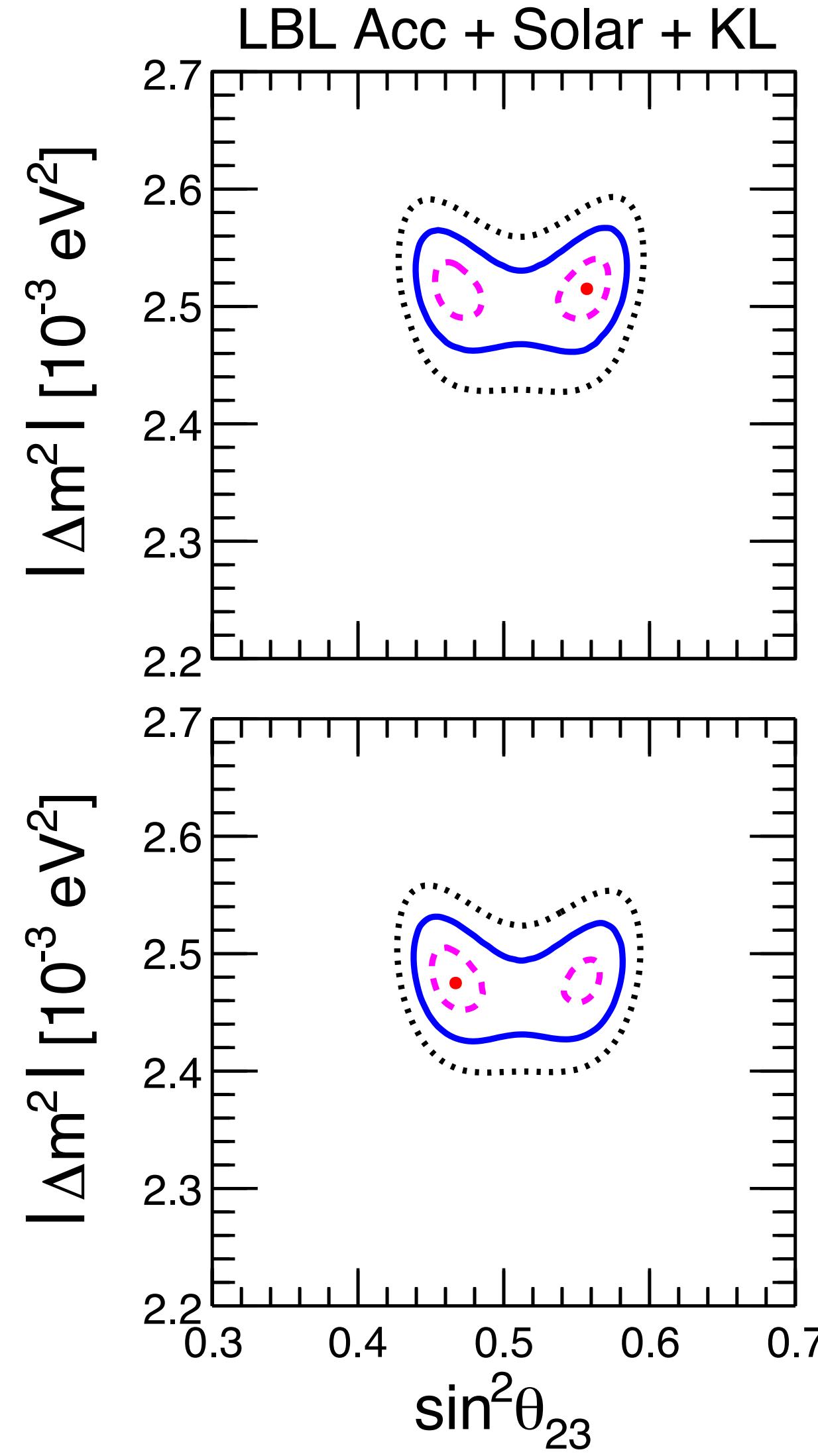
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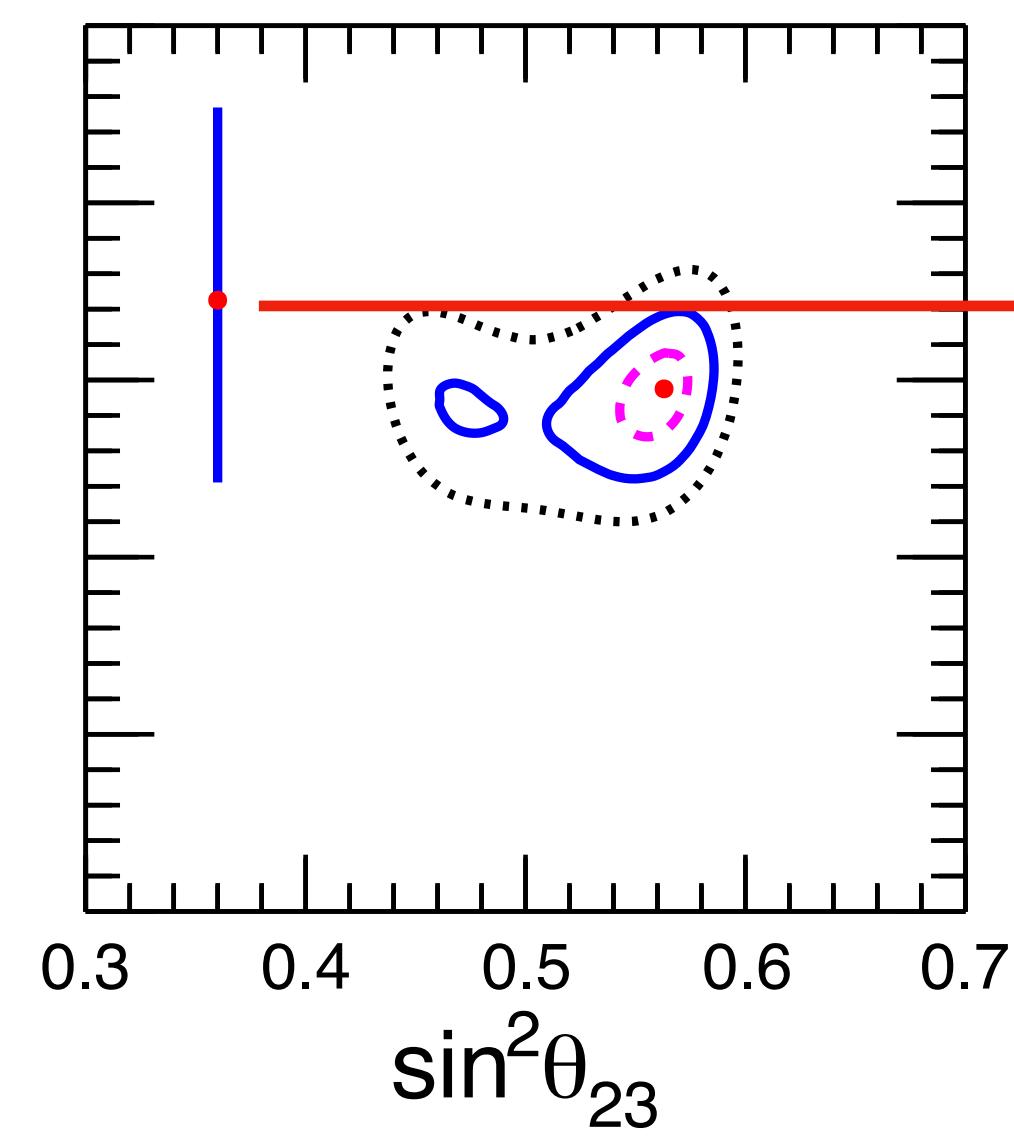
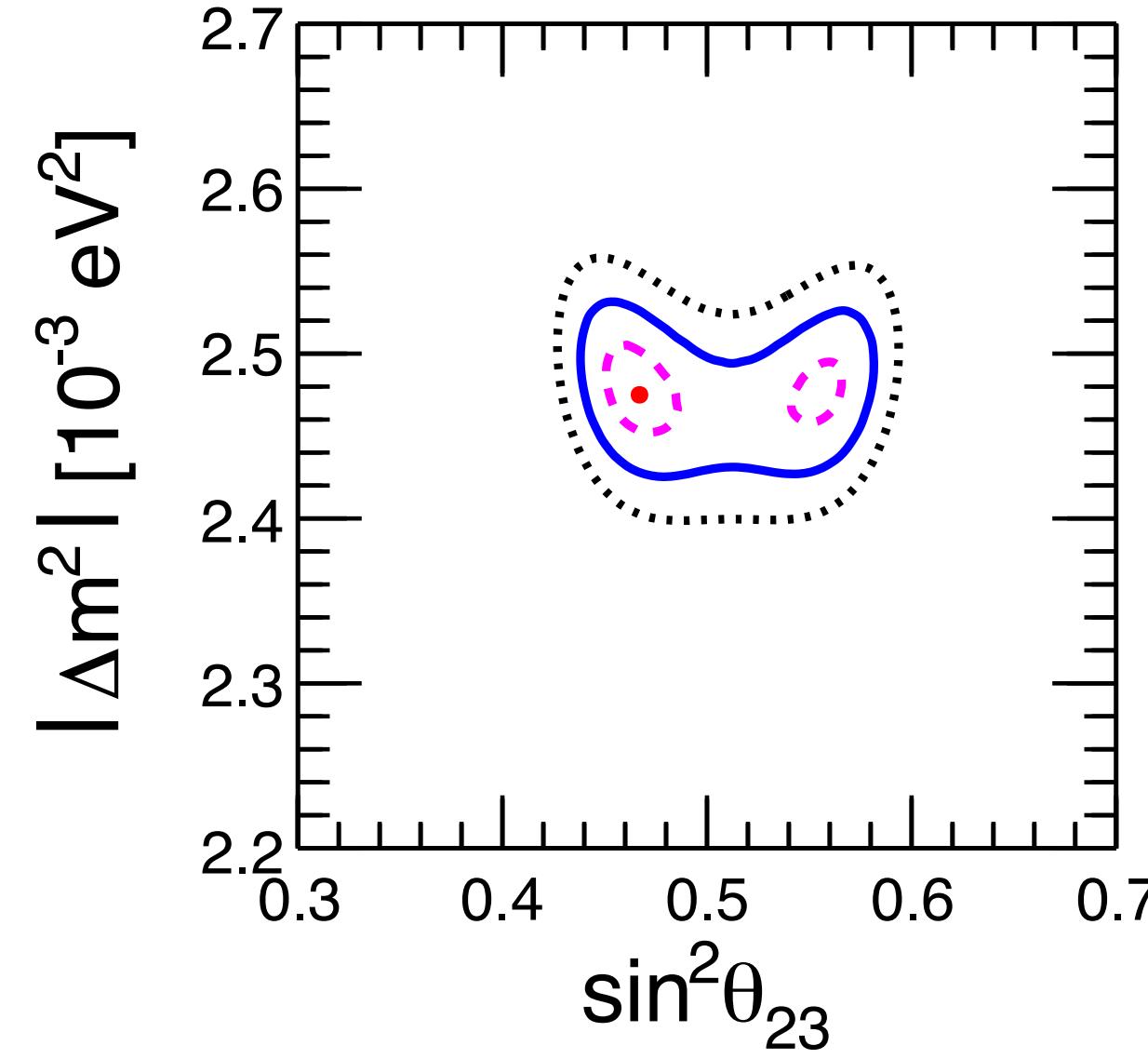
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Good agreement in NO



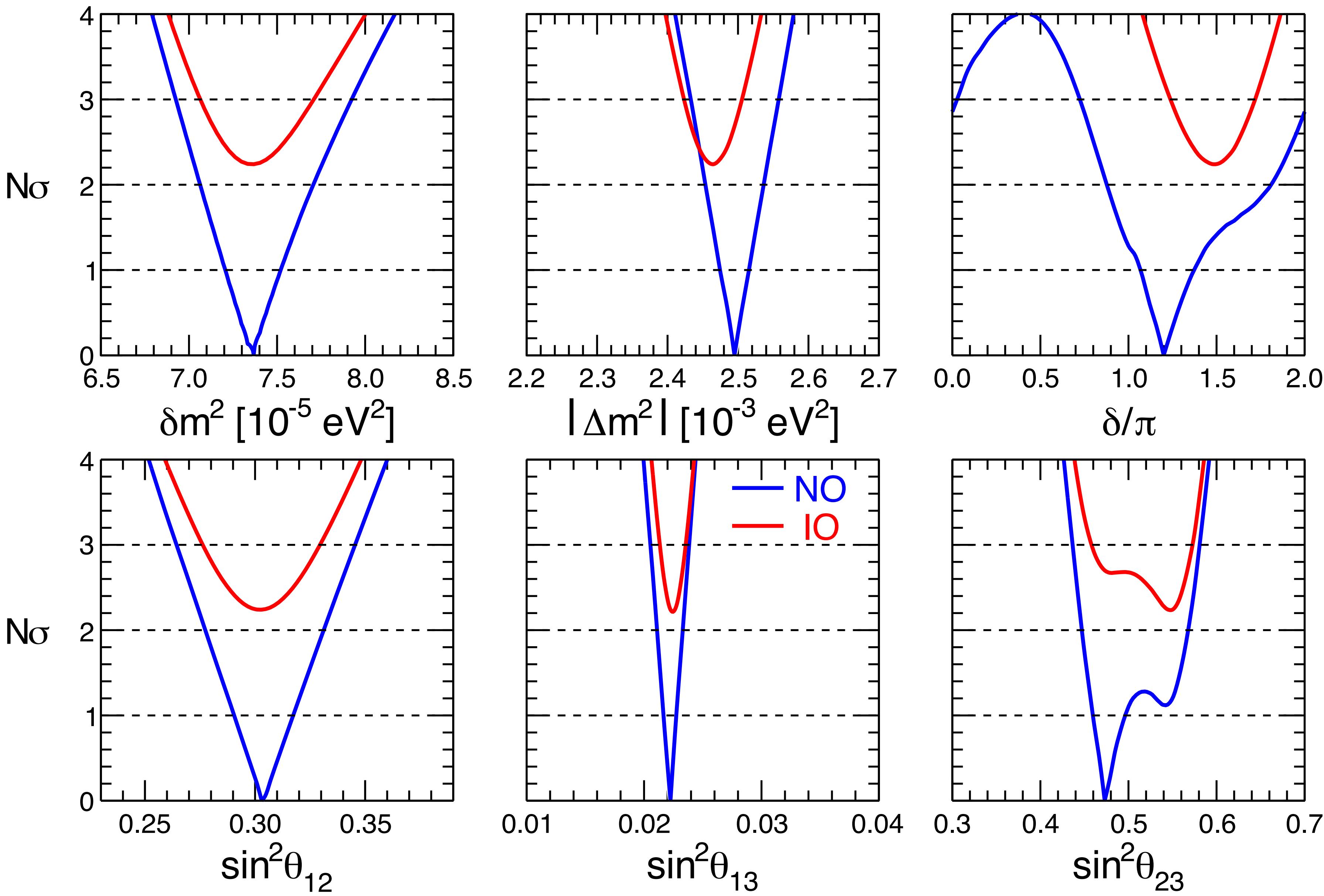
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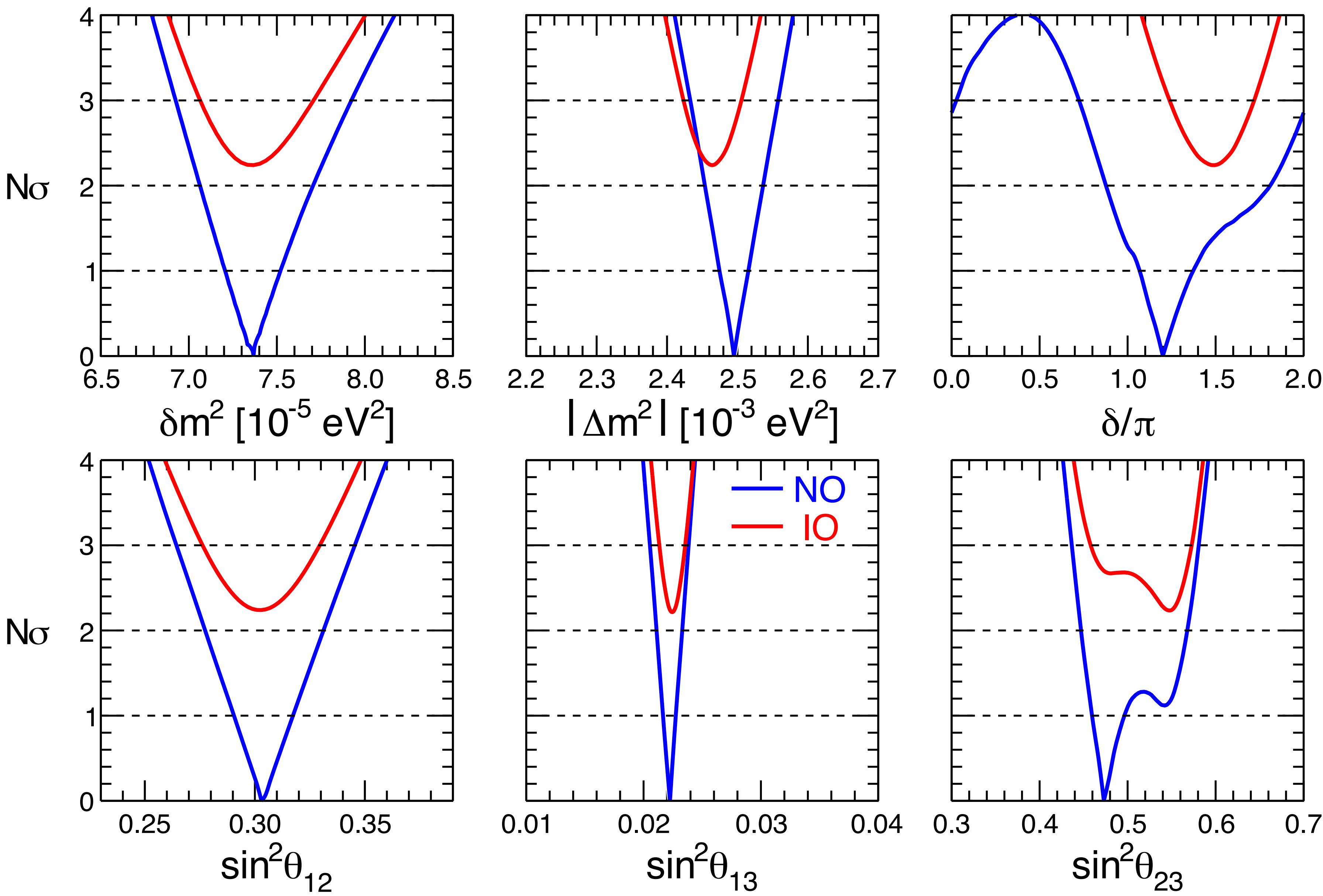


Slightly higher value in IO

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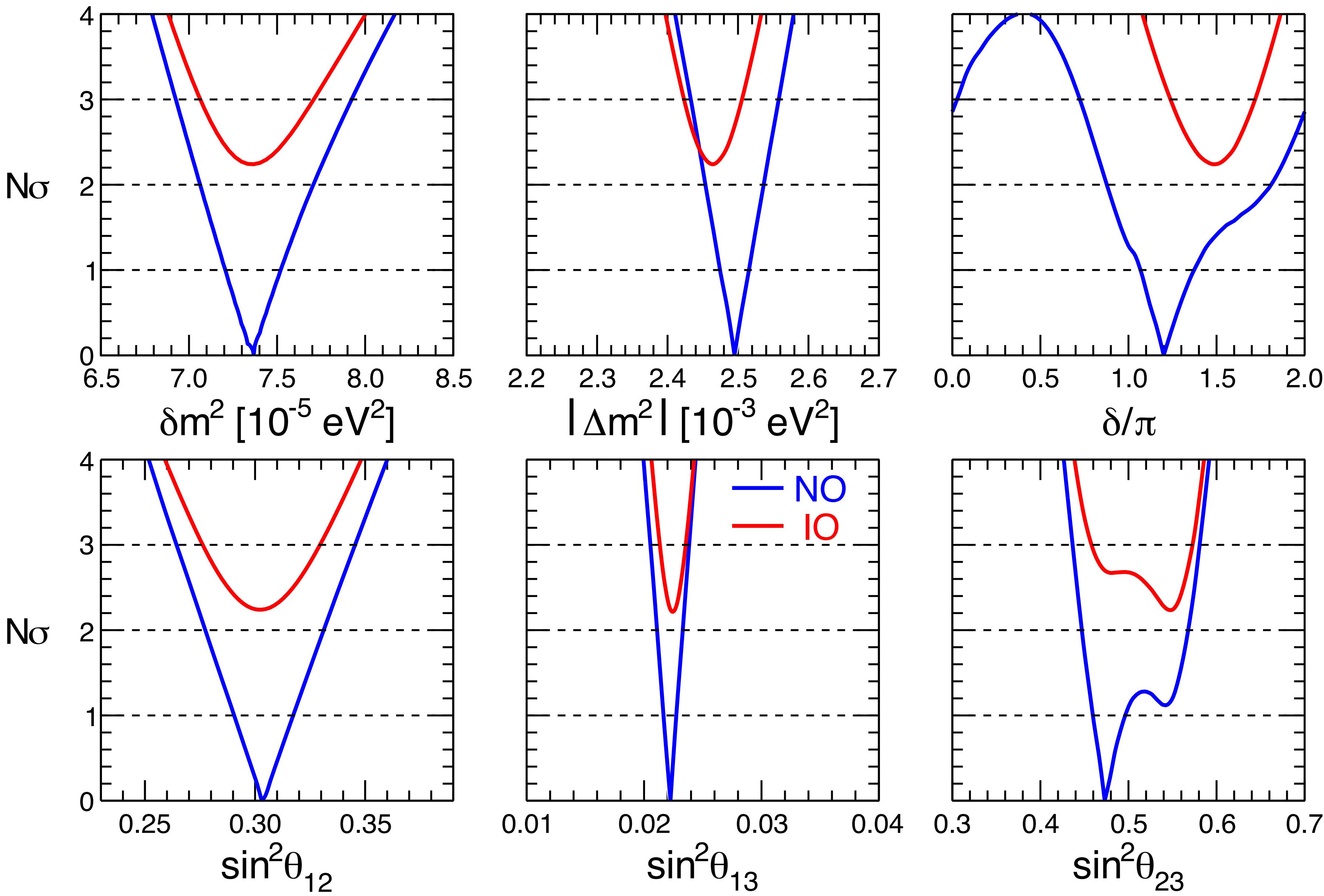


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In addition, reac+acc
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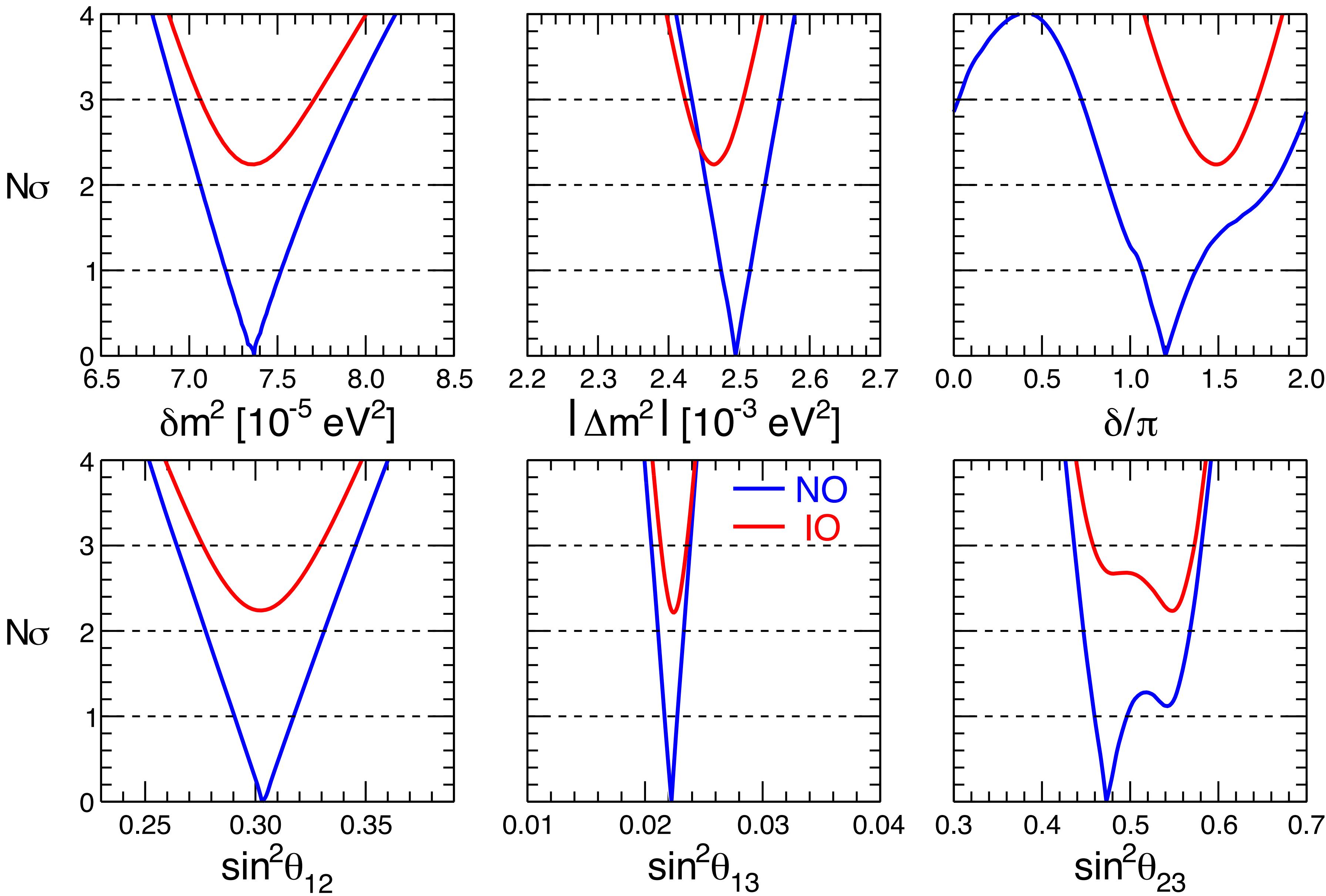
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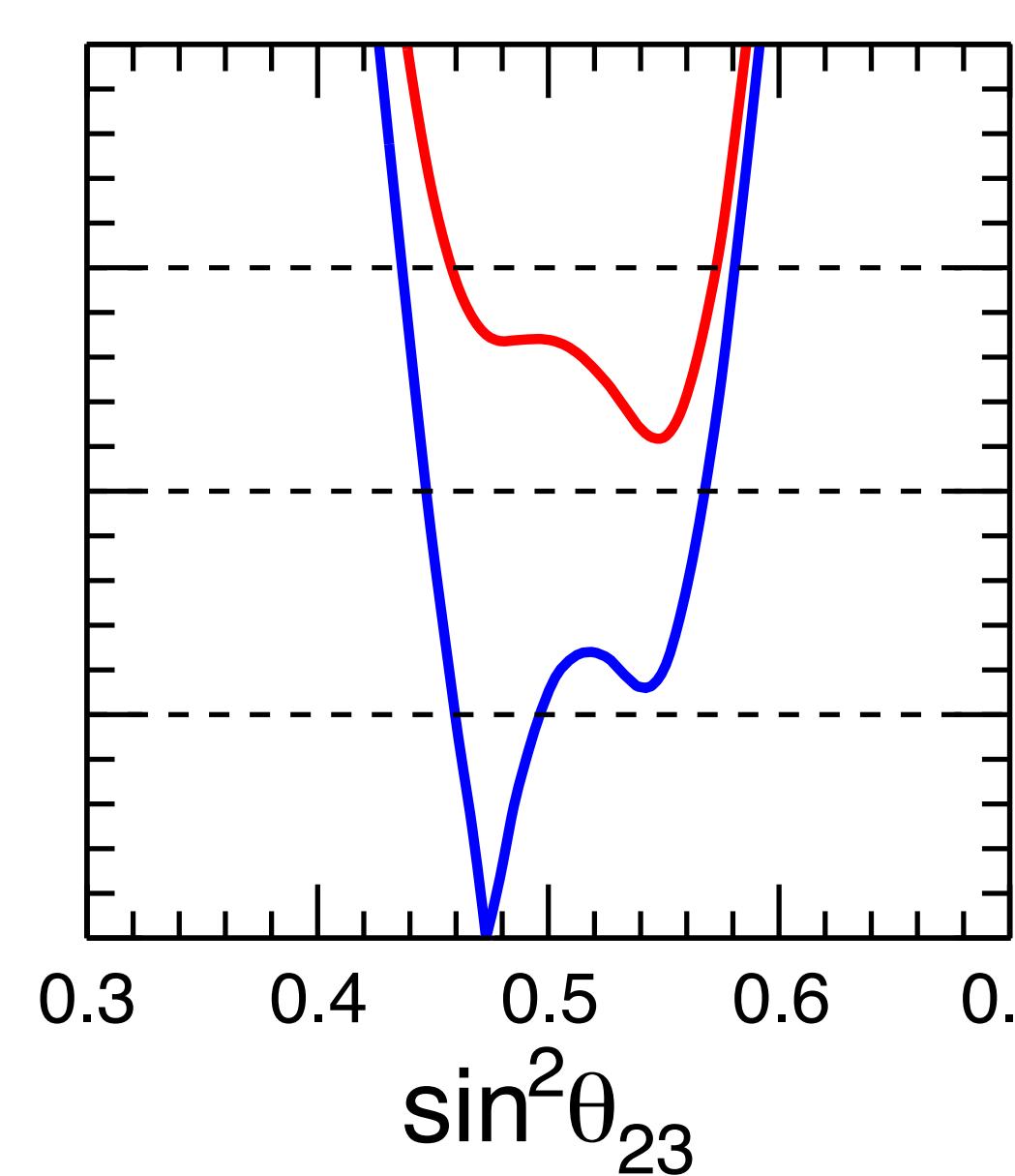
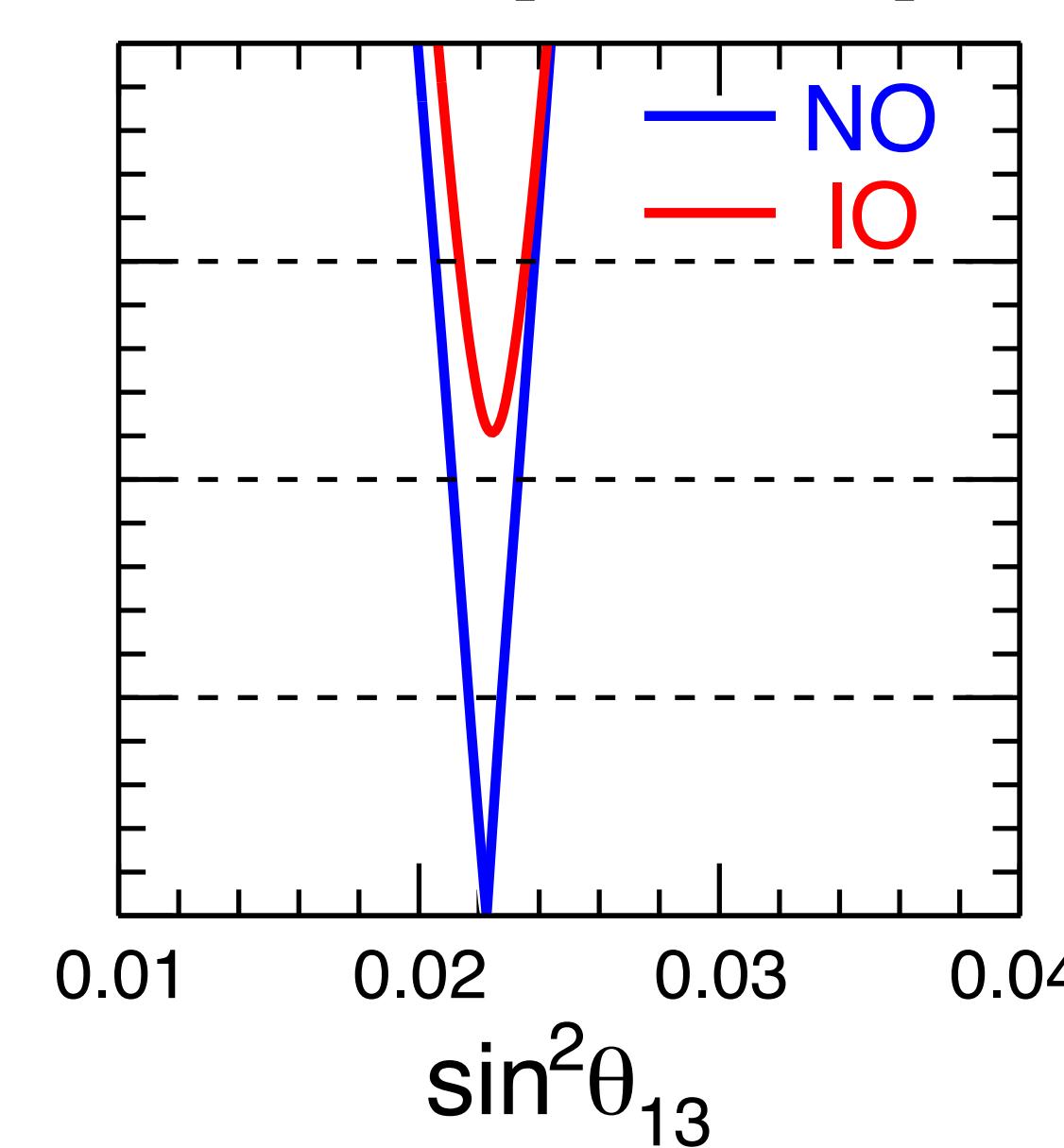
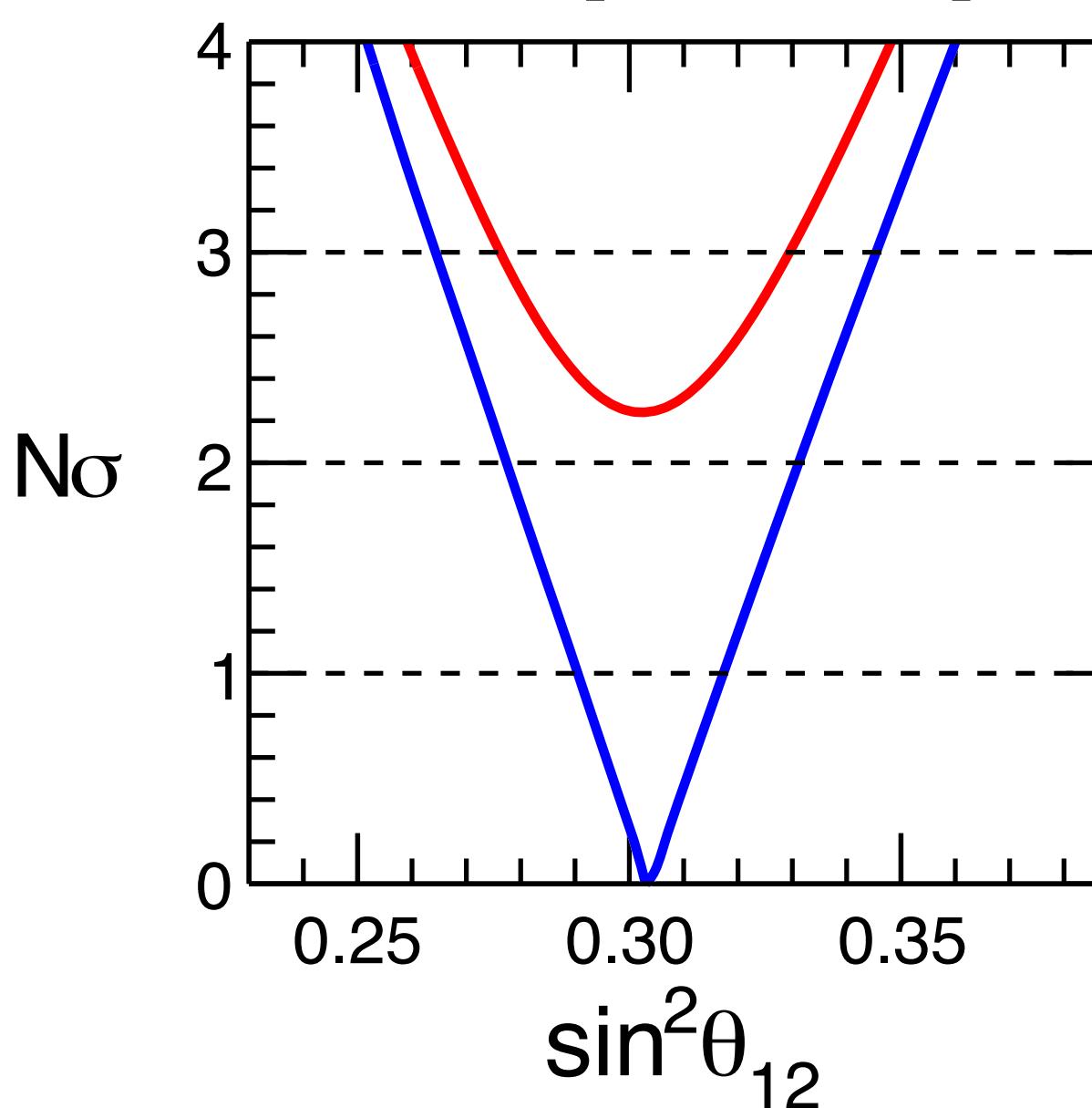
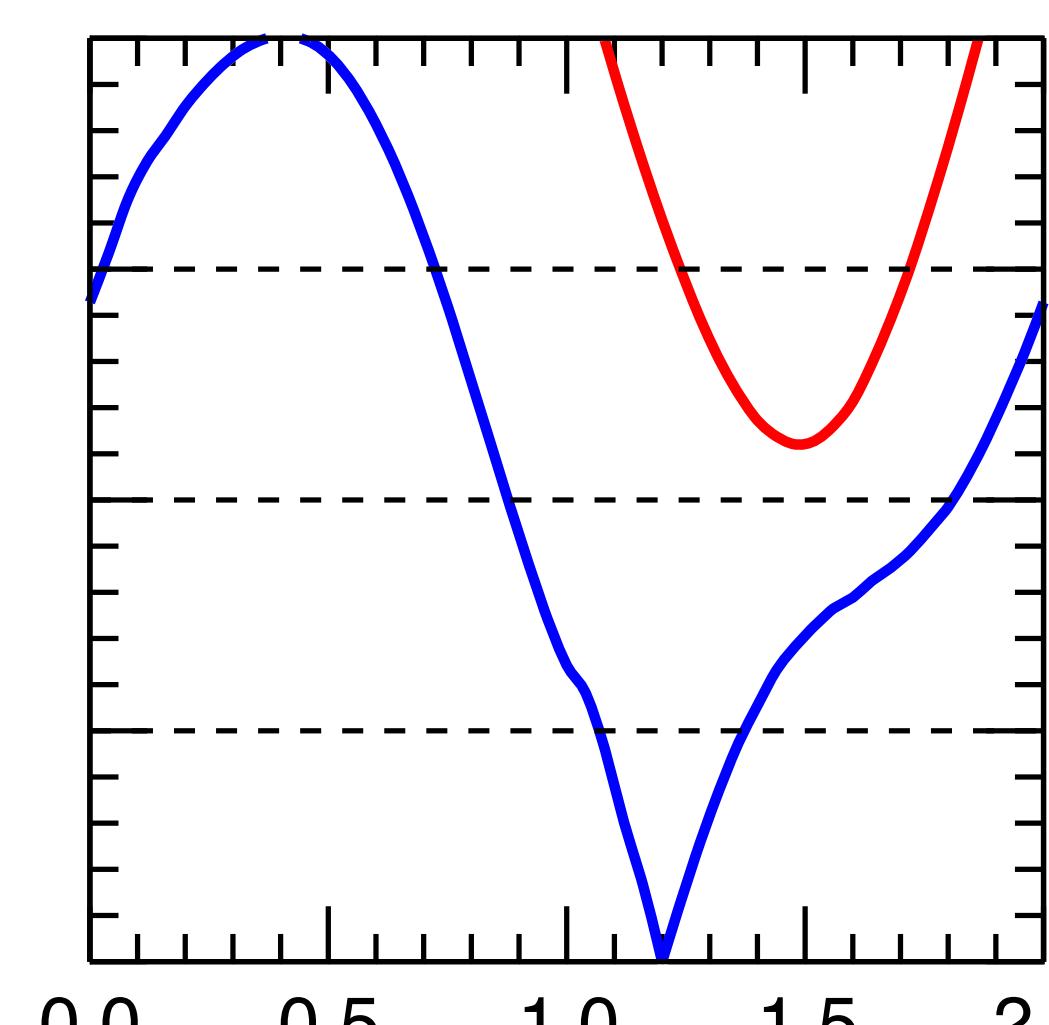
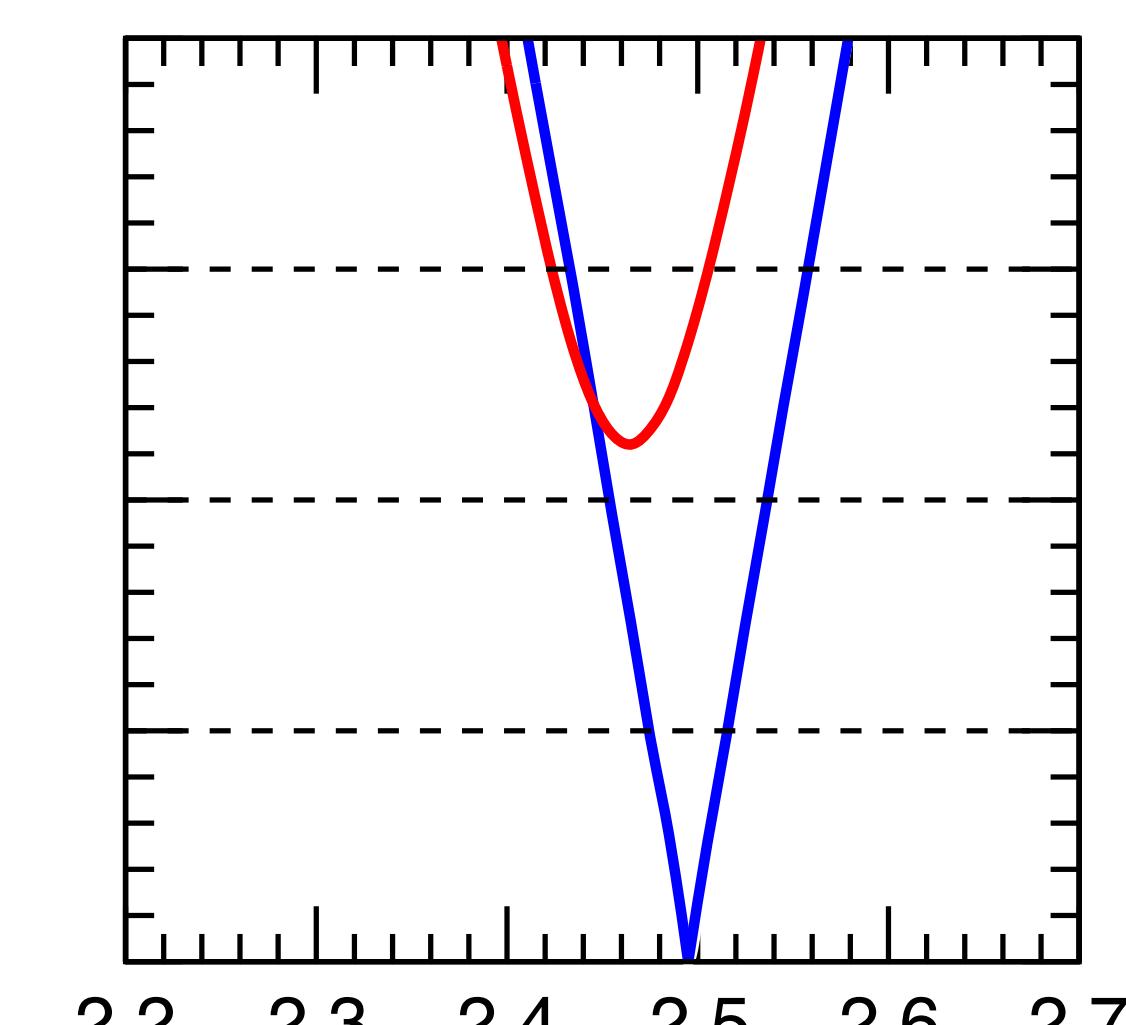
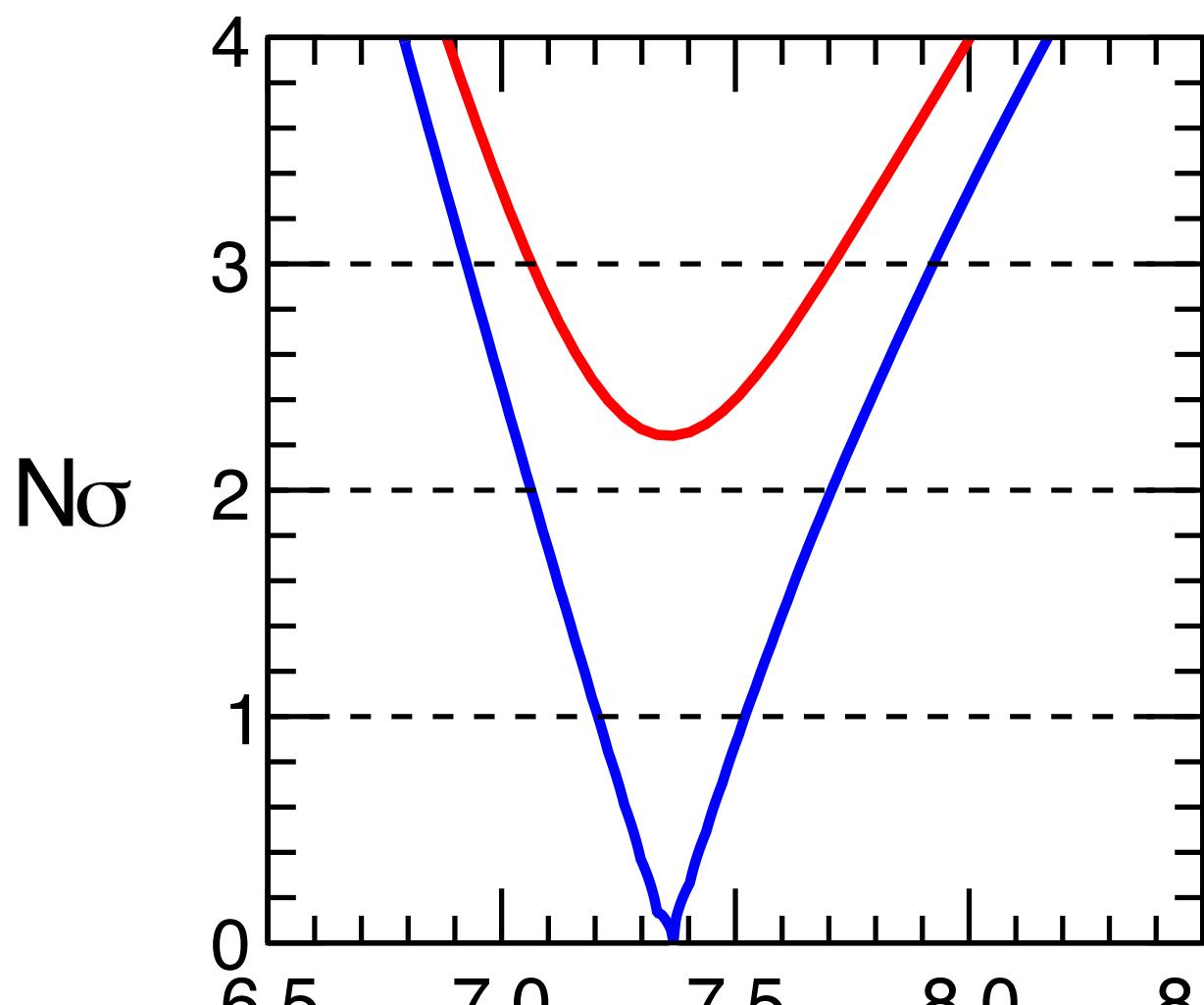


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Weak hint for CP violation ($\sim 1.3\sigma$) and first octant ($\sim 1.1\sigma$)

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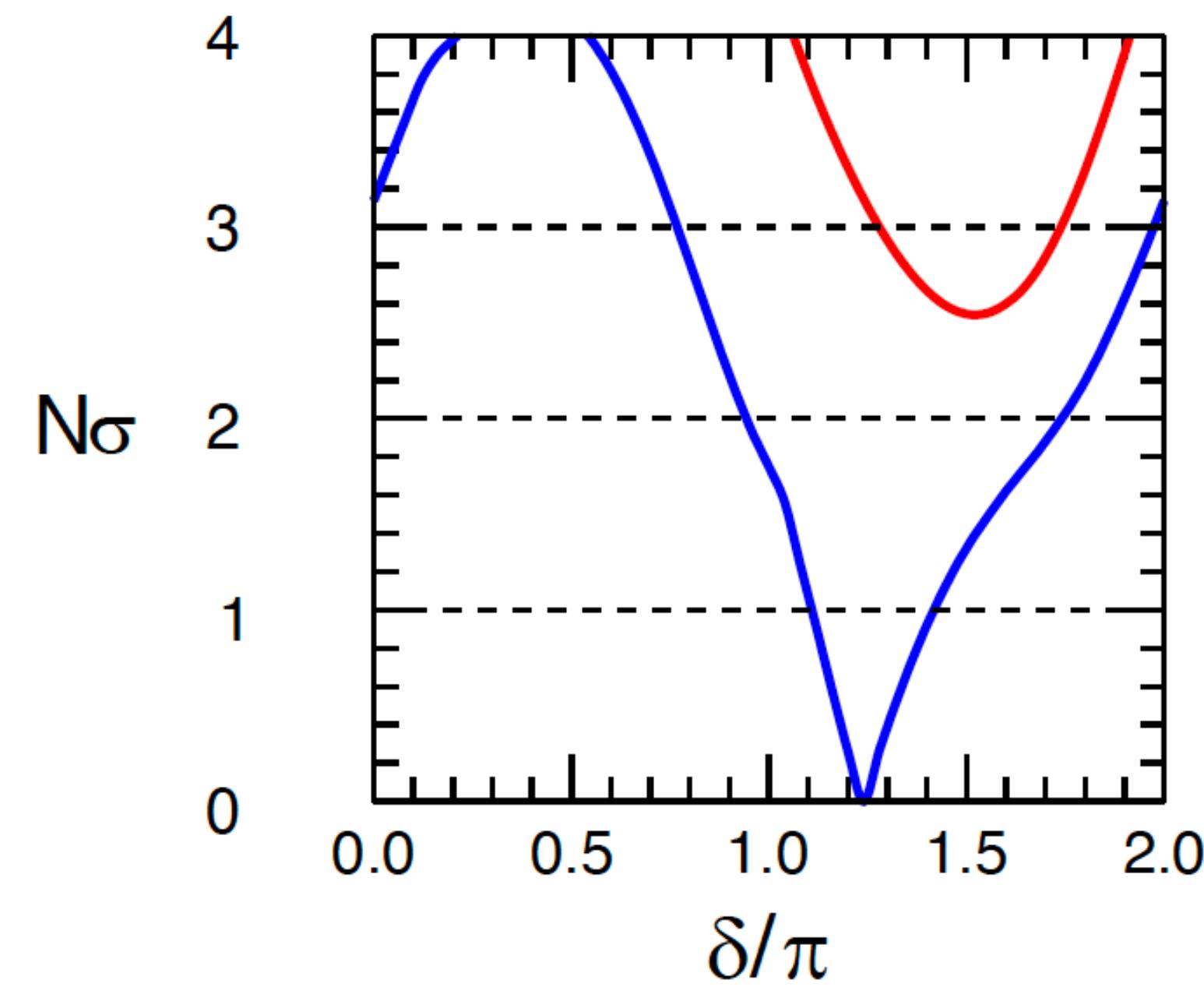
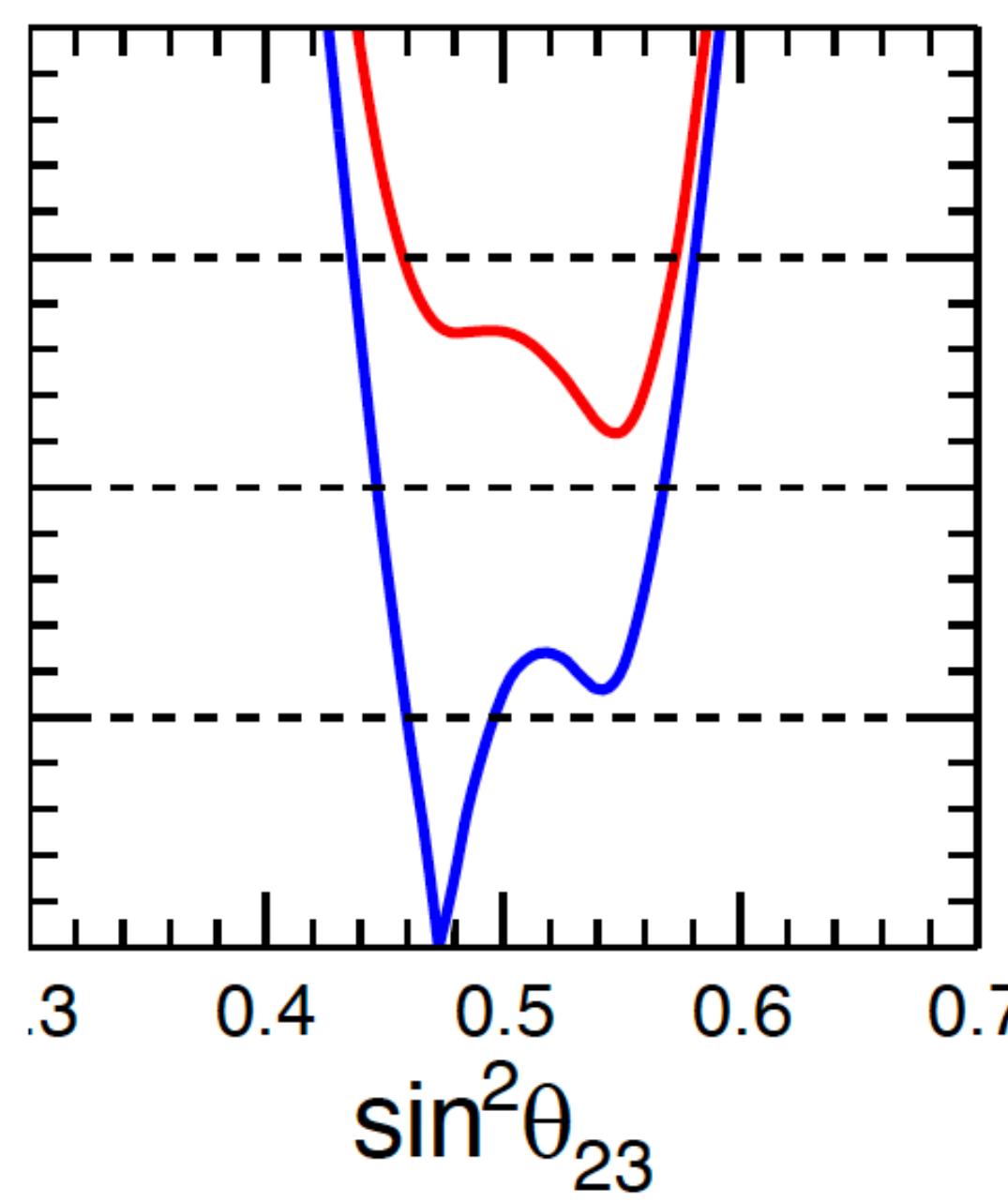
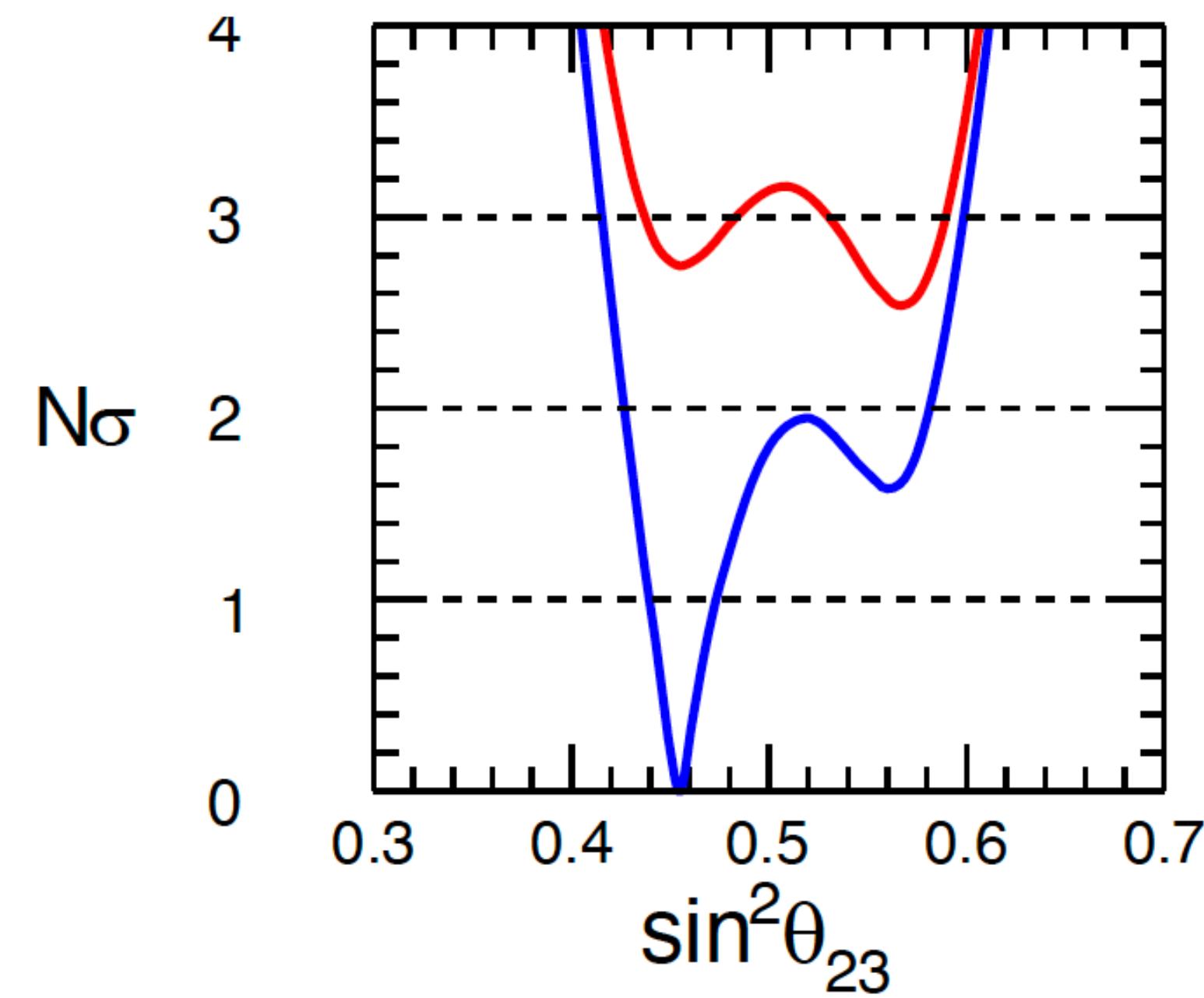
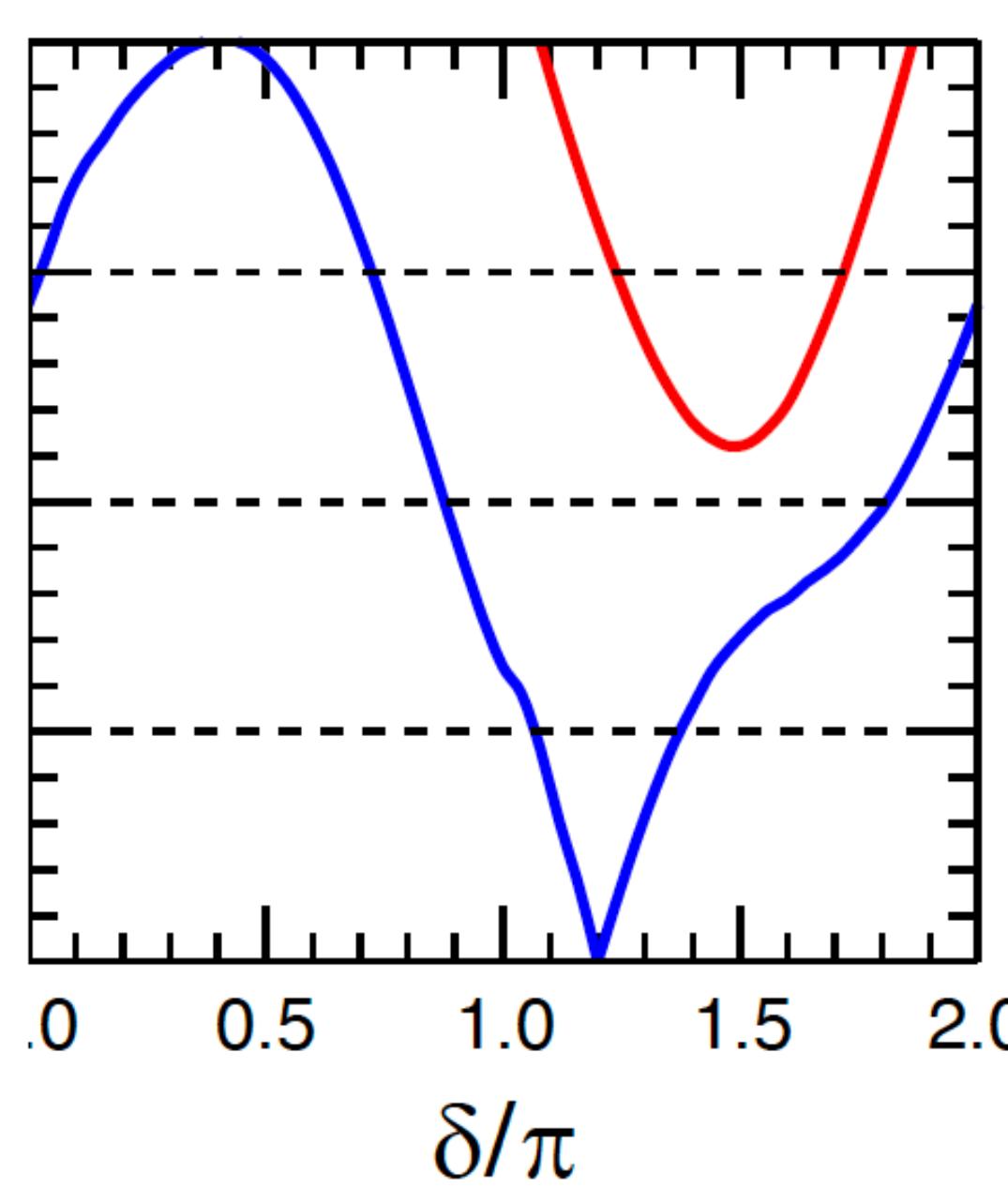


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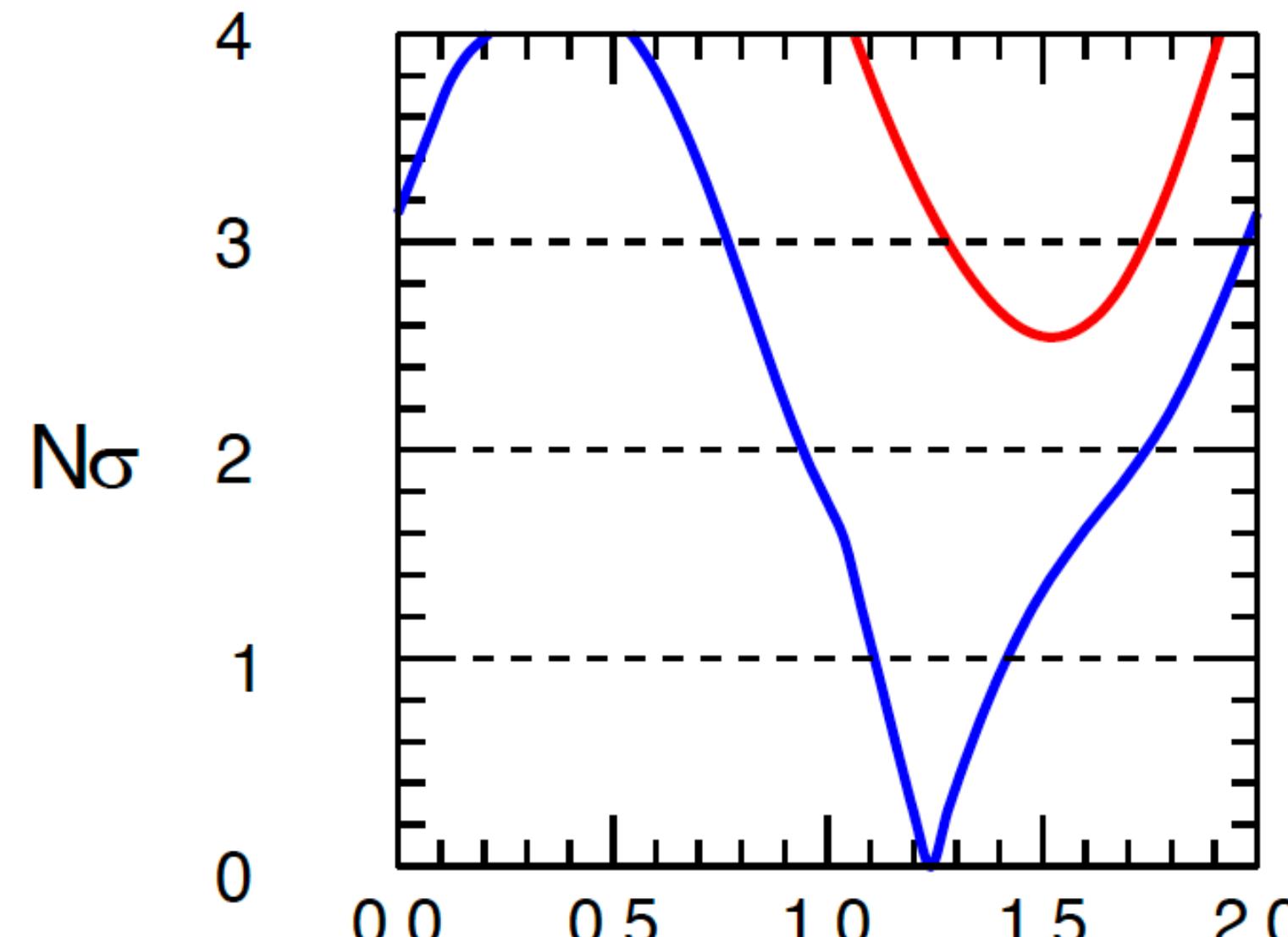
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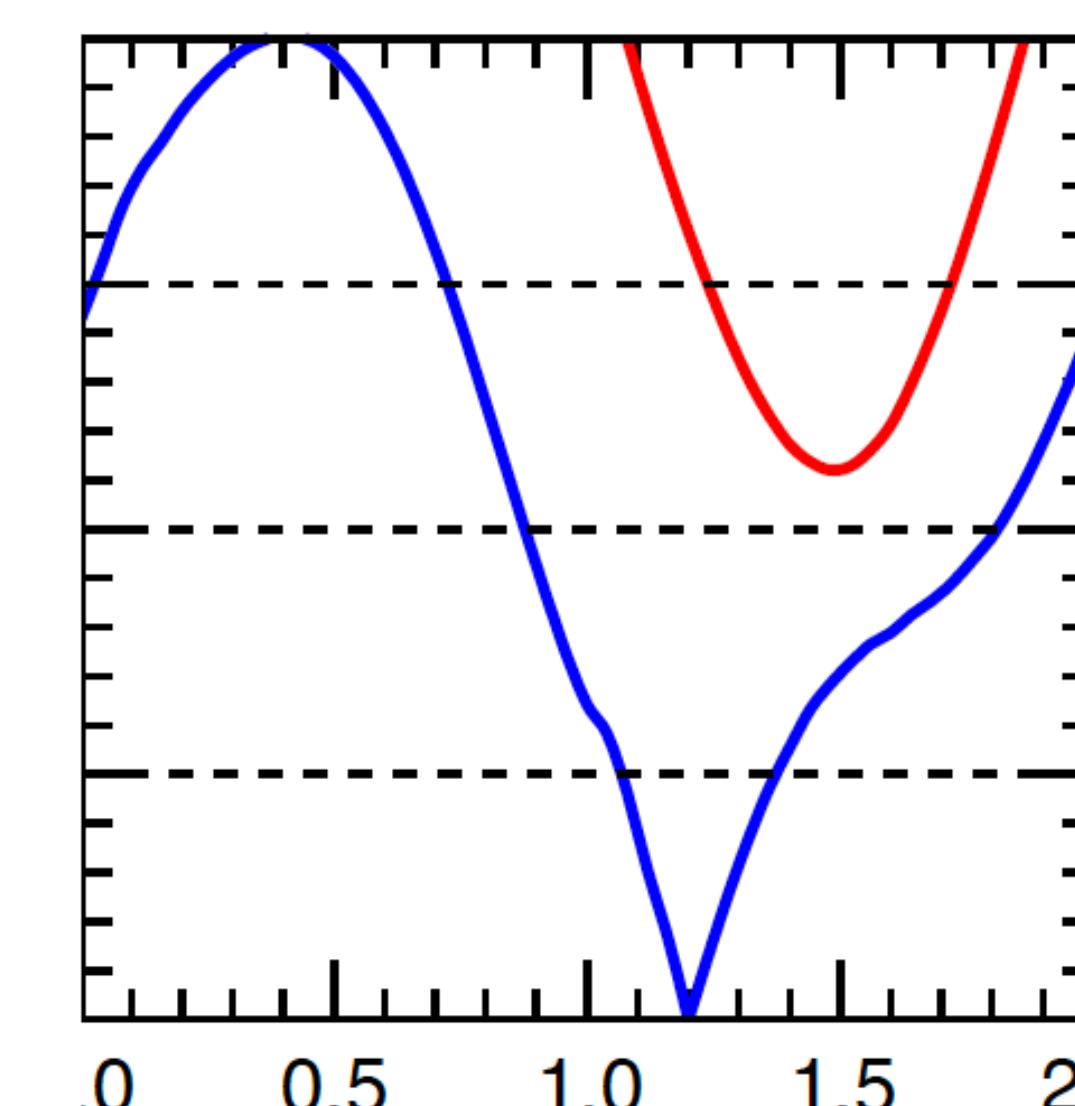
Overall status of oscillation unknowns is more uncertain than in older analyses

2021**2025**

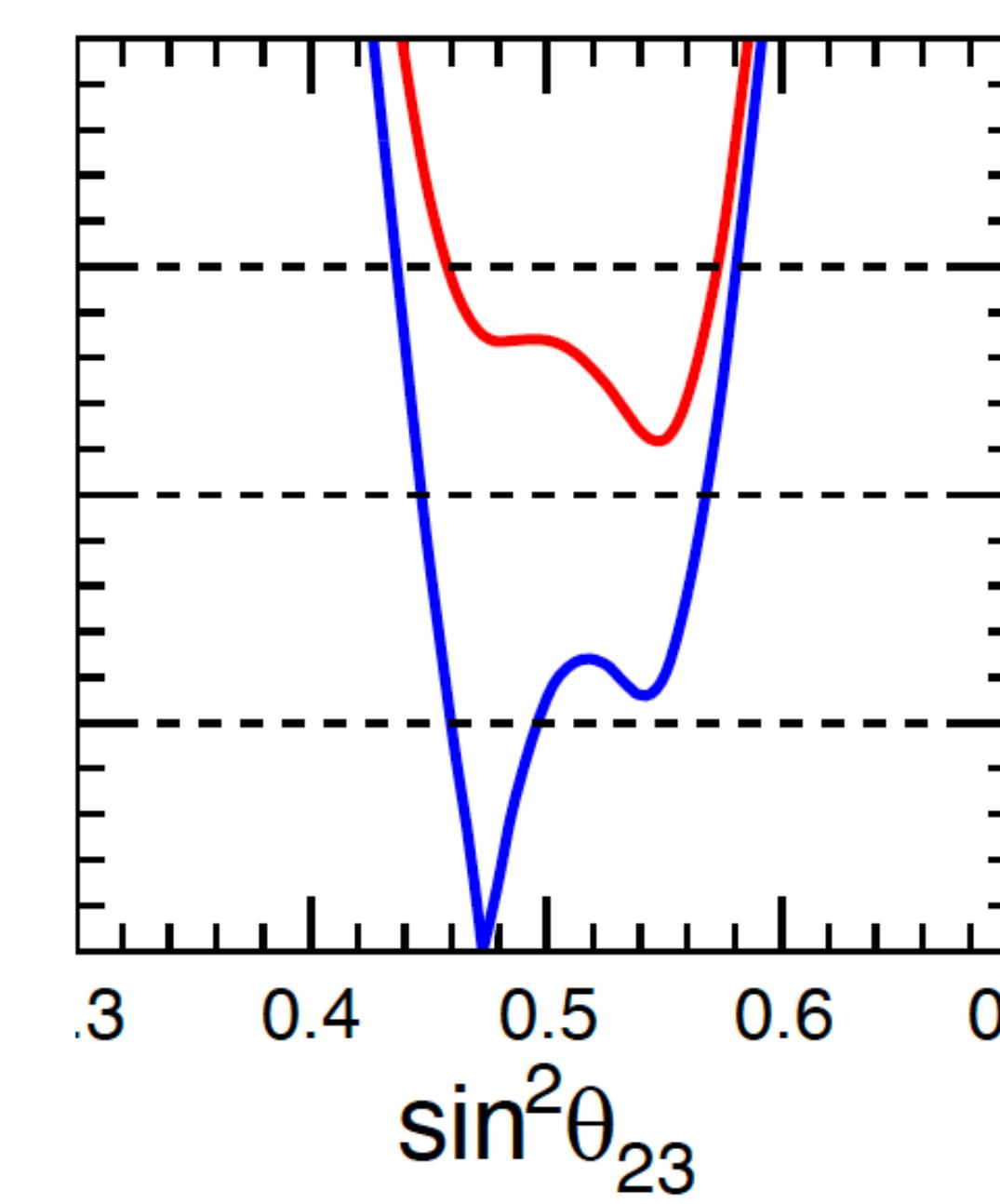
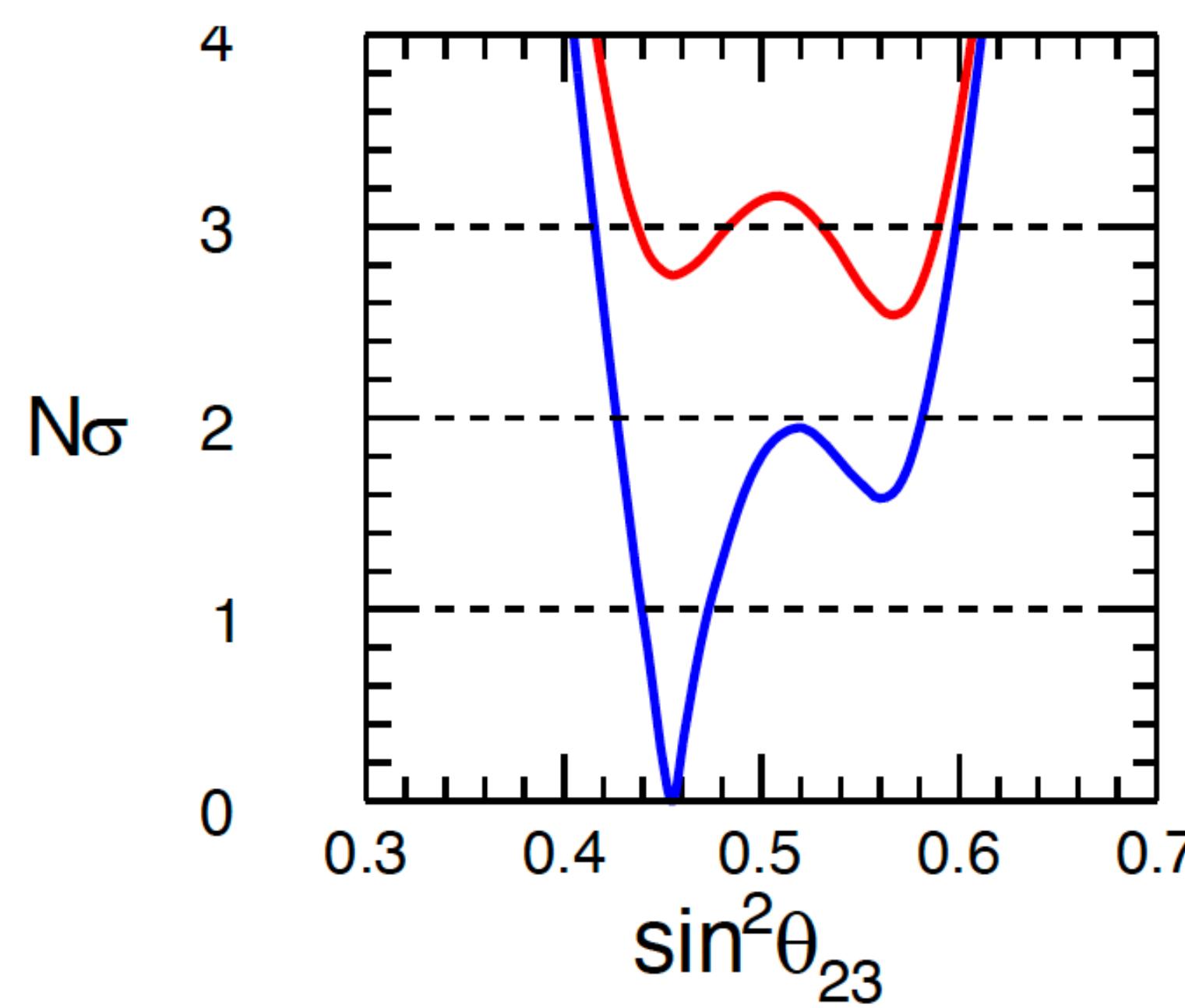
2021



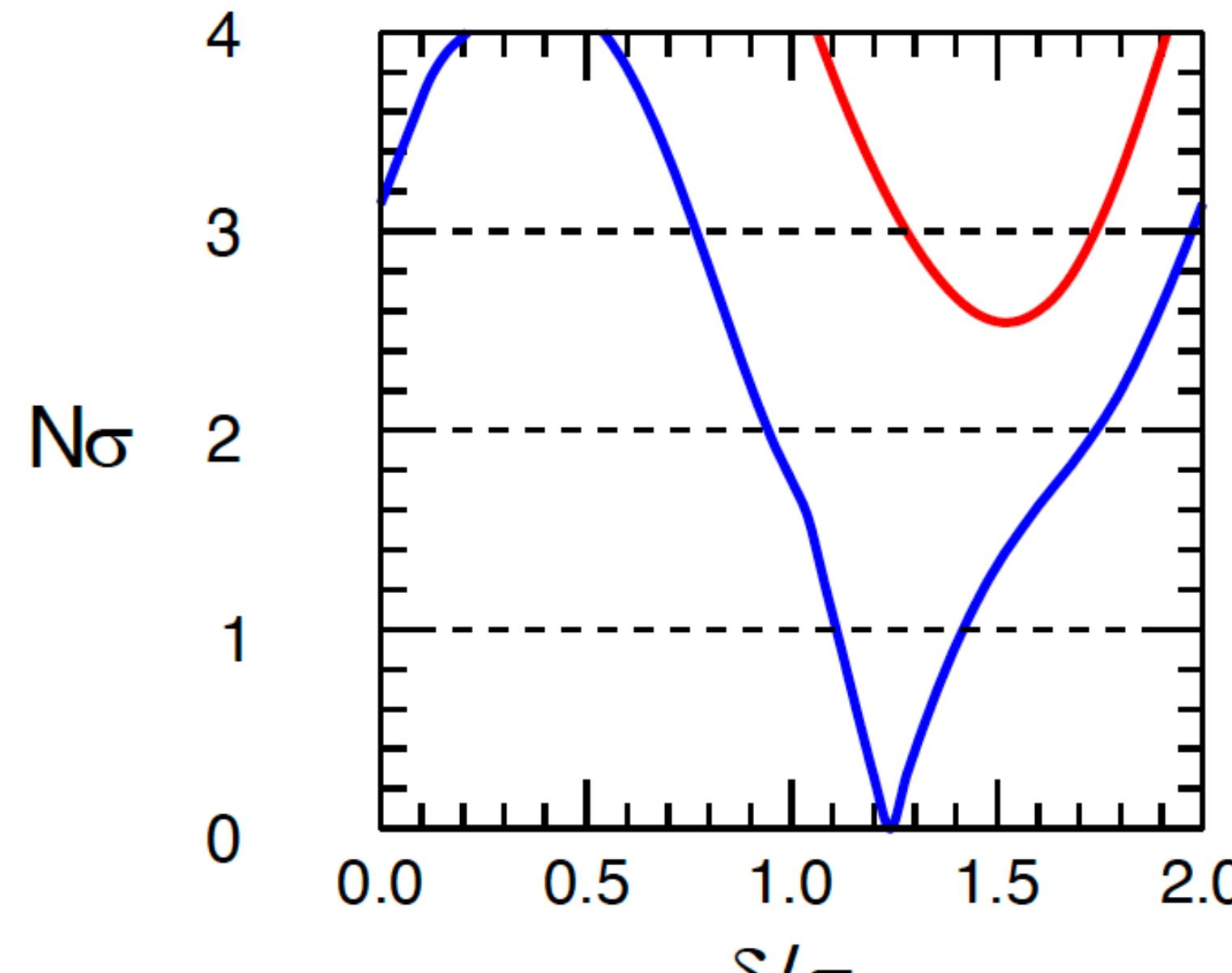
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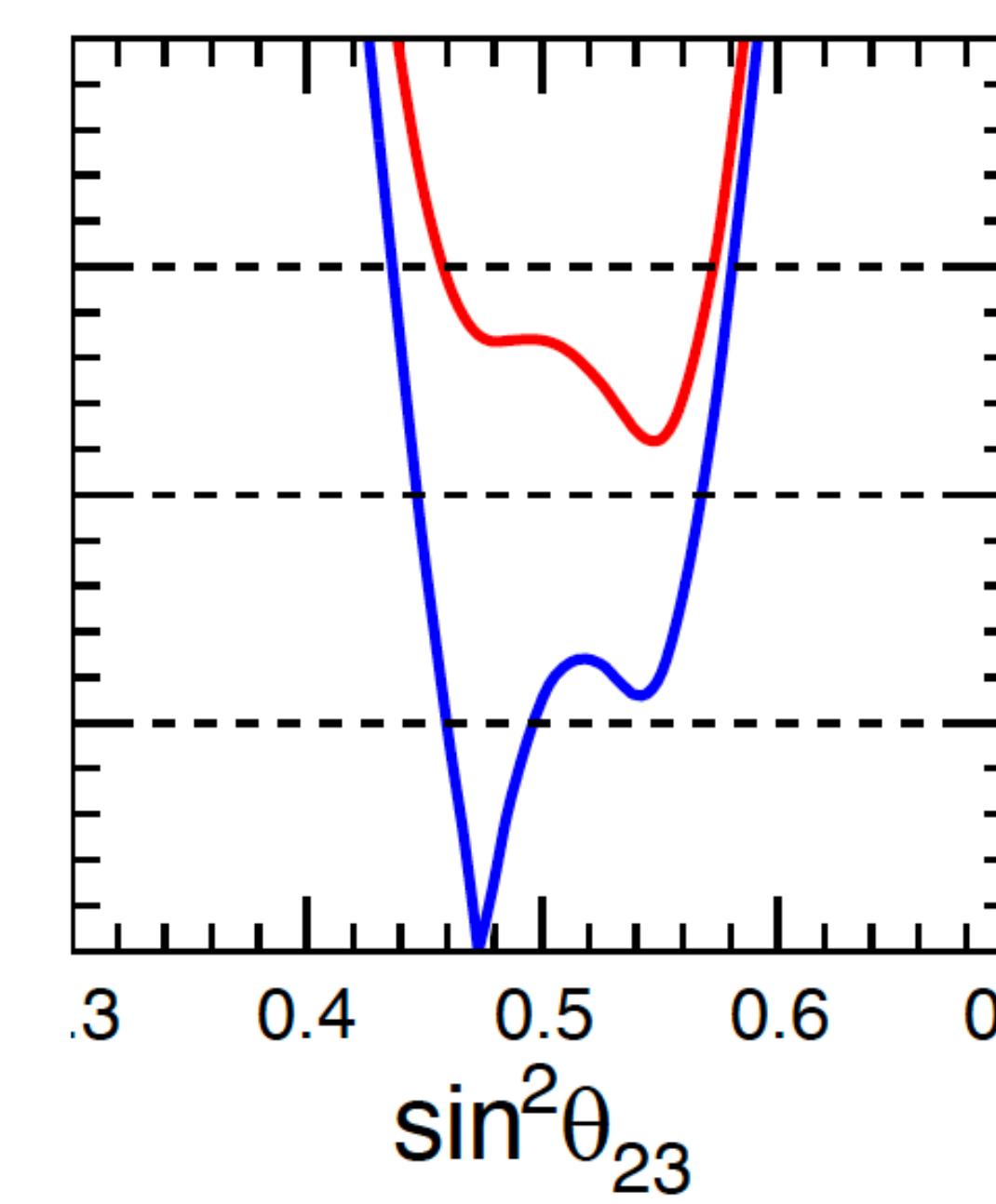
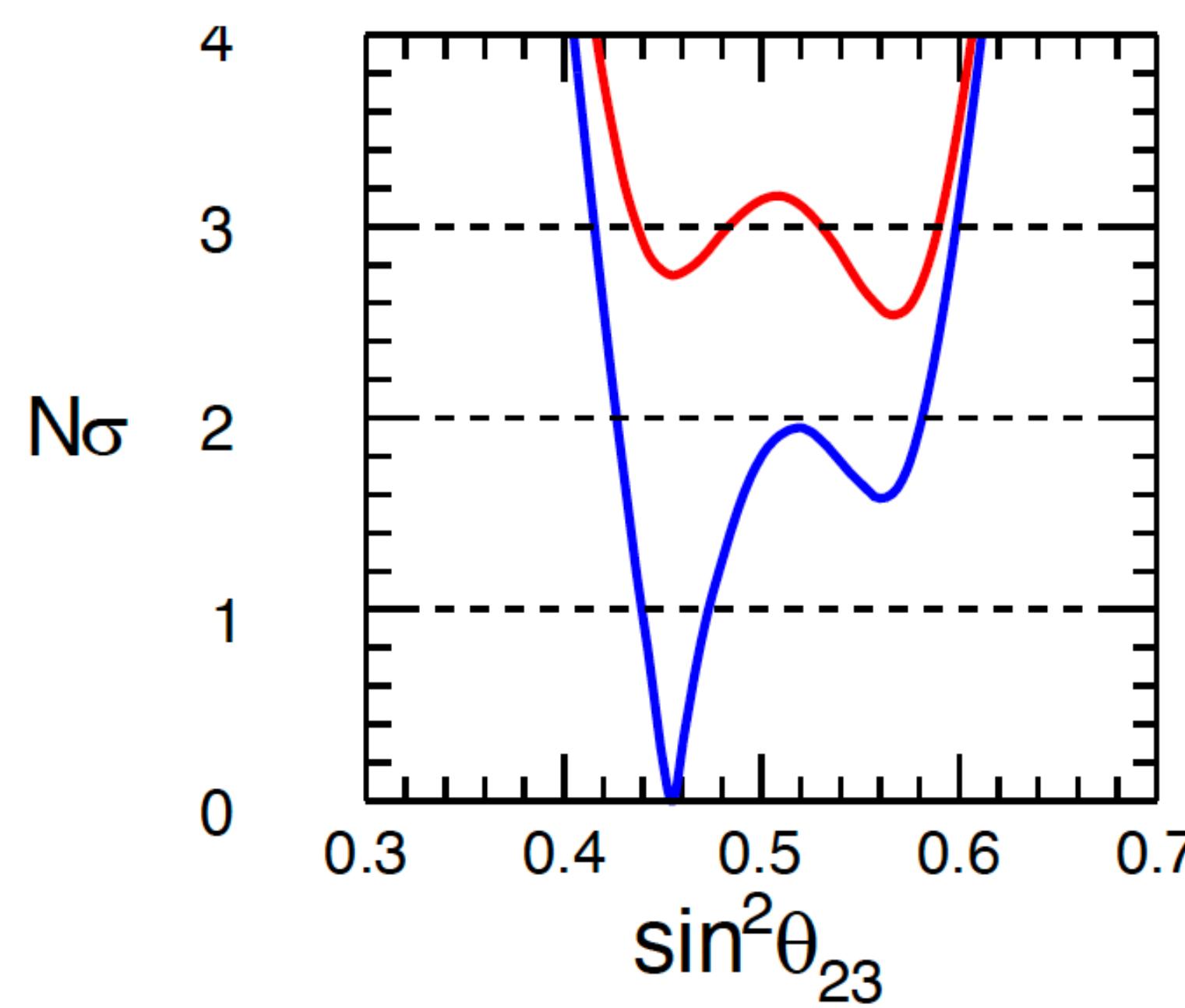
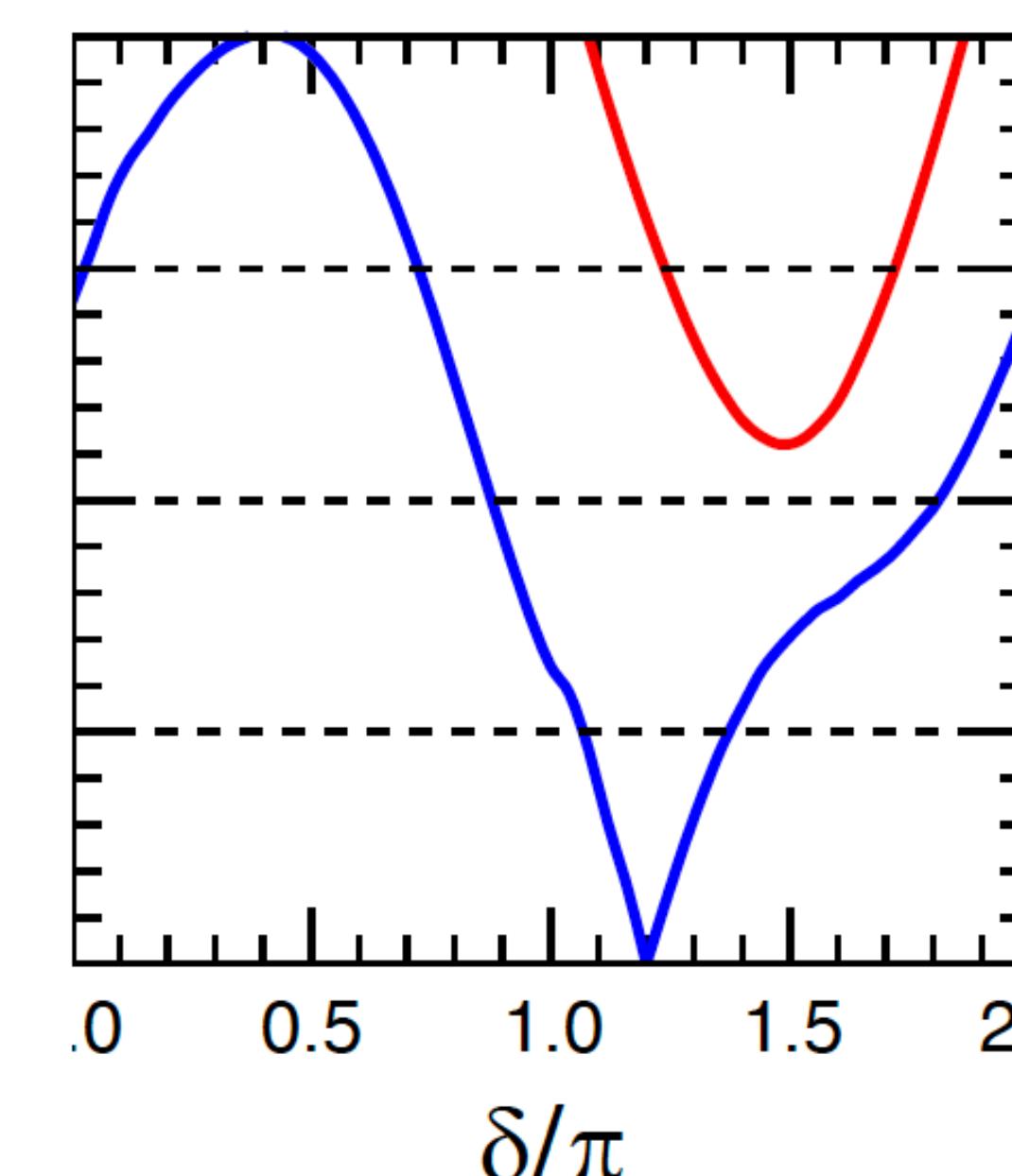
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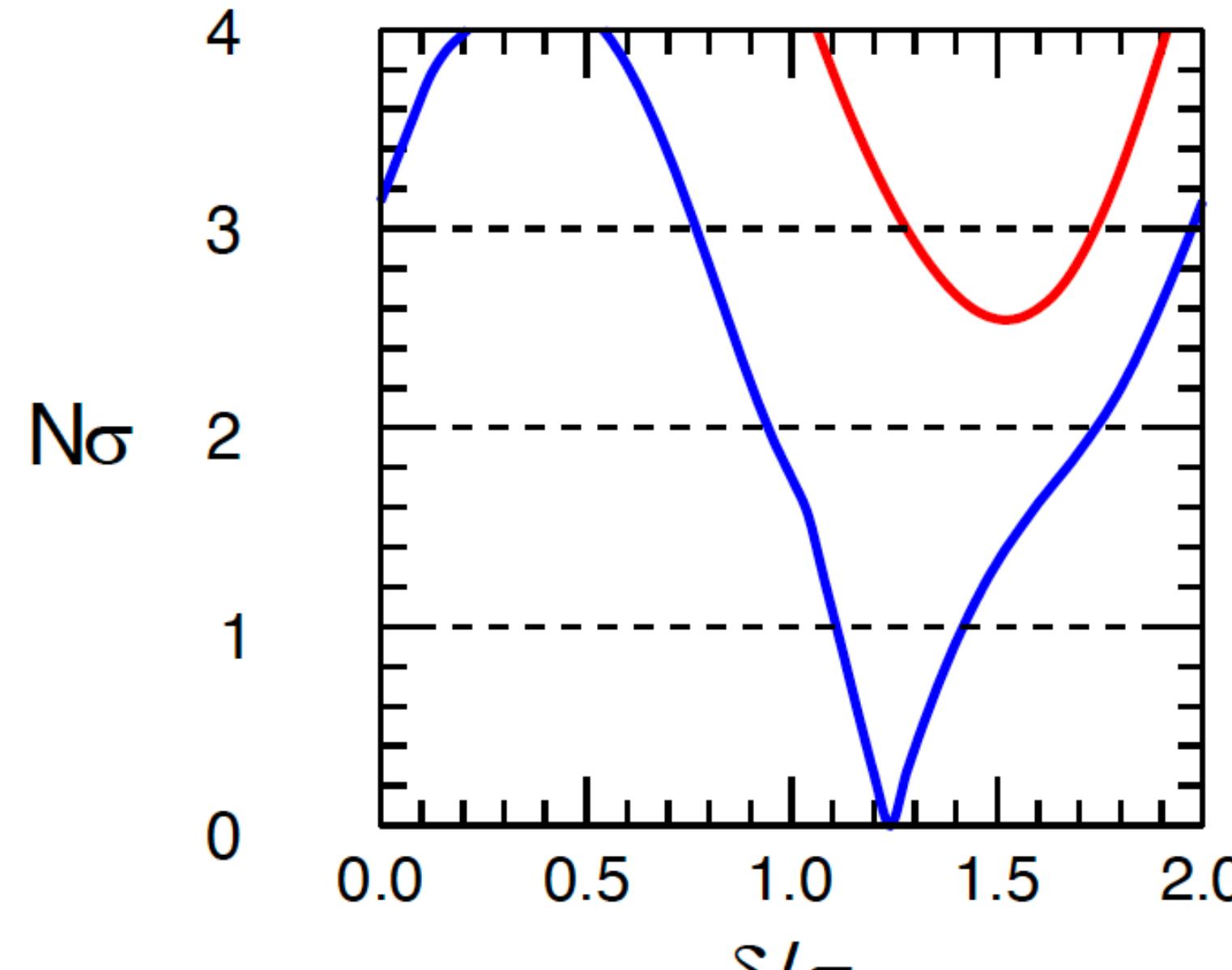
2025



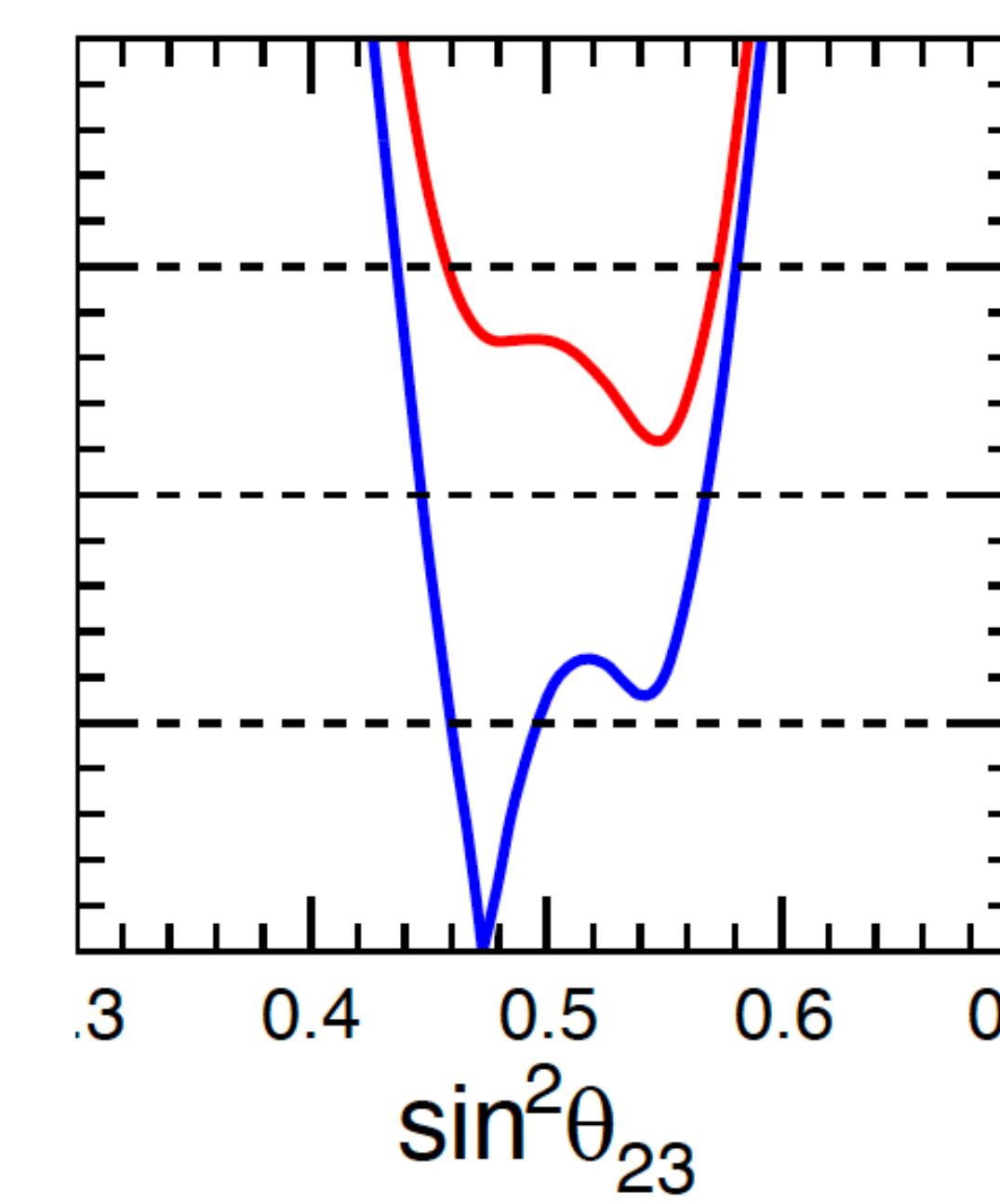
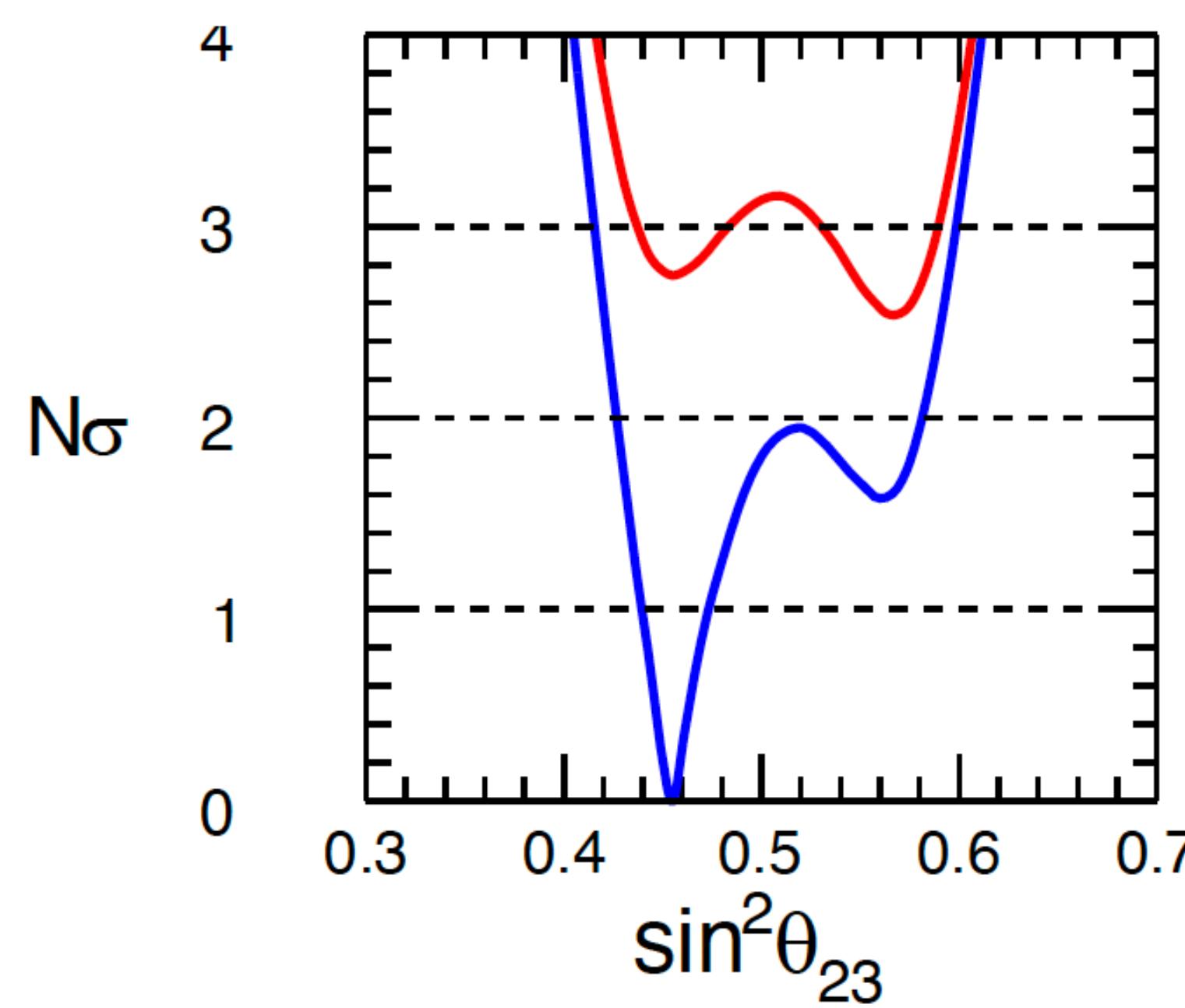
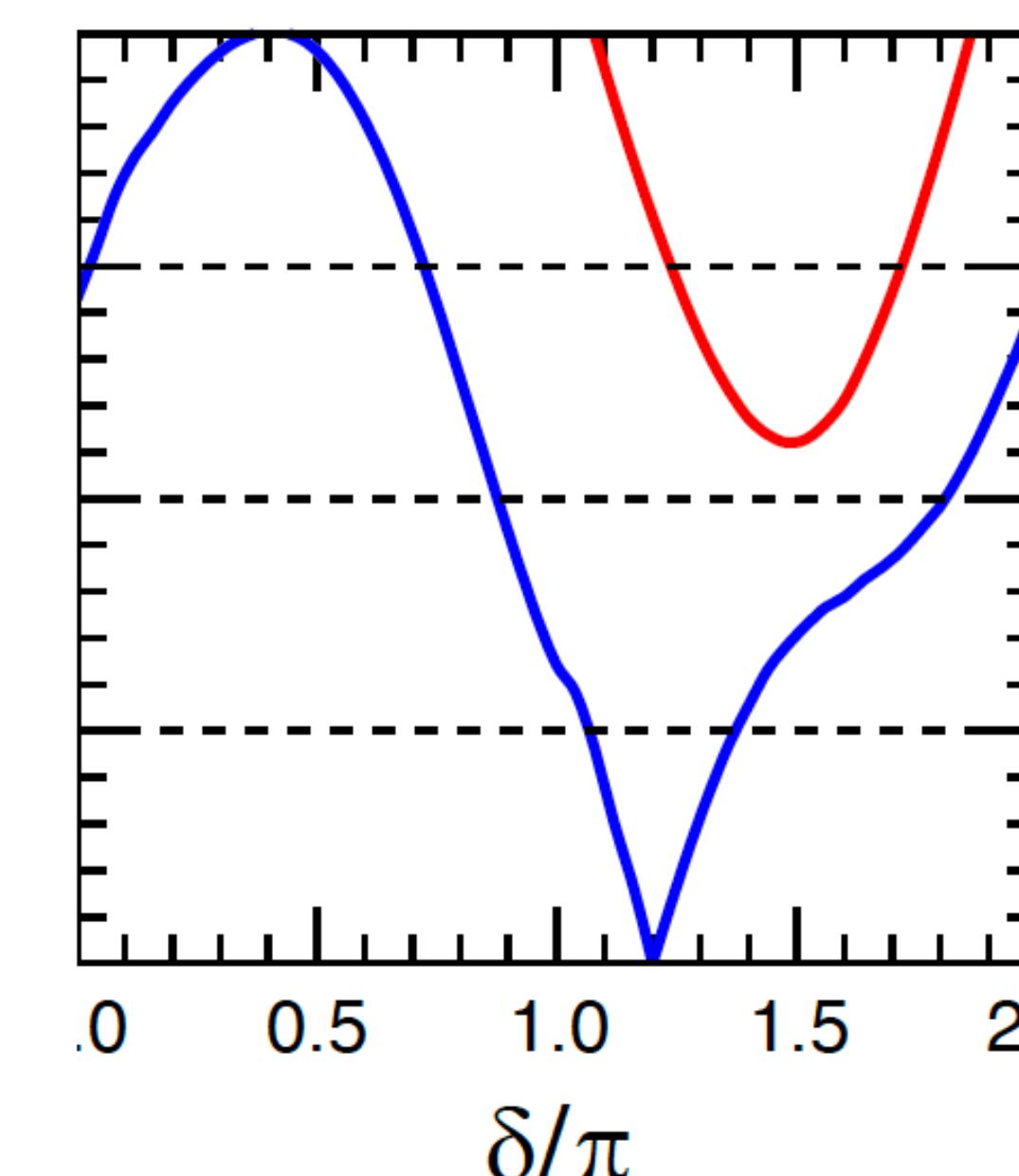
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Weaker hint for NO
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Closer and more
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TABLE I. Global 3ν oscillation analysis: best-fit values and allowed ranges at $N_\sigma = 1, 2, 3$, for either NO or IO. The last column shows the formal “ 1σ parameter accuracy,” defined as $1/6$ of the 3σ range, divided by the best-fit value (in percent). We recall that $\Delta m^2 = m_3^2 - (m_1^2 + m_2^2)/2$ and that δ/π is cyclic (mod 2). Last row: $\Delta\chi^2$ offset between IO and NO.

Parameter	Ordering	Best fit	1σ range	2σ range	3σ range	“ 1σ ” (%)
$\delta m^2/10^{-5}$ eV 2	NO, IO	7.37	7.21–7.52	7.06–7.71	6.93–7.93	2.3
$\sin^2 \theta_{12}/10^{-1}$	NO, IO	3.03	2.91–3.17	2.77–3.31	2.64–3.45	4.5
$ \Delta m^2 /10^{-3}$ eV 2	NO	2.495	2.475–2.515	2.454–2.536	2.433–2.558	0.8
	IO	2.465	2.444–2.485	2.423–2.506	2.403–2.527	0.8
$\sin^2 \theta_{13}/10^{-2}$	NO	2.23	2.17–2.27	2.11–2.33	2.06–2.38	2.4
	IO	2.23	2.19–2.30	2.14–2.35	2.08–2.41	2.4
$\sin^2 \theta_{23}/10^{-1}$	NO	4.73	4.60–4.96	4.47–5.68	4.37–5.81	5.1
	IO	5.45	5.28–5.60	4.58–5.73	4.43–5.83	4.3
δ/π	NO	1.20	1.07–1.37	0.88–1.81	0.73–2.03	18
	IO	1.48	1.36–1.61	1.24–1.72	1.12–1.83	8
$\Delta\chi^2_{\text{IO-NO}}$	IO-NO	+5.0				

Percent accuracy on “known” parameters

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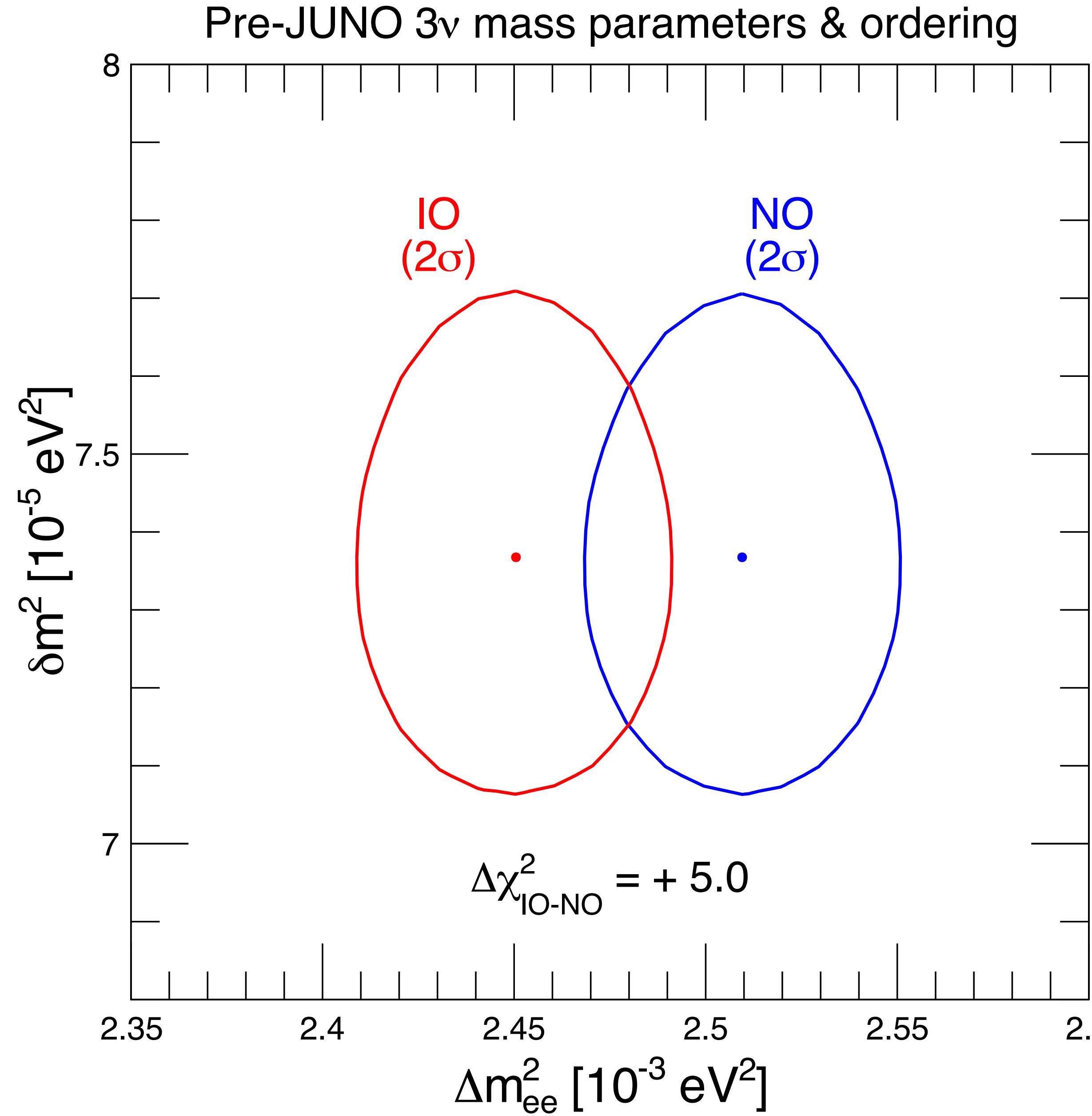
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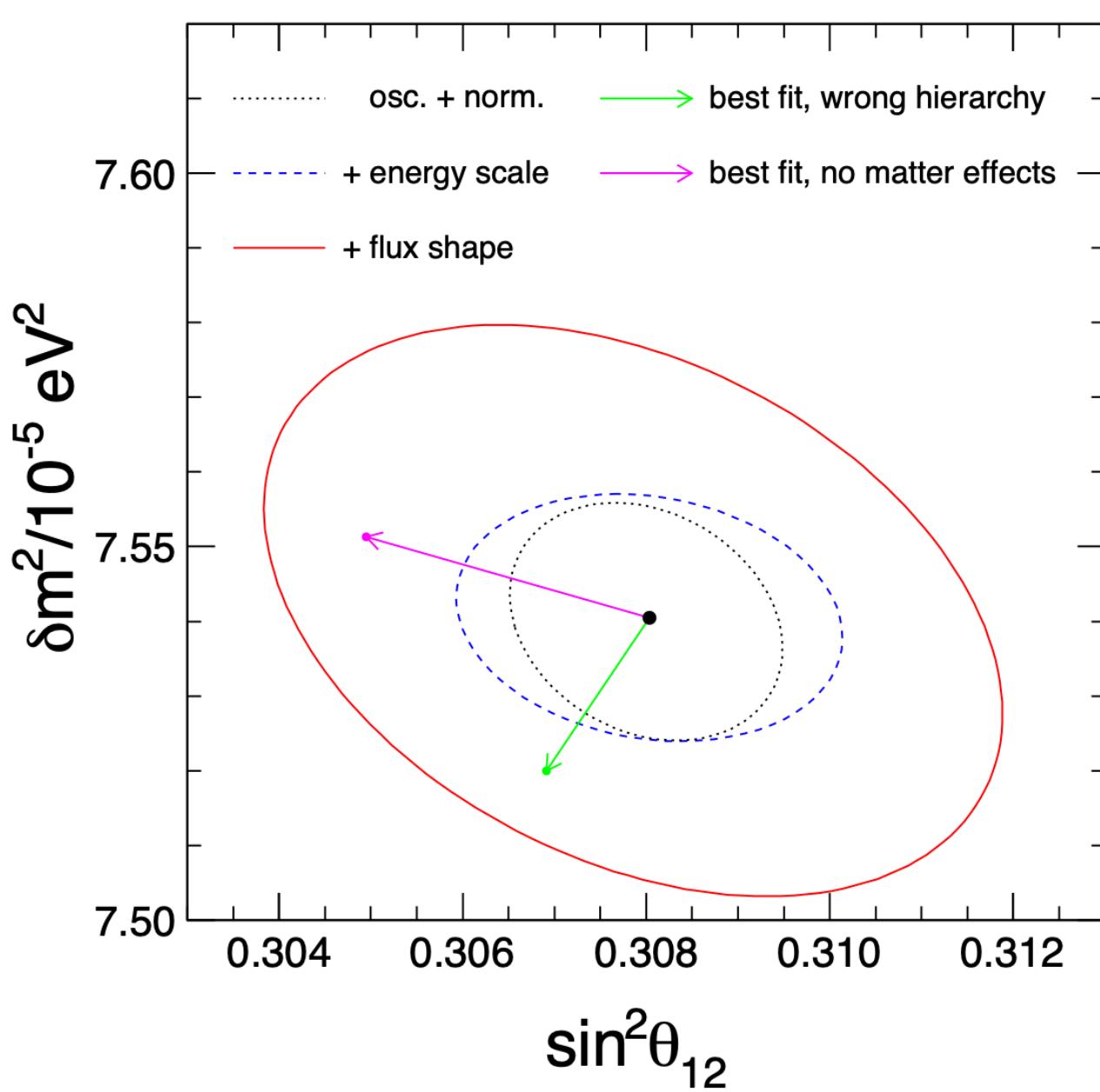
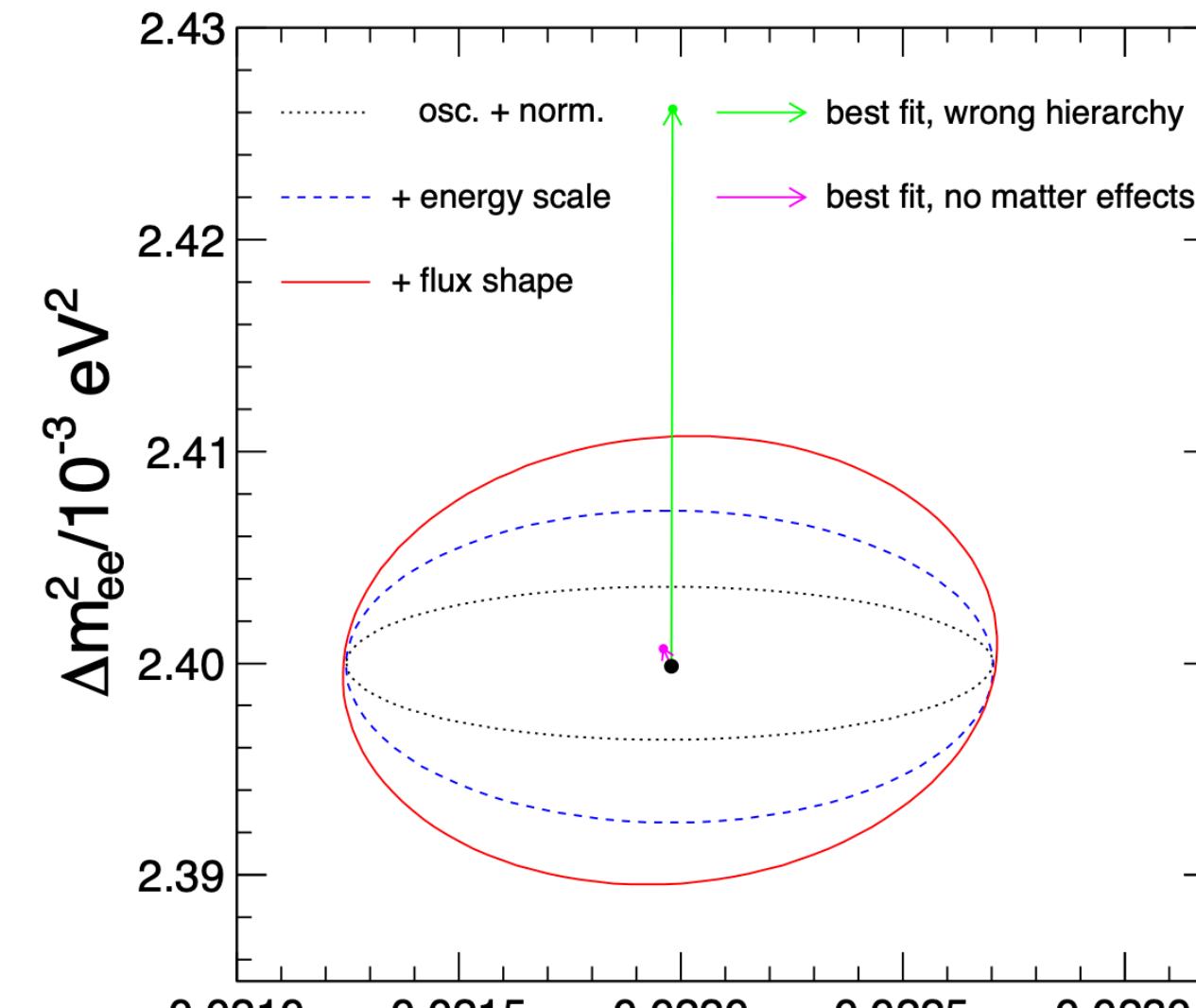
However, one should be cautious about interpreting subpercent-level accuracies, since correlated effects from neutrino energy reconstruction, interaction models, and systematic uncertainties across accelerator and atmospheric experiments still require significant improvement

Present knowledge about the two JUNO oscillation frequencies

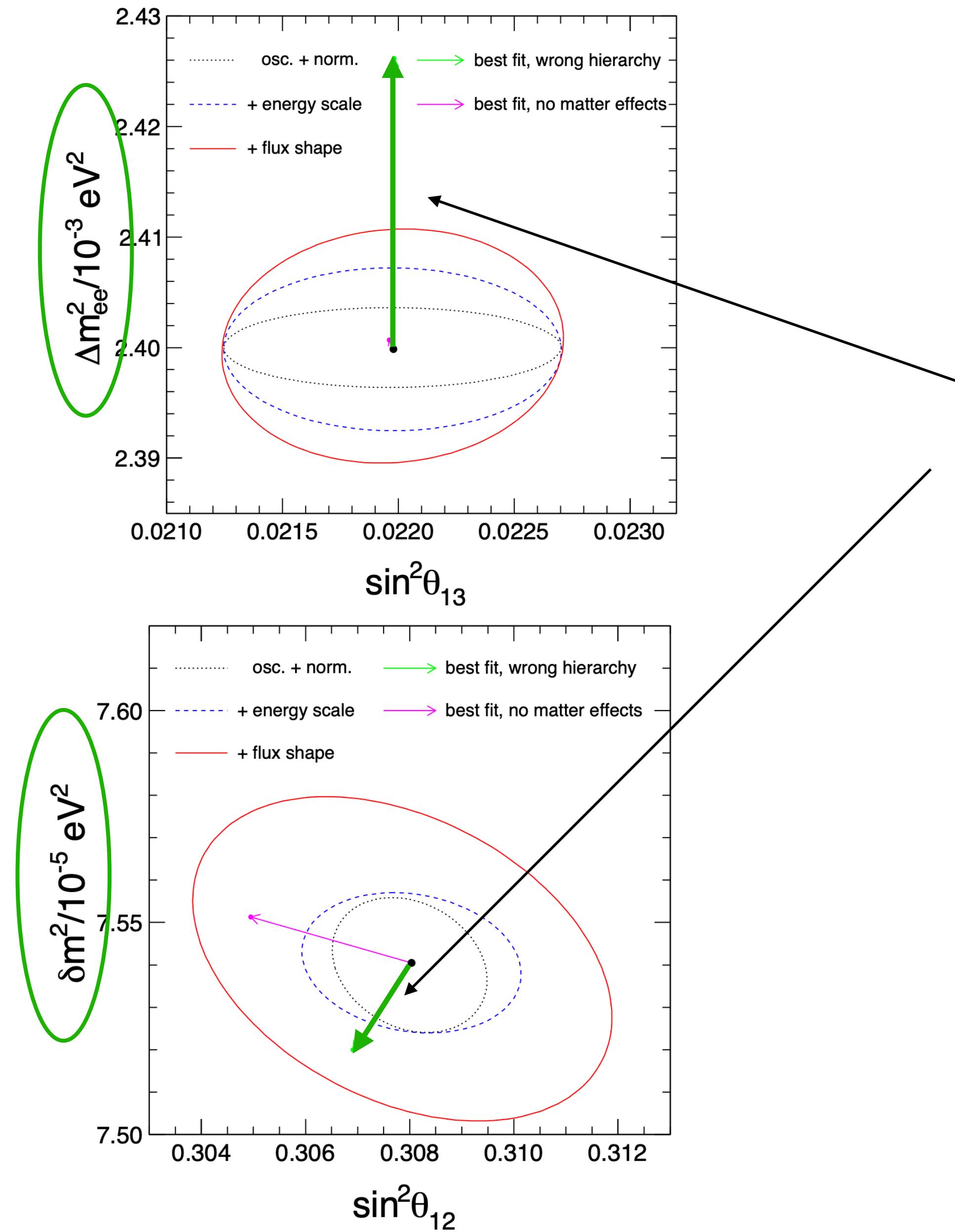
Present knowledge about the two JUNO oscillation frequencies



JUNO measurements will lead to
slightly displaced best fits for the
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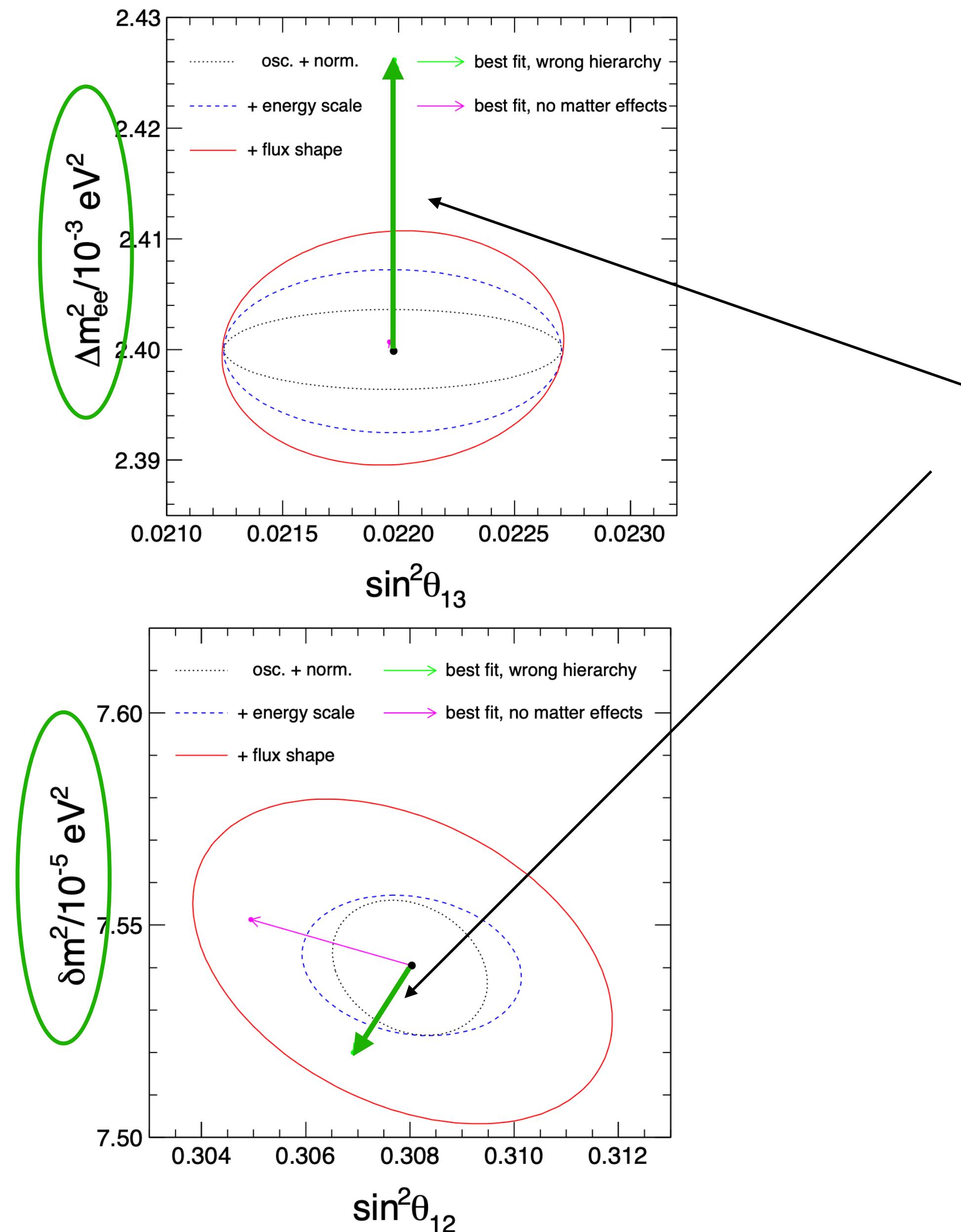


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Green arrows: shifts of best fits when passing from NO to IO assumption

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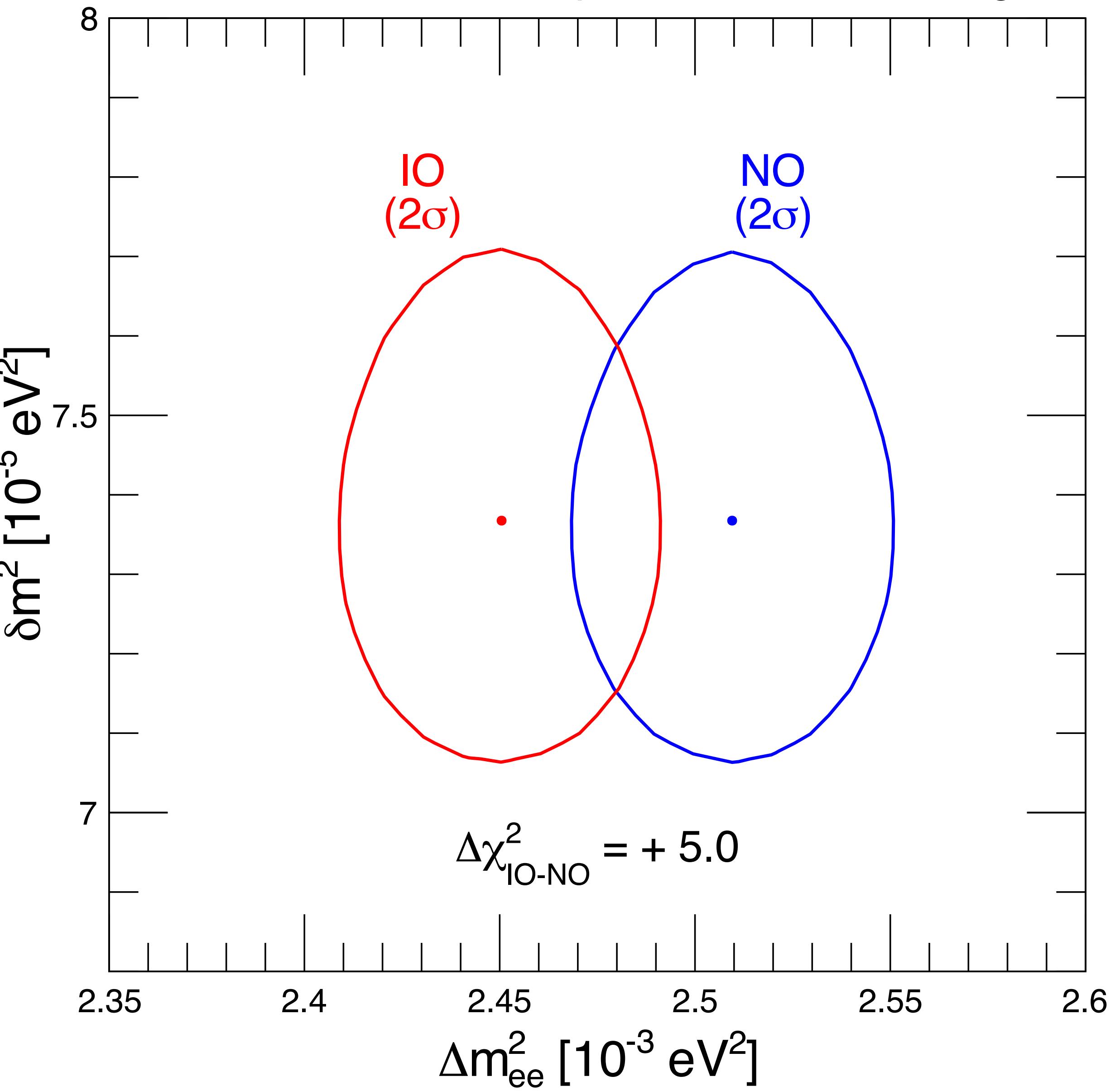


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JUNO measurements will lead to slightly displaced best fits for the two frequencies in NO and IO

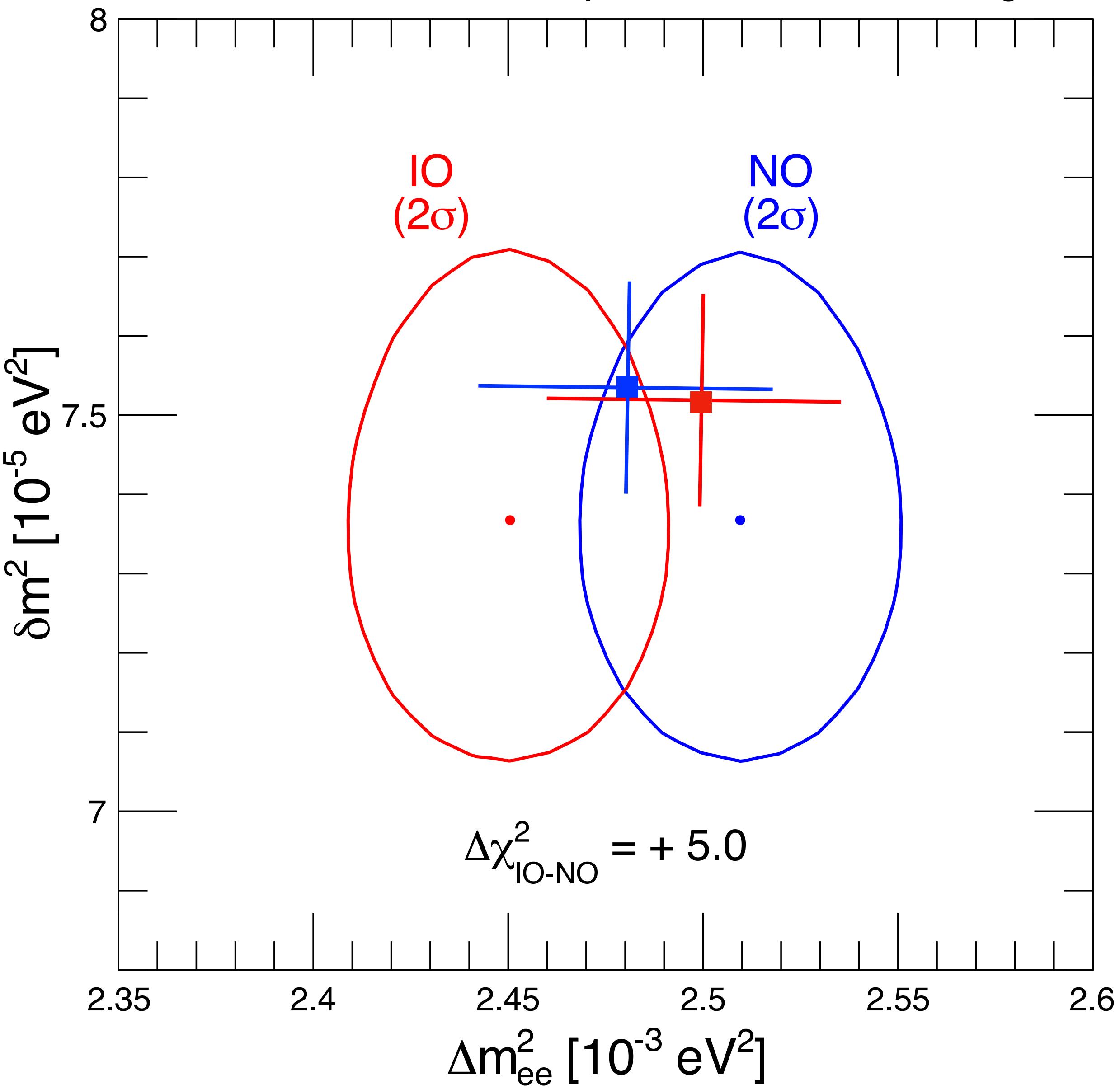
Shift of Δm^2 discussed in many papers (see Parke et al. for instance)
Specific values depend little on fit details.

Pre-JUNO 3v mass parameters & ordering



Typical relative displacement between
JUNO bestfit point in NO and IO

Pre-JUNO 3v mass parameters & ordering



Typical relative displacement between JUNO bestfit point in NO and IO

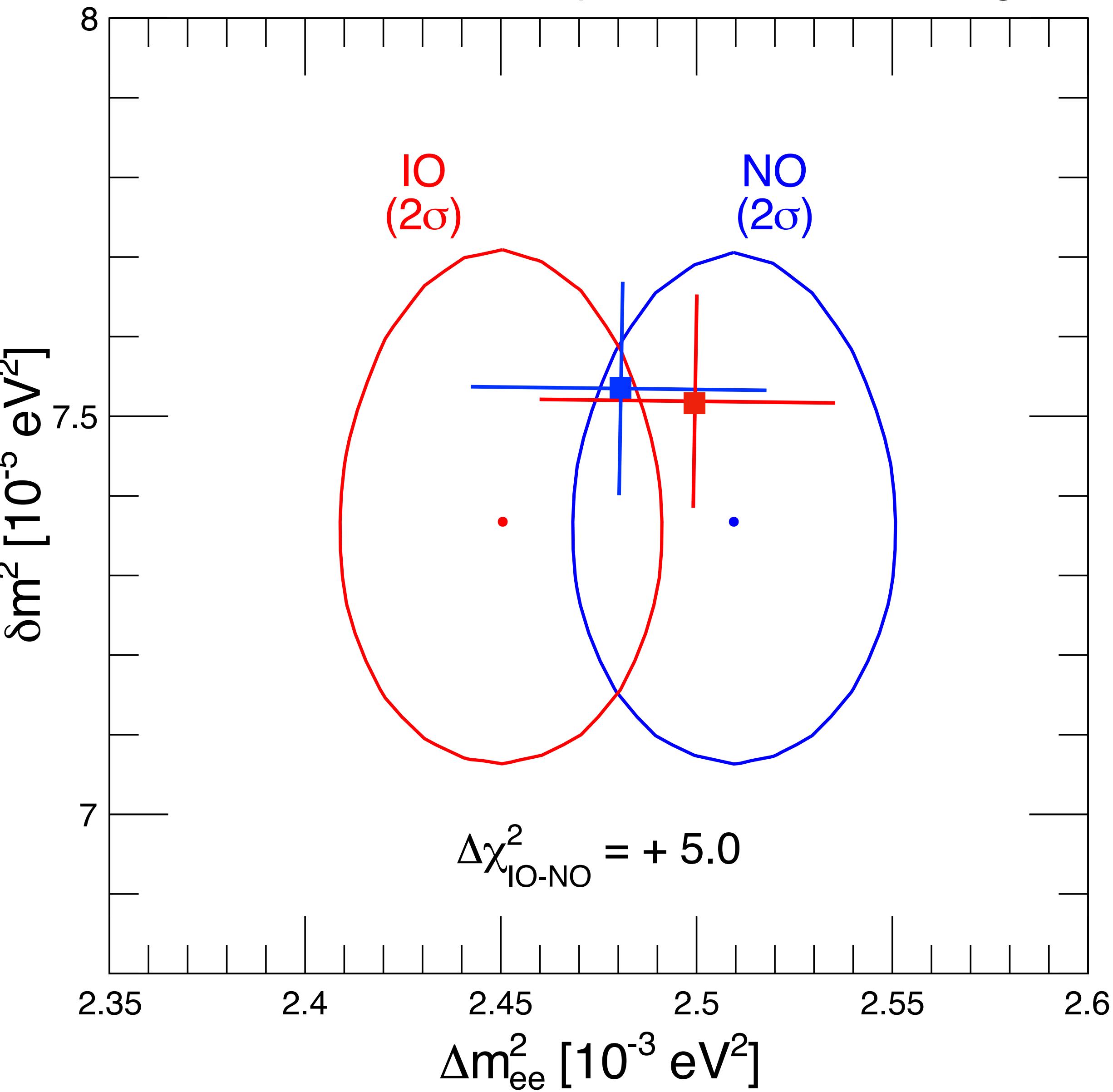
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$$\Delta m_{ee}^2 (2\sigma) \sim 0.04 \times 10^{-3} \text{ eV}^2$$

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To cite this article: Angel Abusleme *et al* 2022 *Chinese Phys. C* **46** 123001

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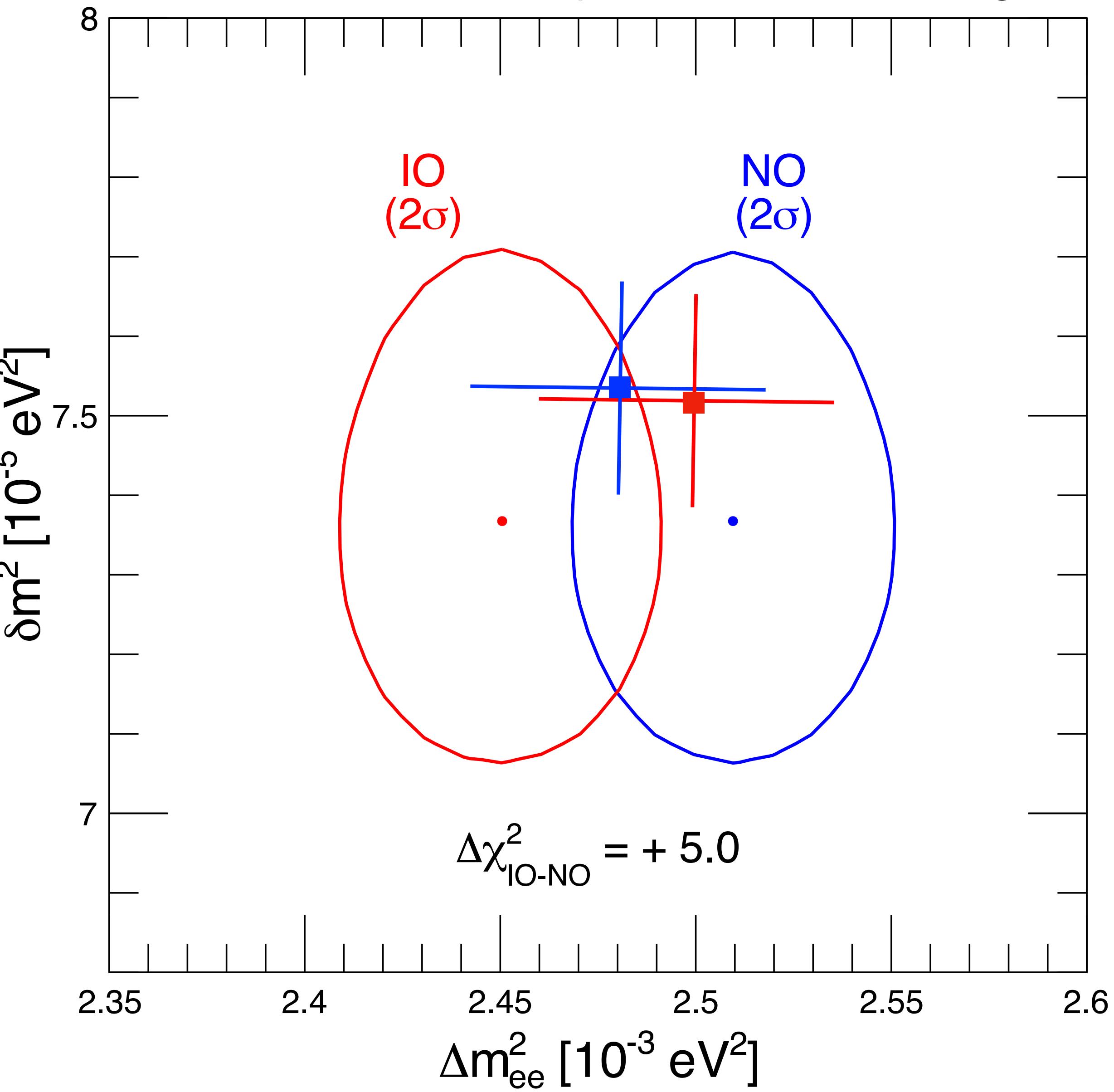
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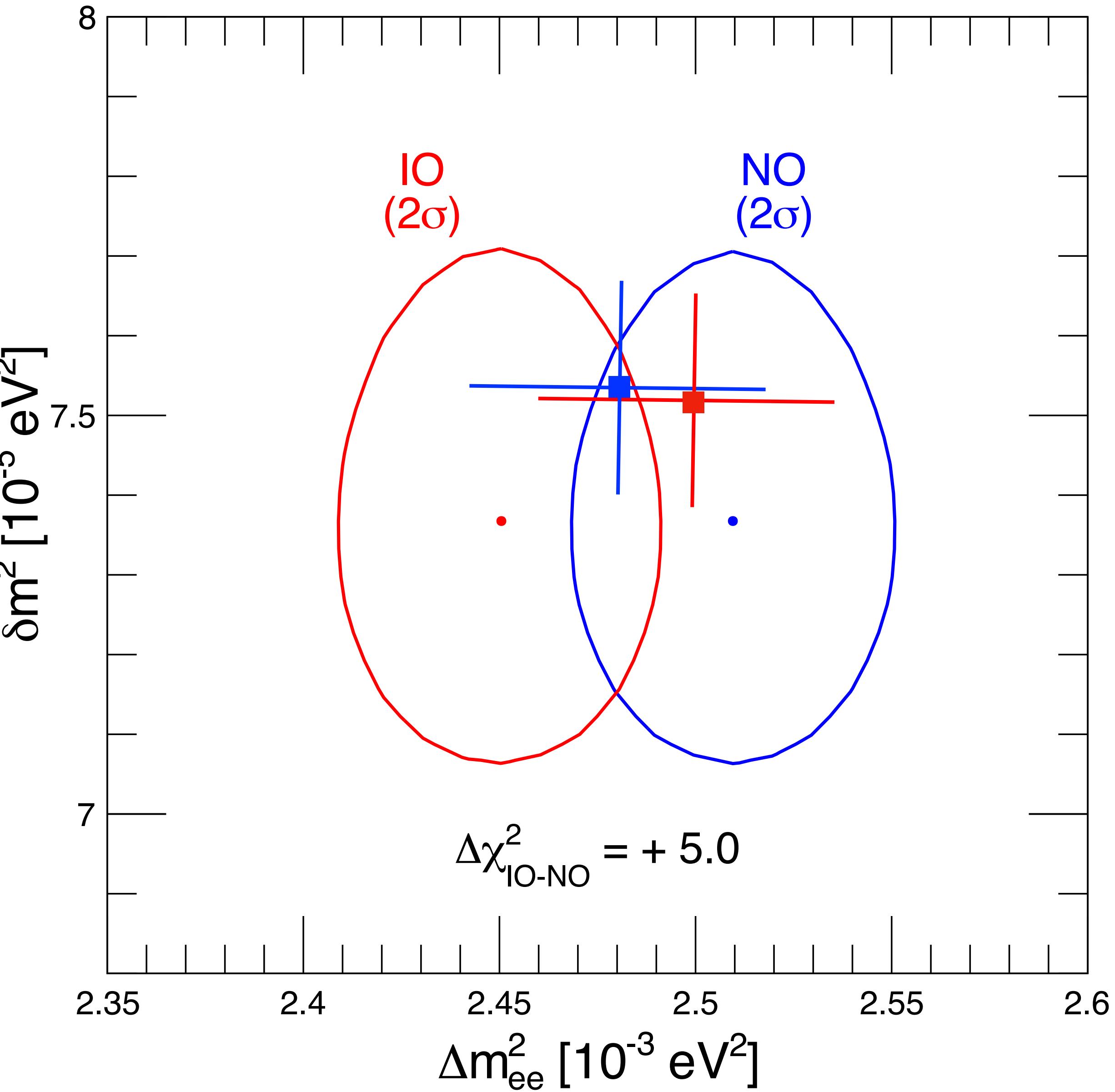
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While statistical fluctuations can initially mask the distinction between NO and IO, with higher exposure the true difference is expected to become evident

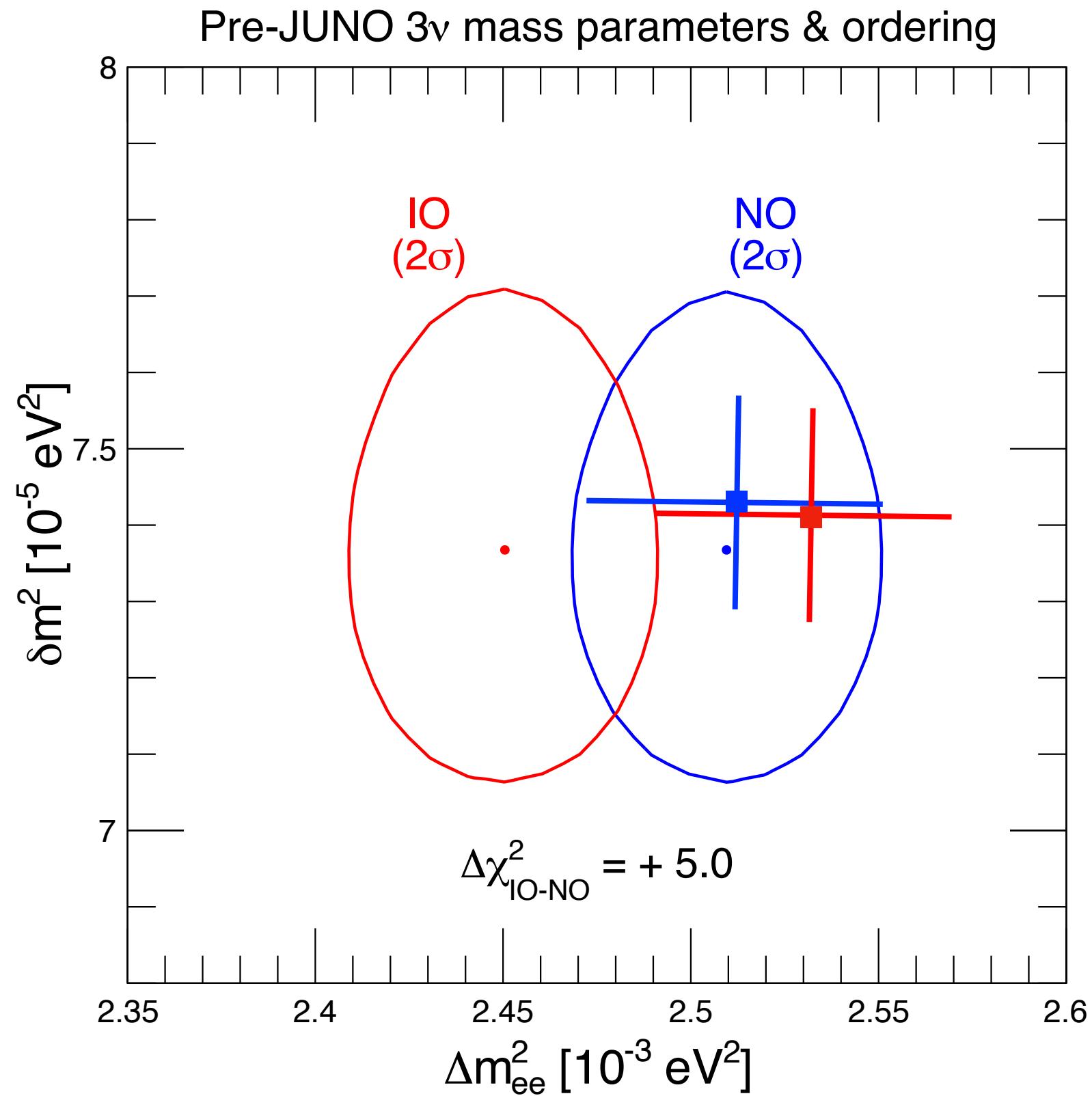
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Examples of possible JUNO first data compared with pre-JUNO data

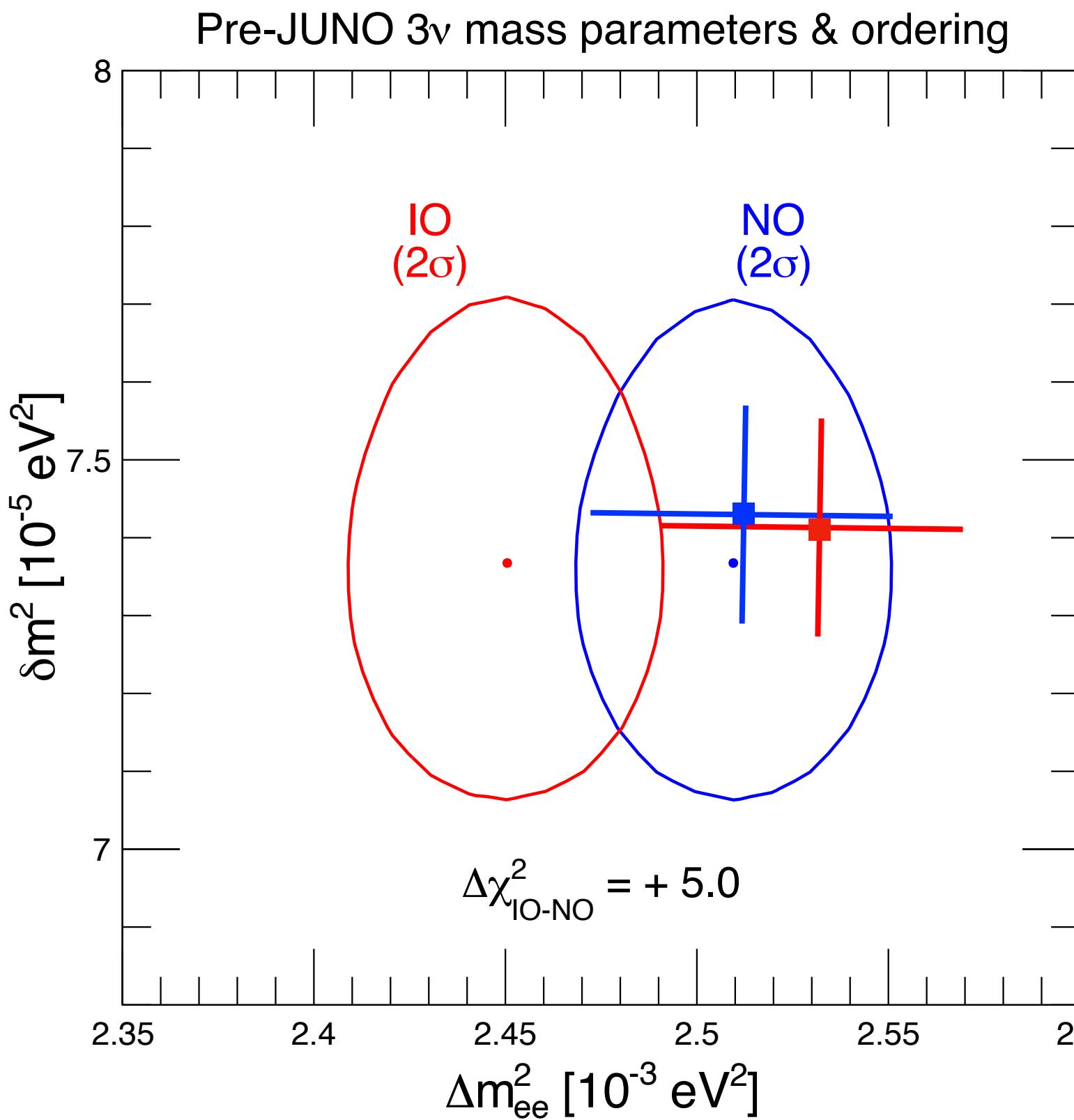
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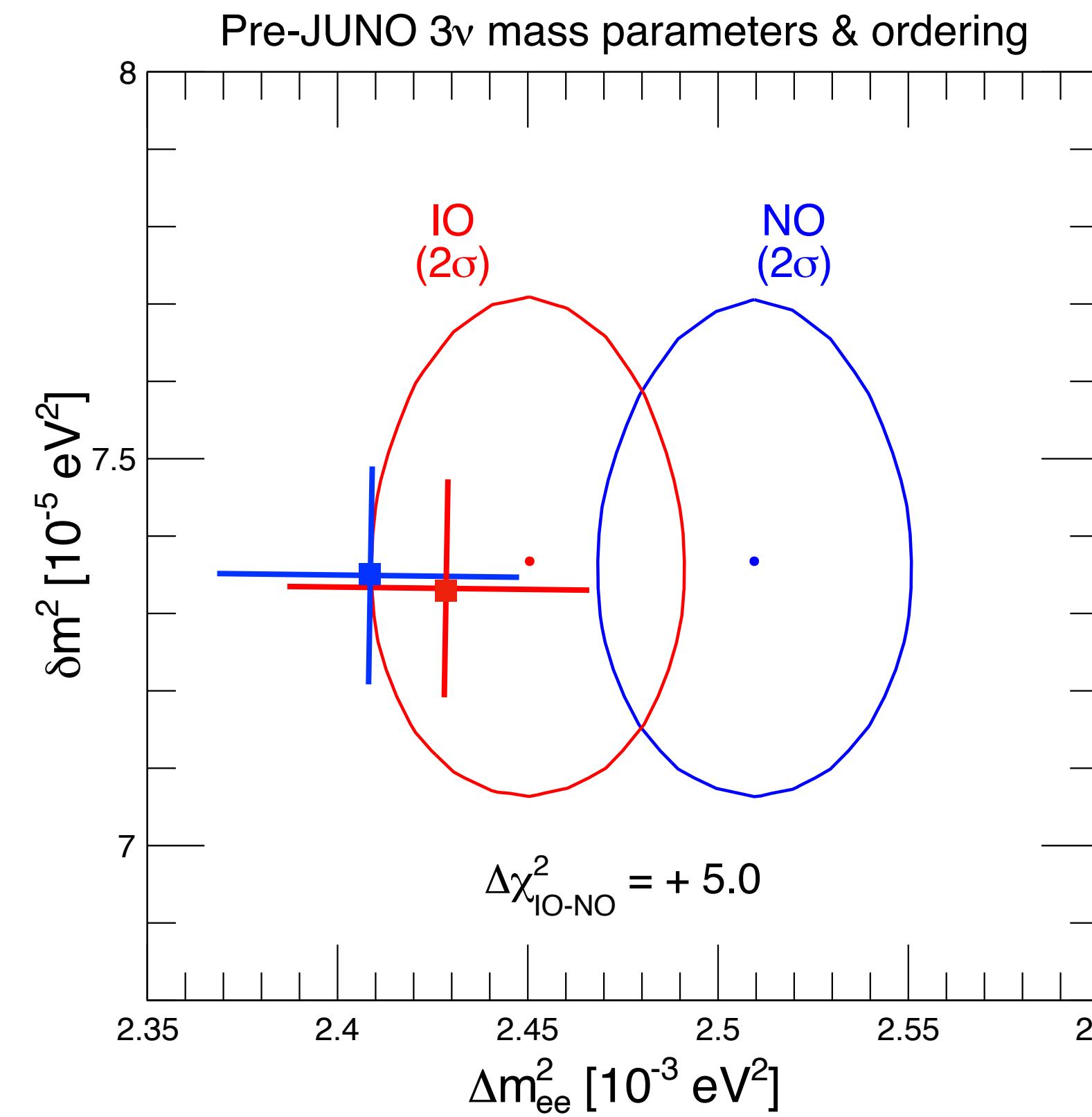


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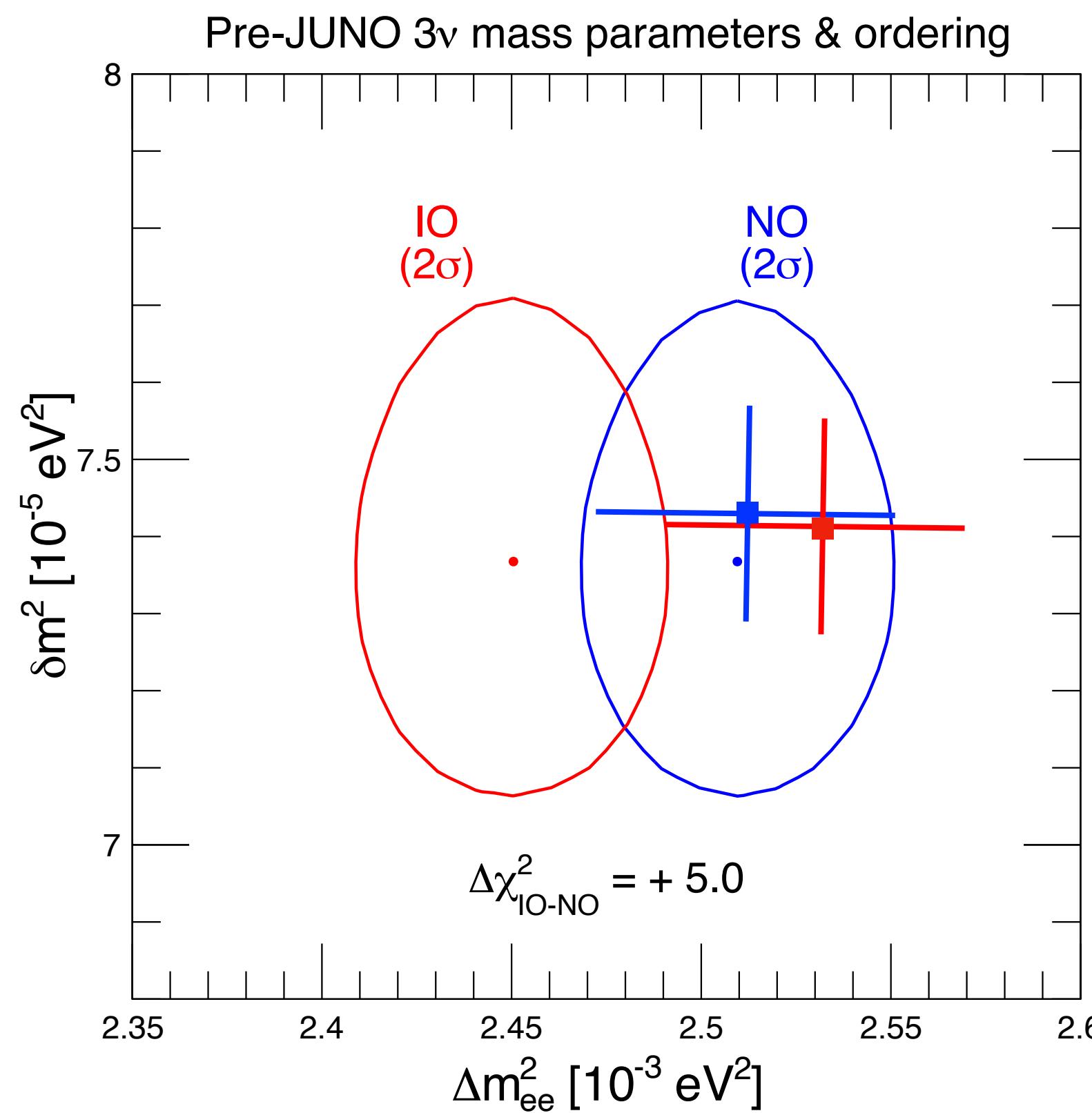


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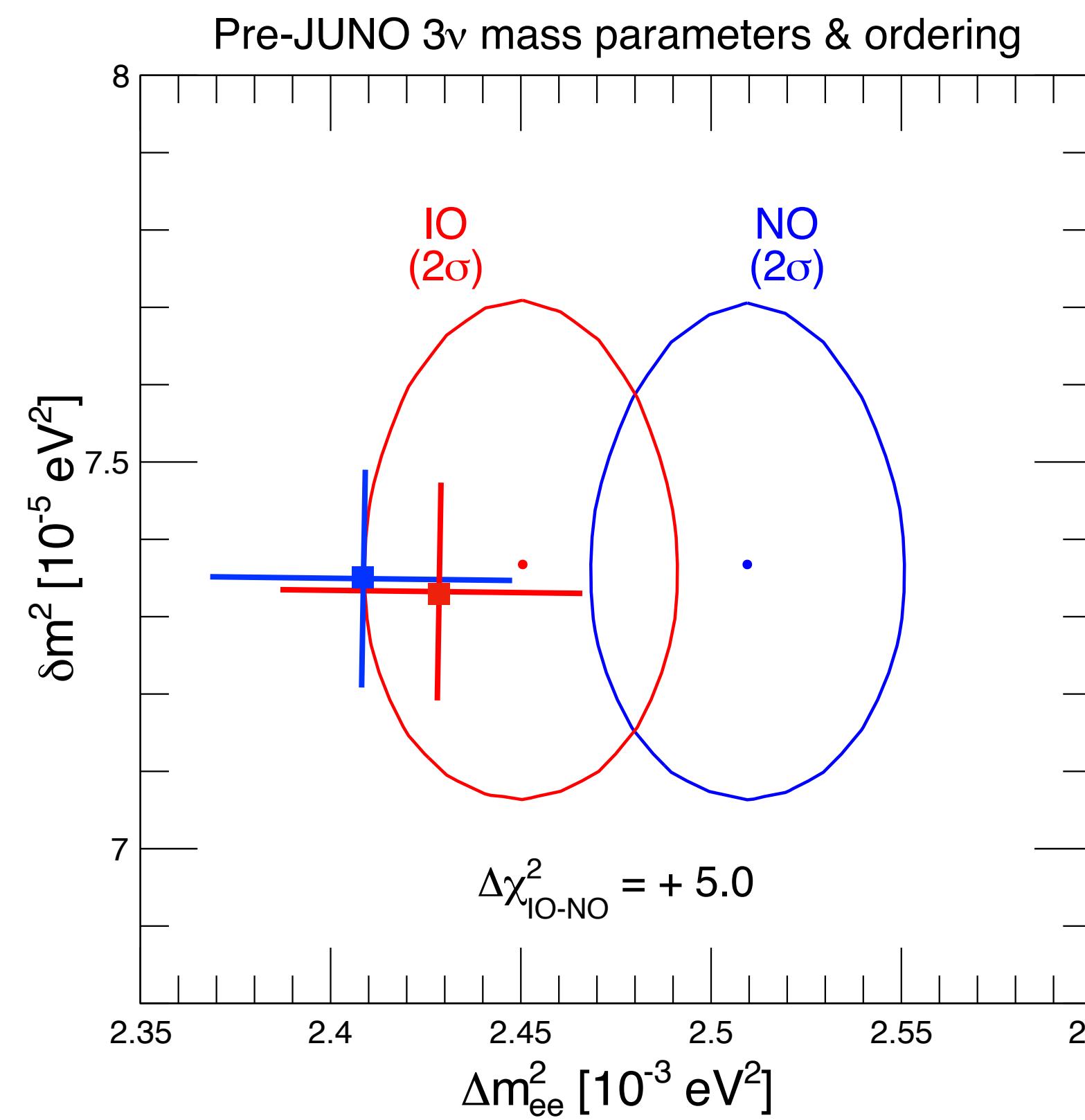


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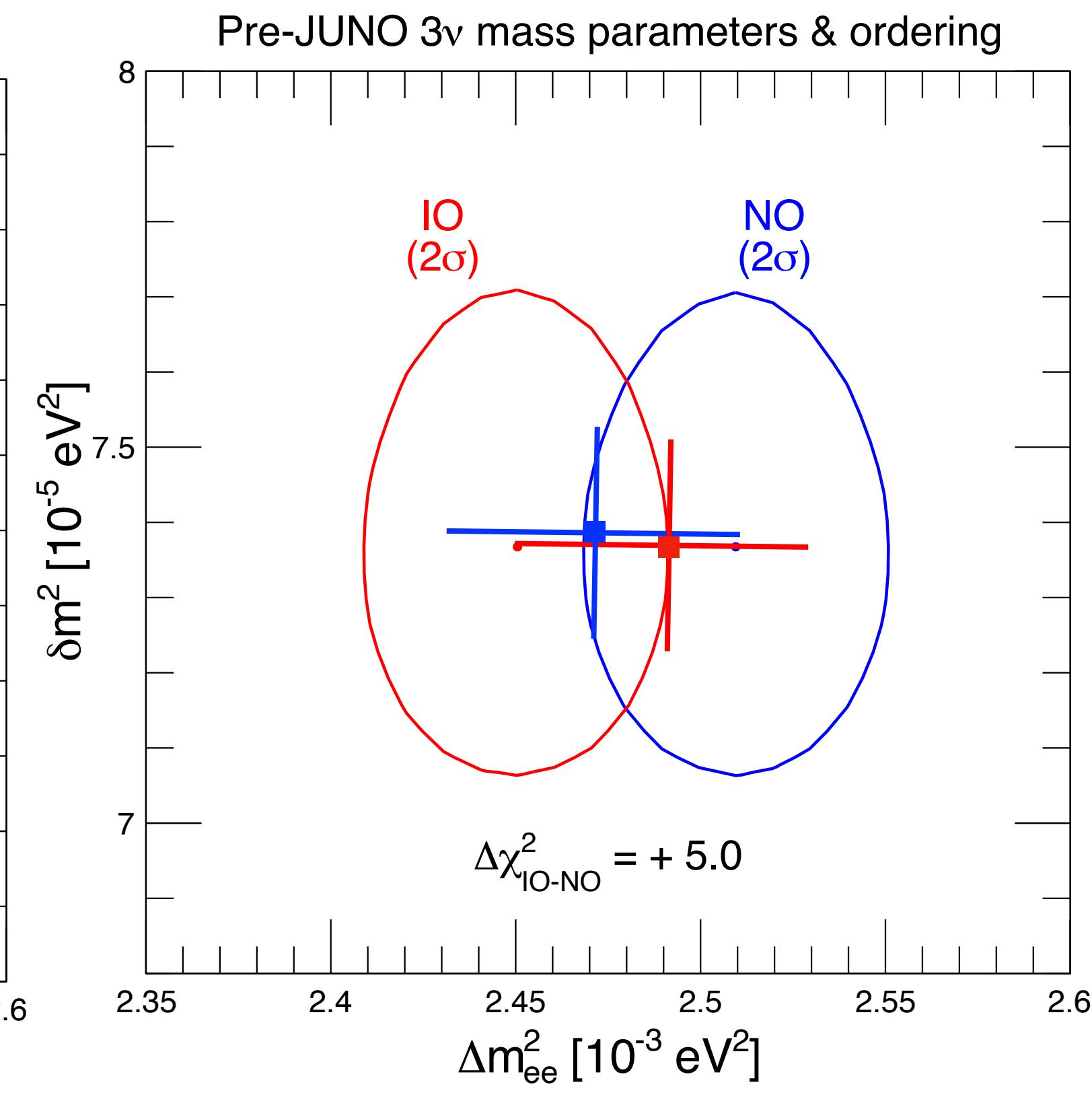
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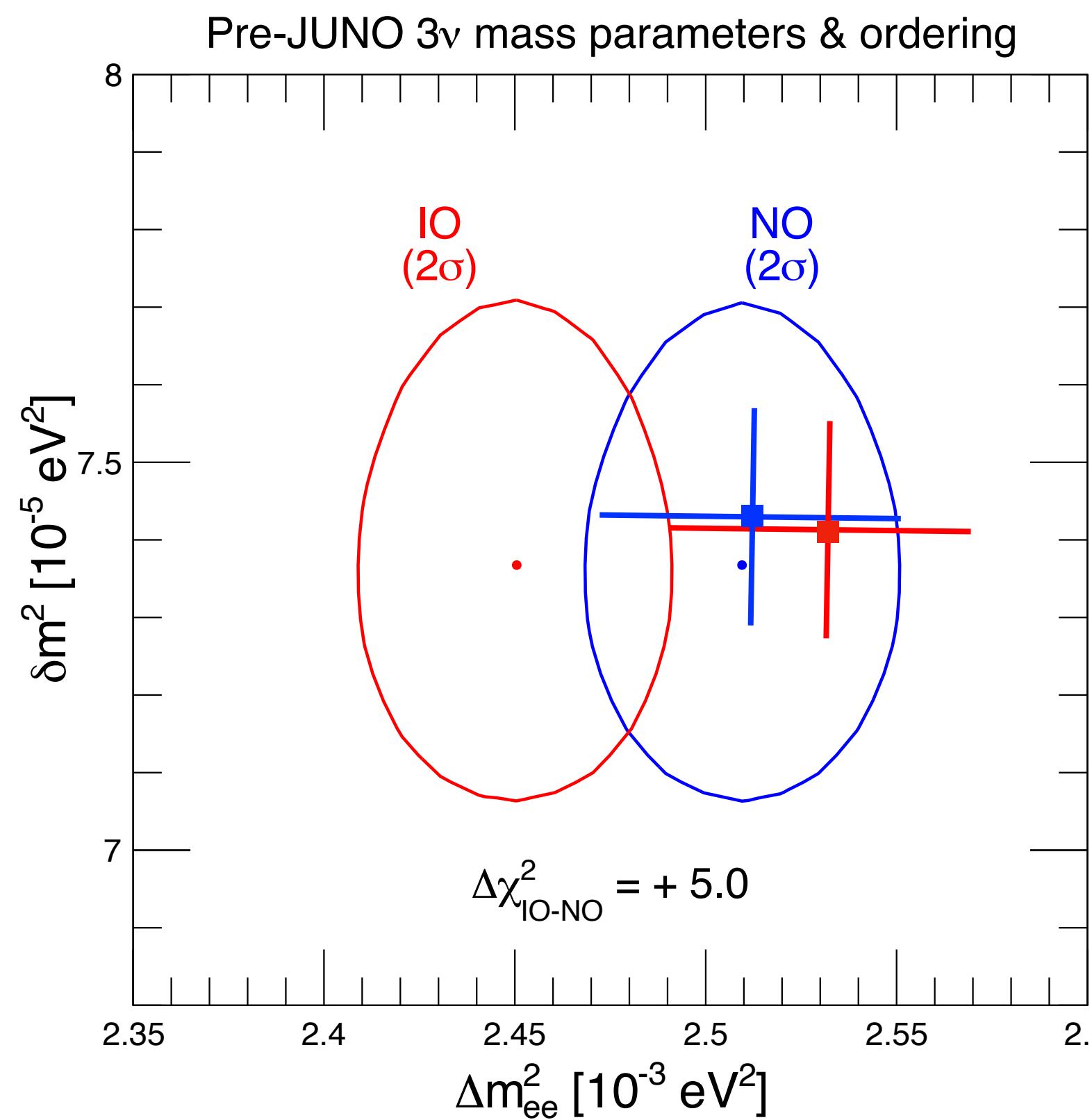


An undecided NO/IO

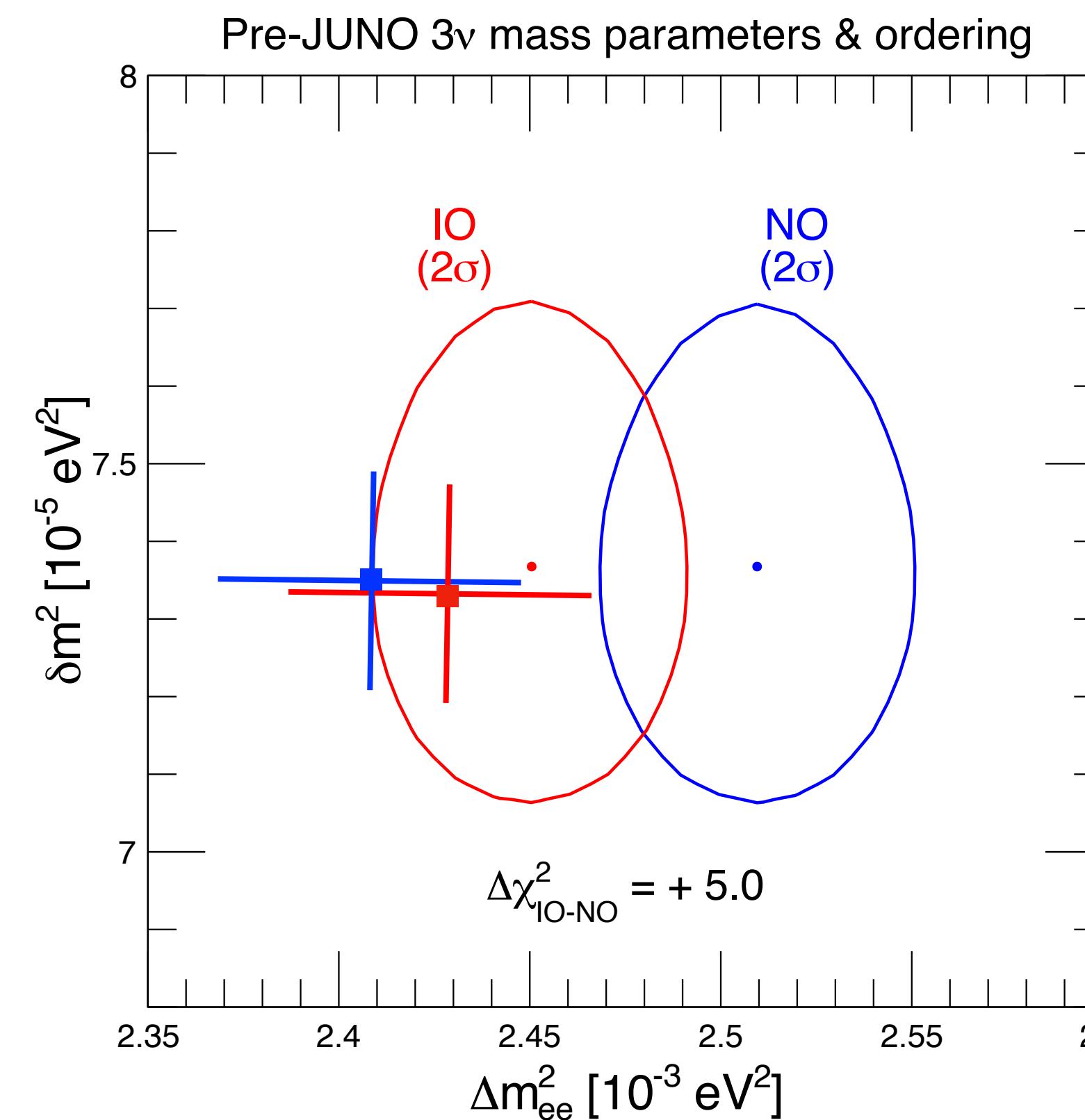


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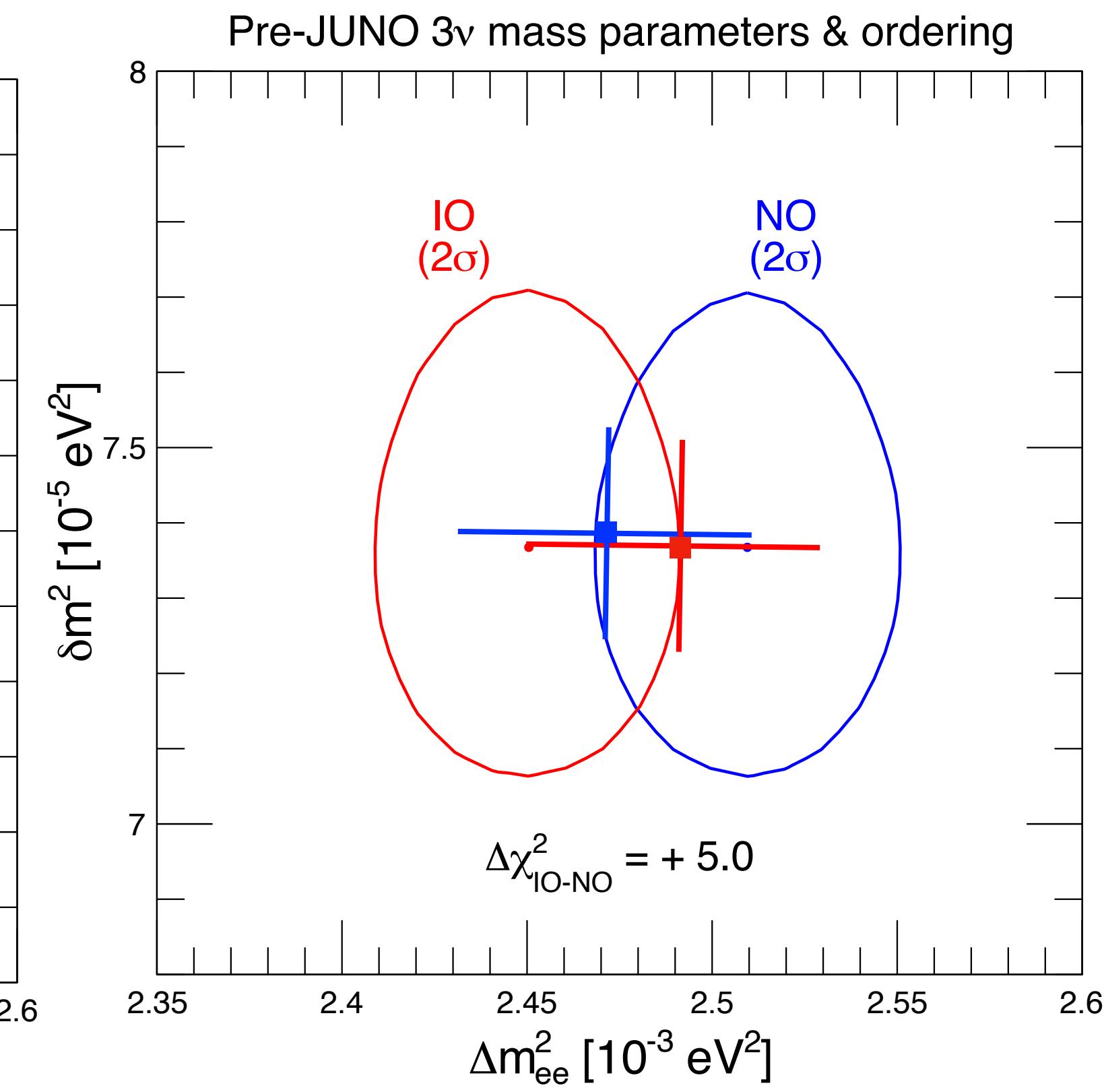
Asynergy favoring NO



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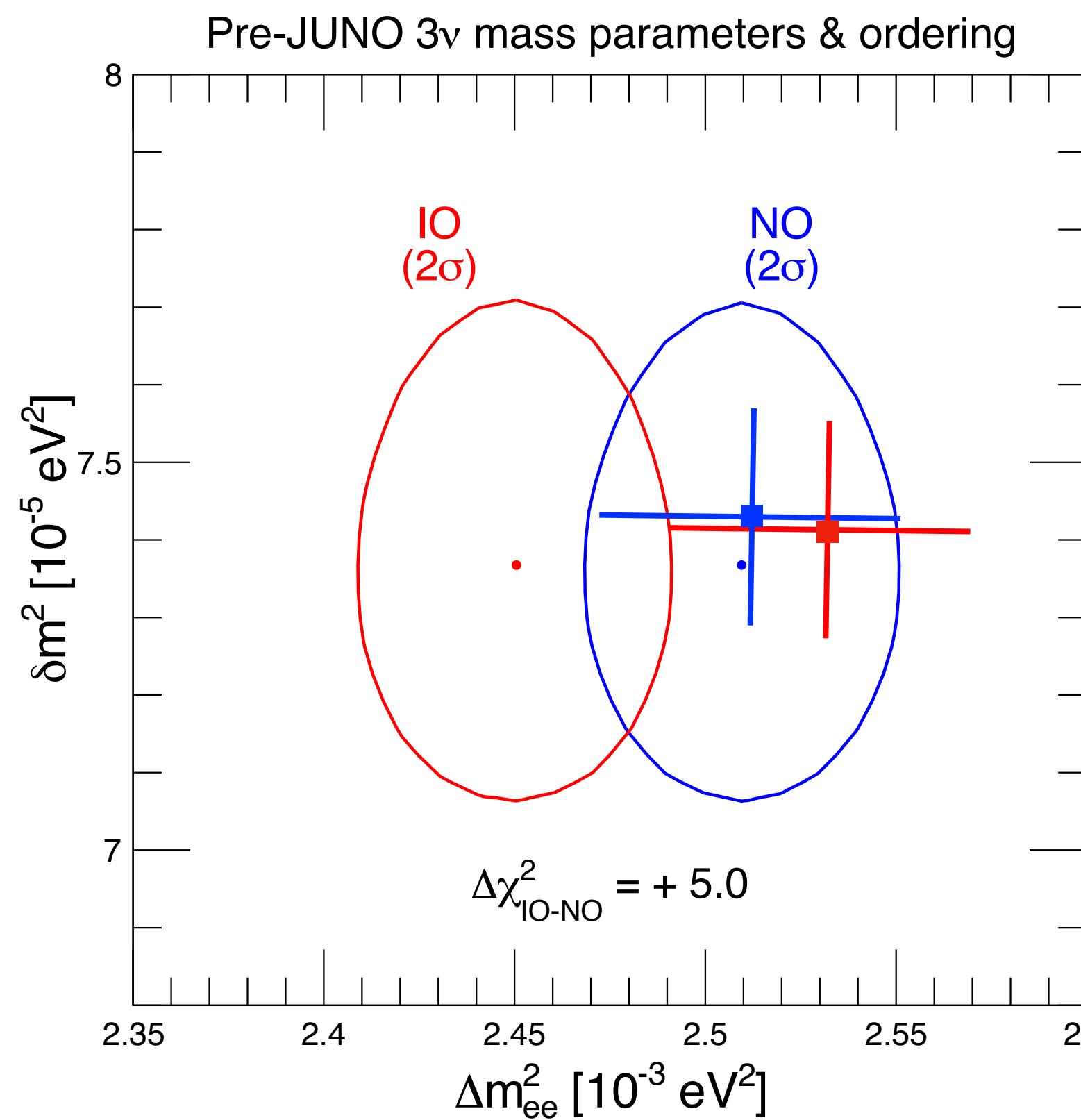
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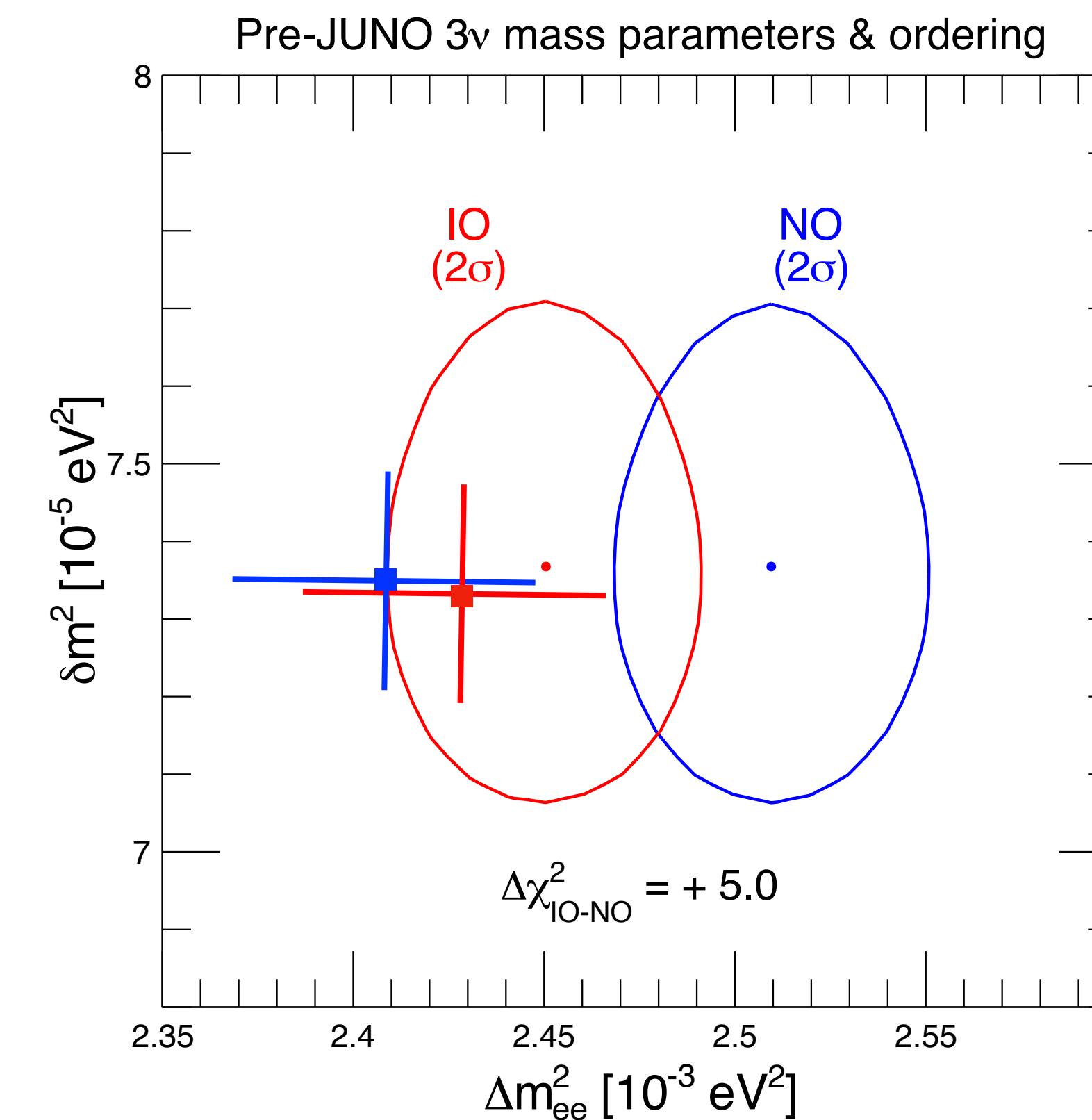
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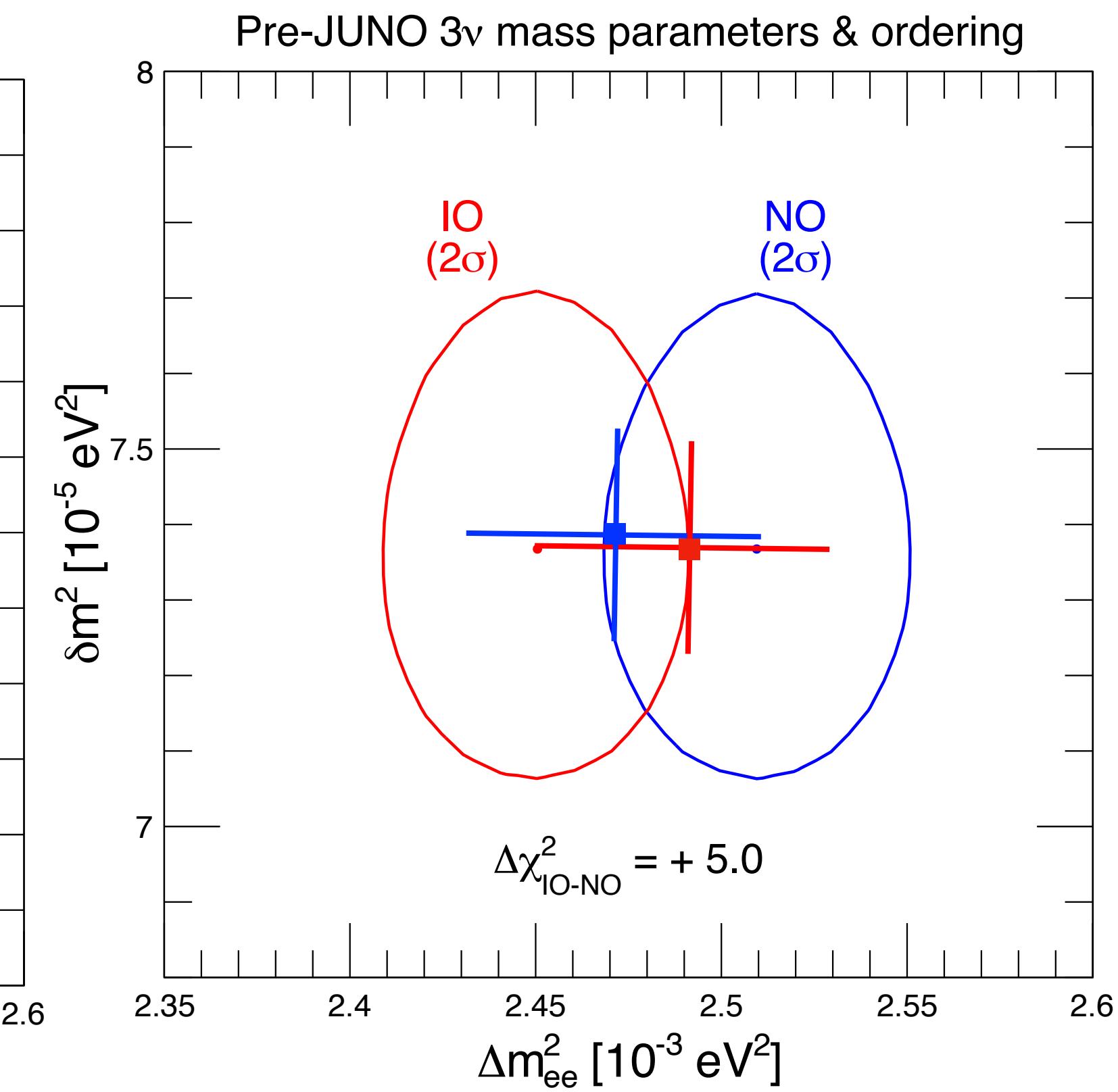
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Global analyses helpful to understand correlated impact on other parameters

It will be instructive to locate the first JUNO data in this plane and eventually compare them with JUNO-alone NO/IO findings for convergence.

Three observables $(m_\beta, m_{\beta\beta}, \Sigma)$ sensitive to the absolute ν masses

Three observables (m_β , $m_{\beta\beta}$, Σ) sensitive to the absolute ν masses

β decay experiments, sensitive to the “effective electron neutrino mass”

$$m_\beta = [c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2]^{1/2}$$

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$$\Sigma = m_1 + m_2 + m_3$$

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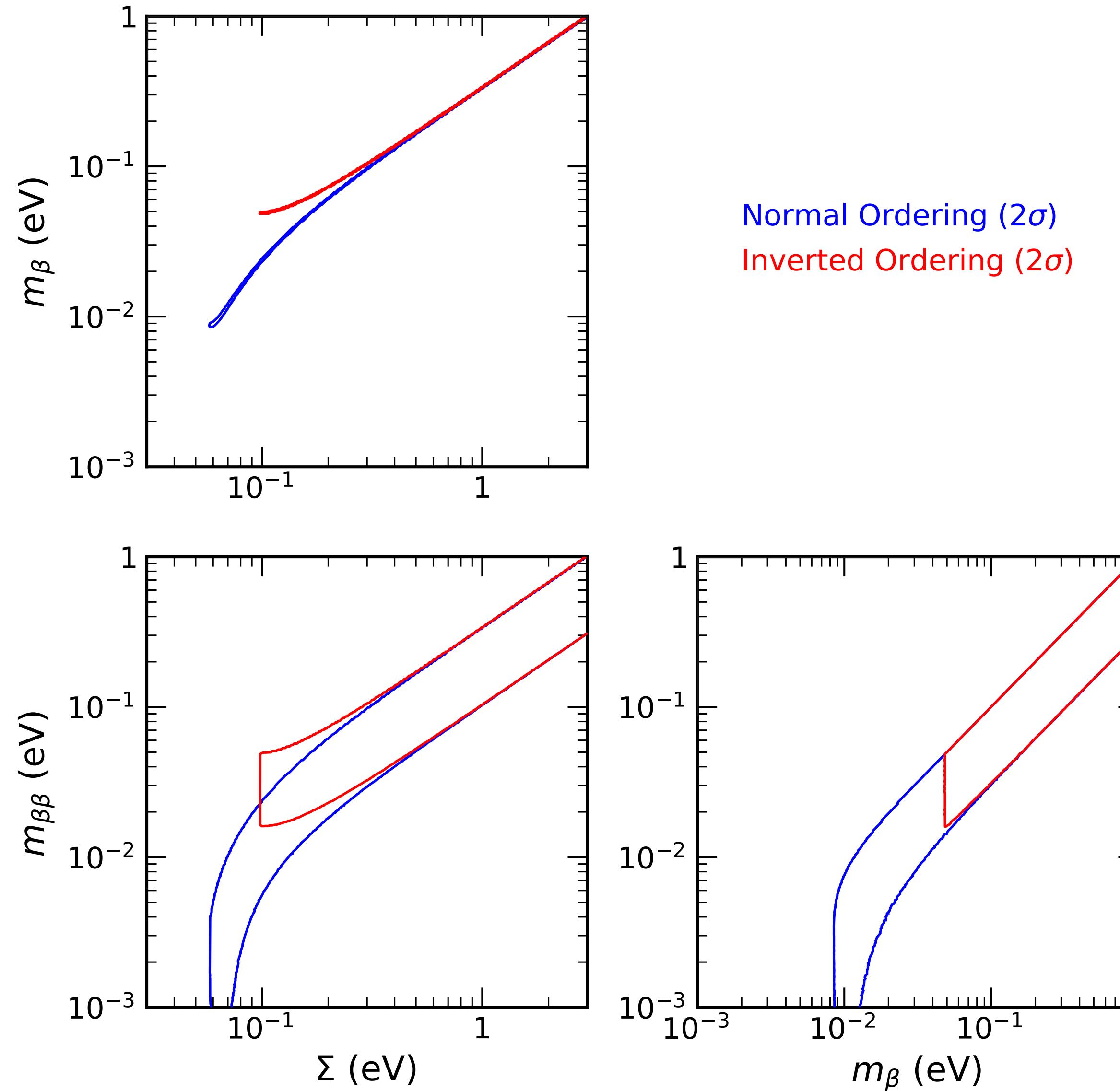
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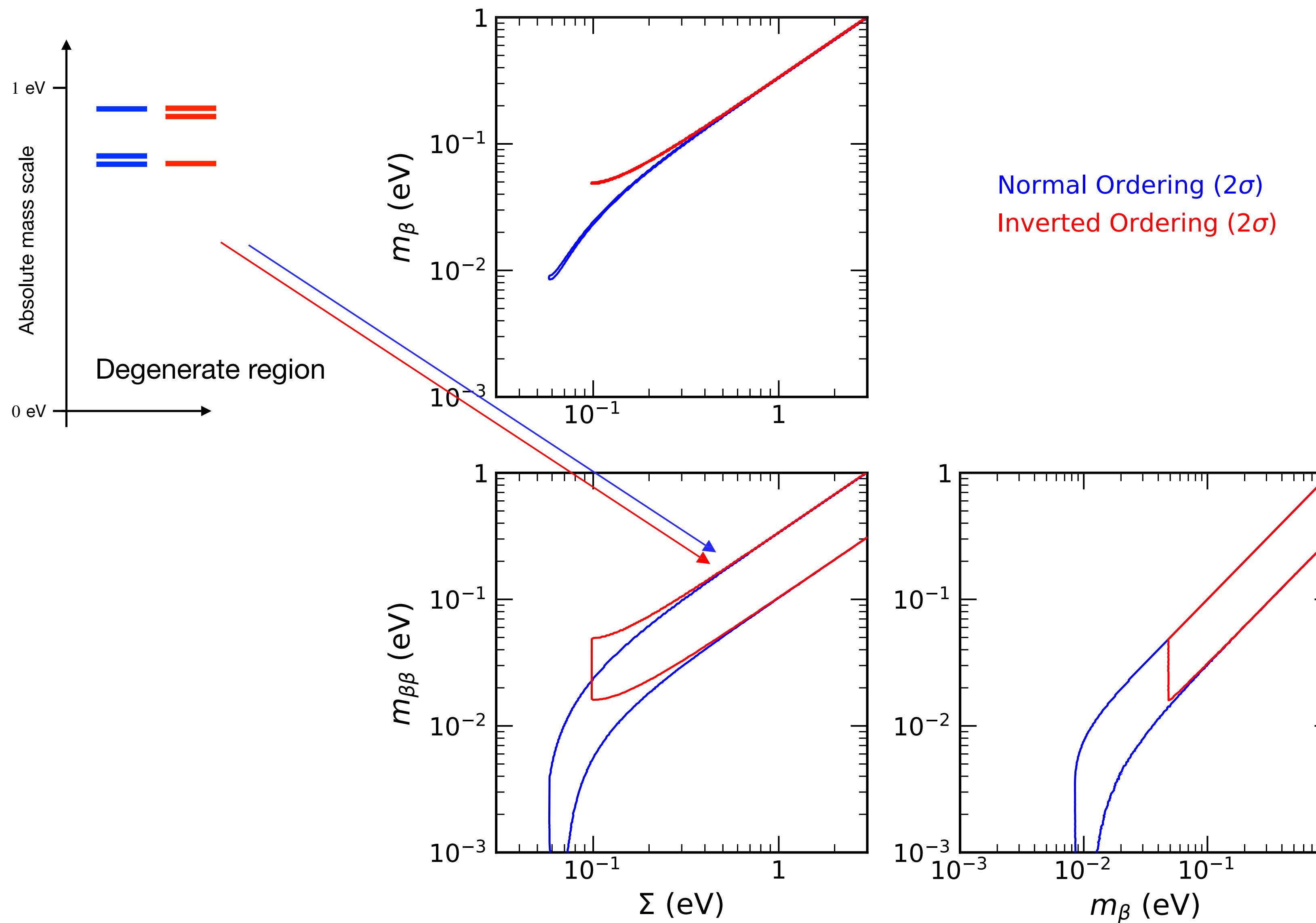
The three observables are correlated by oscillation data →

Regions allowed by oscillations on $(\Sigma, m_\beta, m_{\beta\beta})$

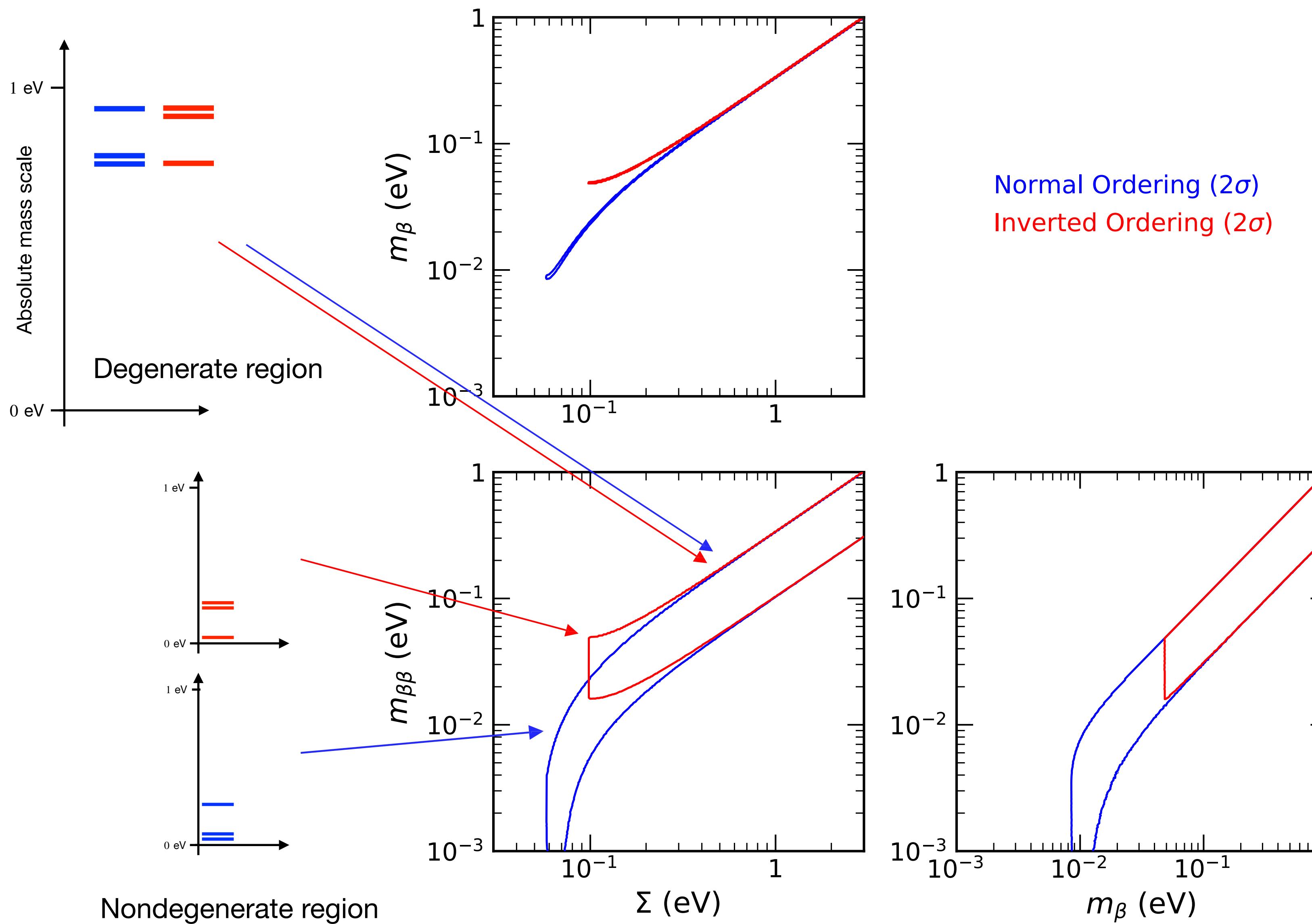
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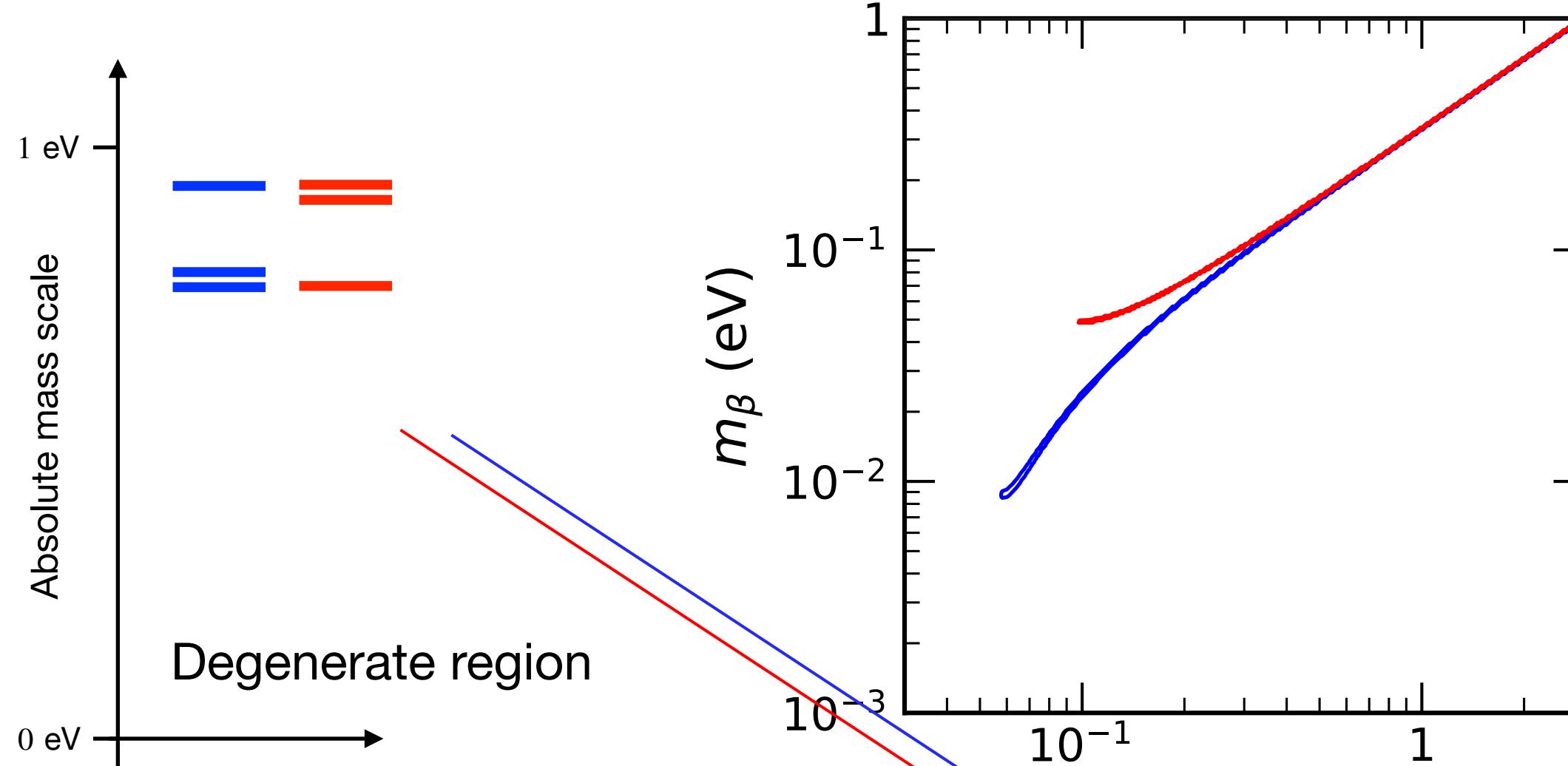
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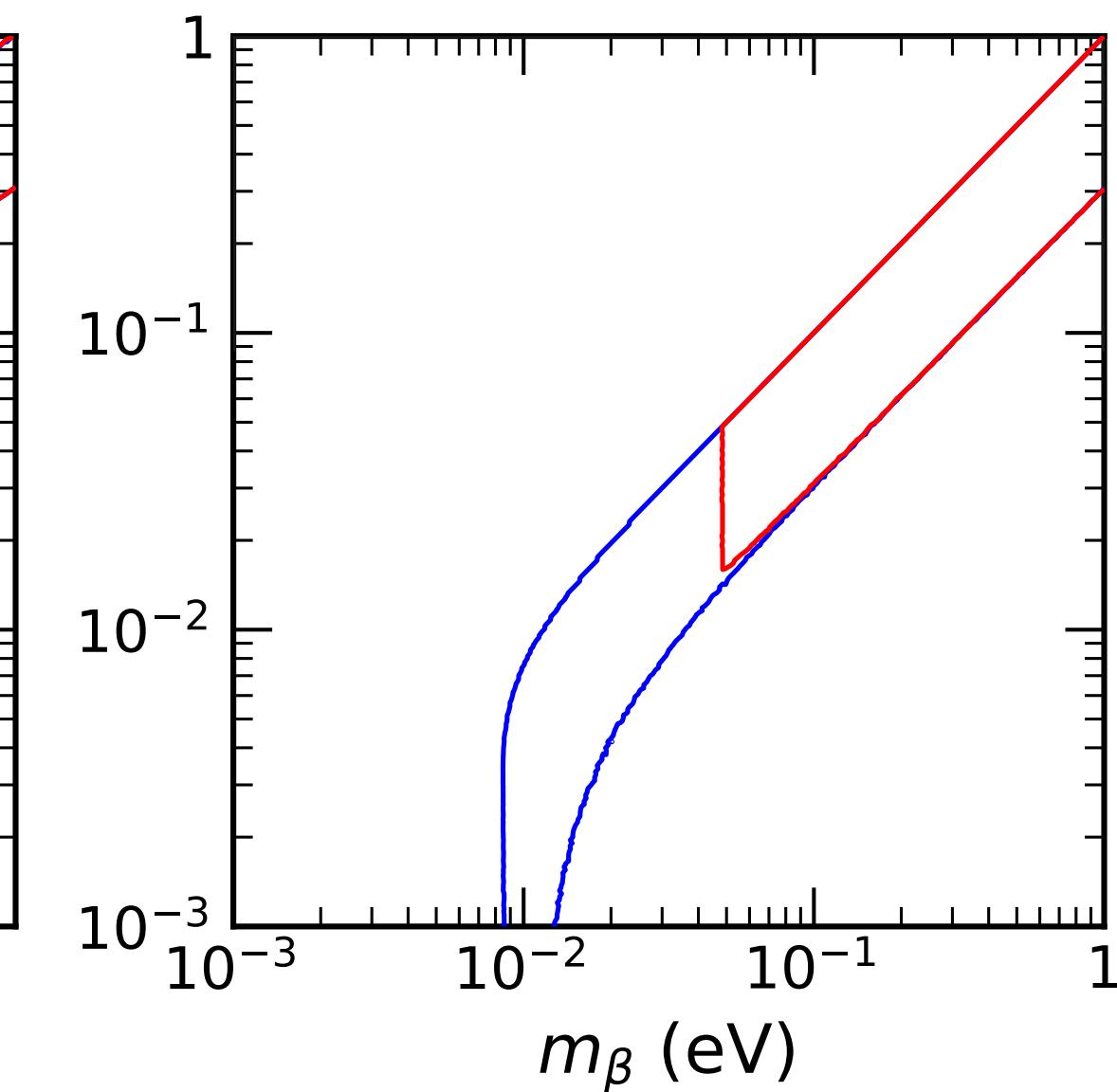
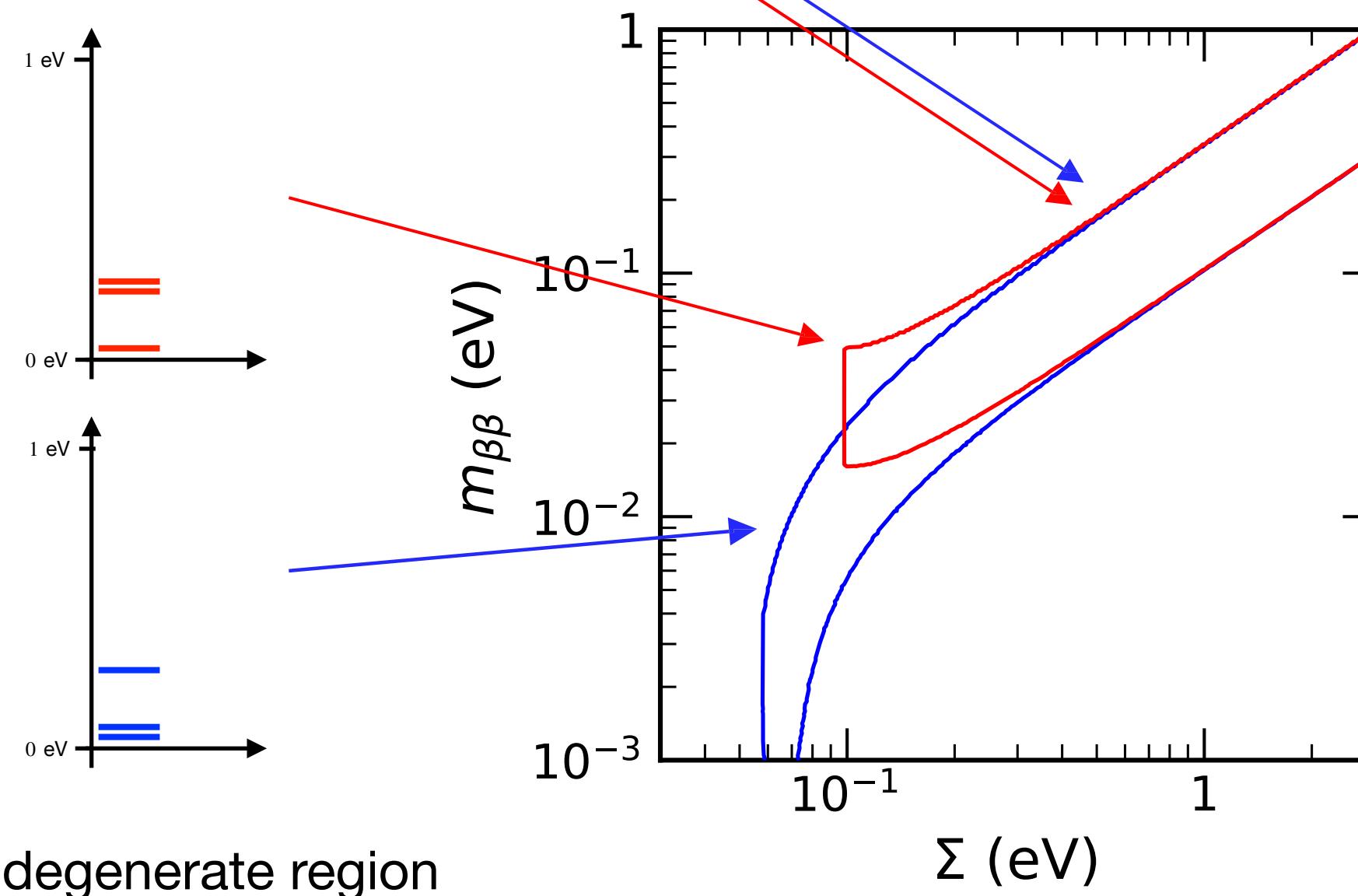
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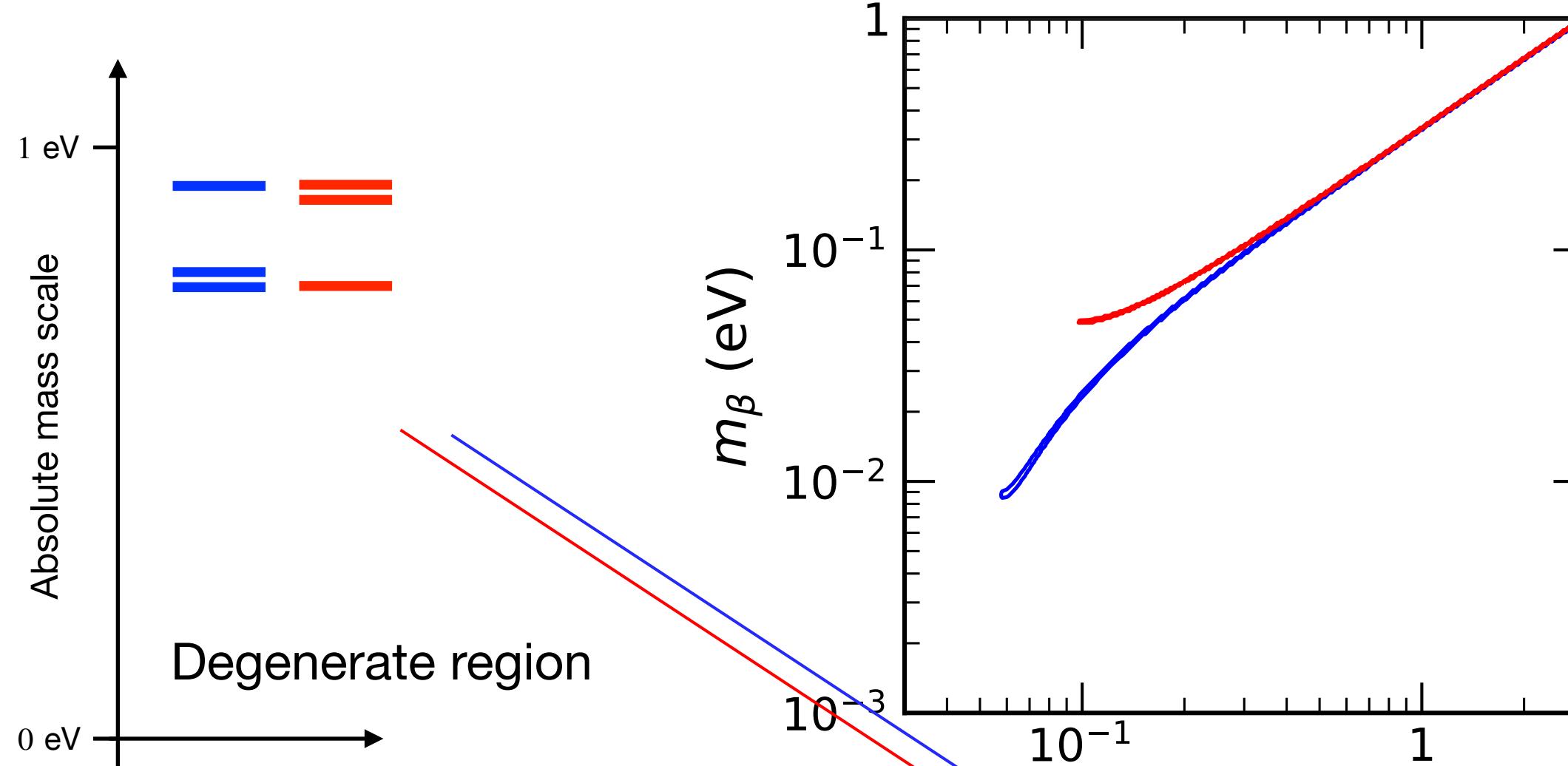
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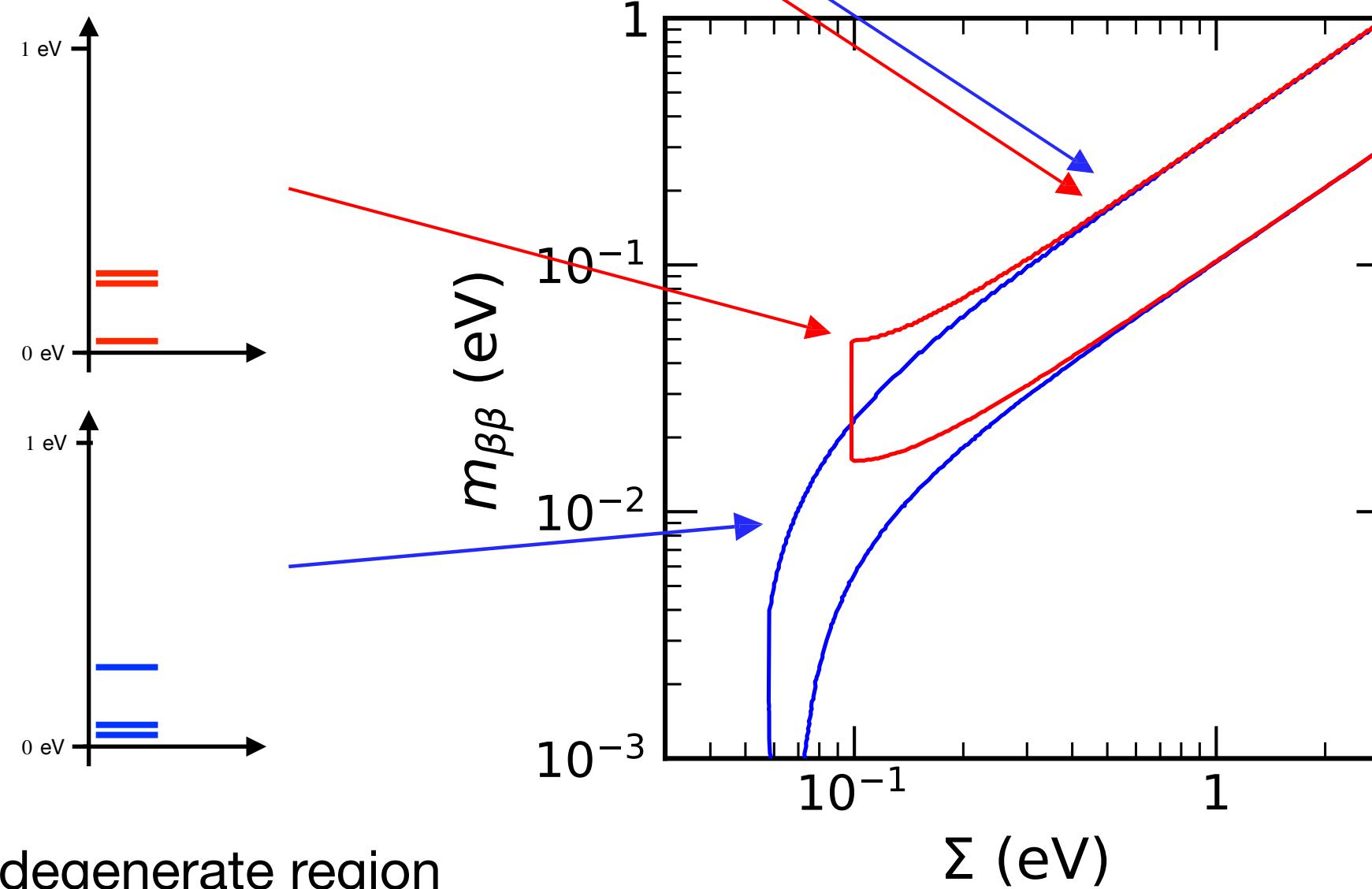
Normal Ordering (2σ)
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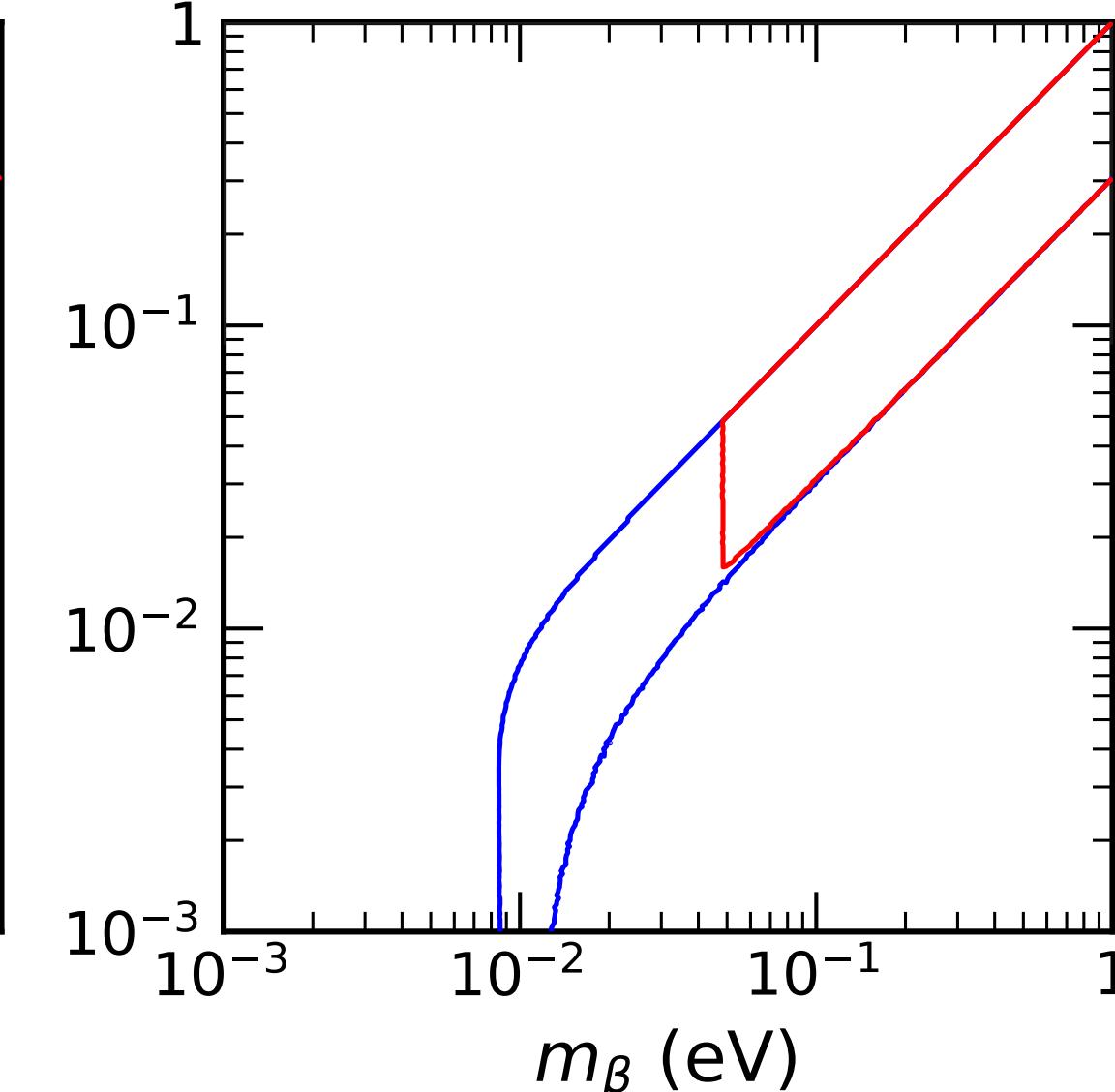


Degenerate region



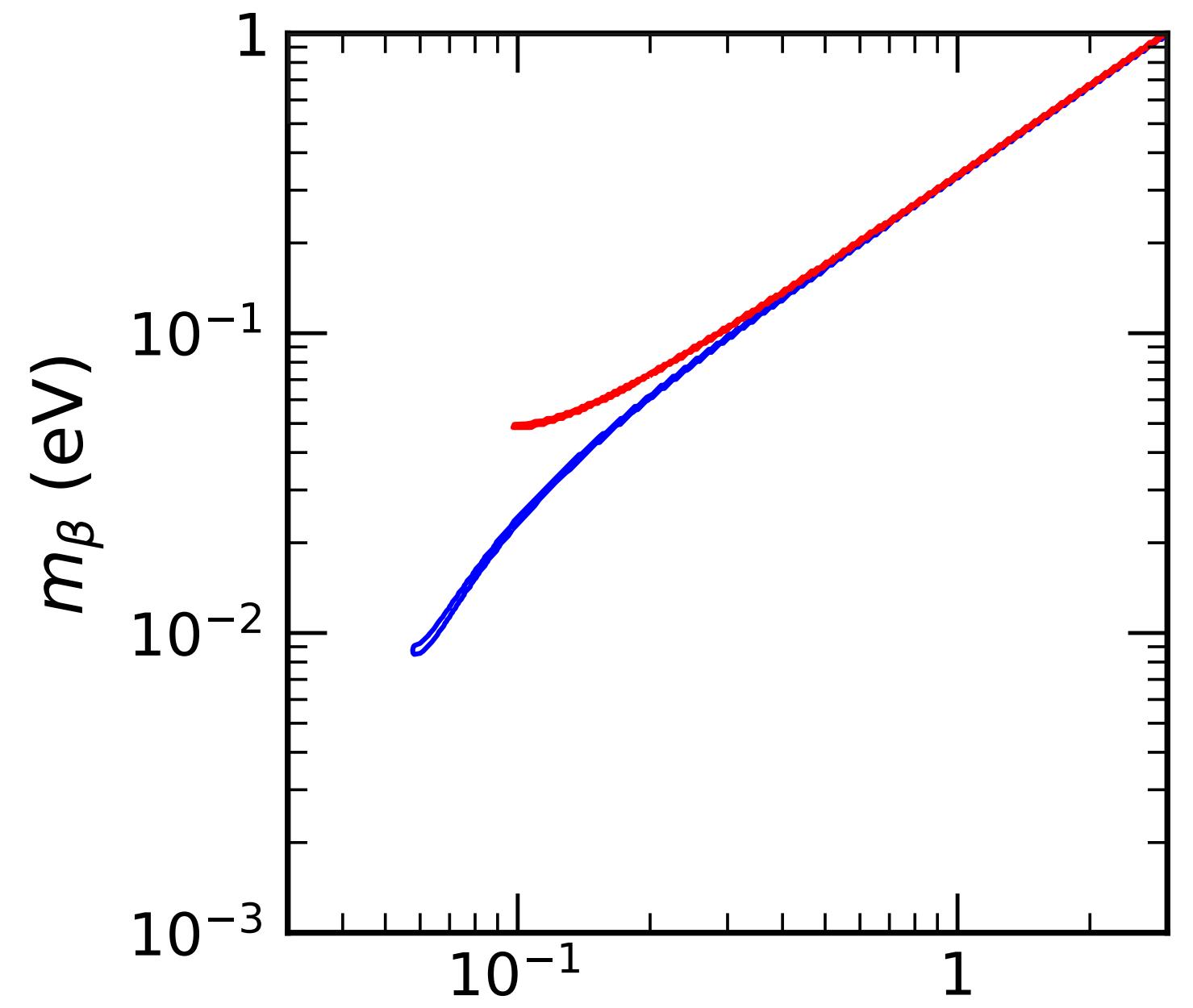
Nondegenerate region

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Inverted Ordering (2 σ)

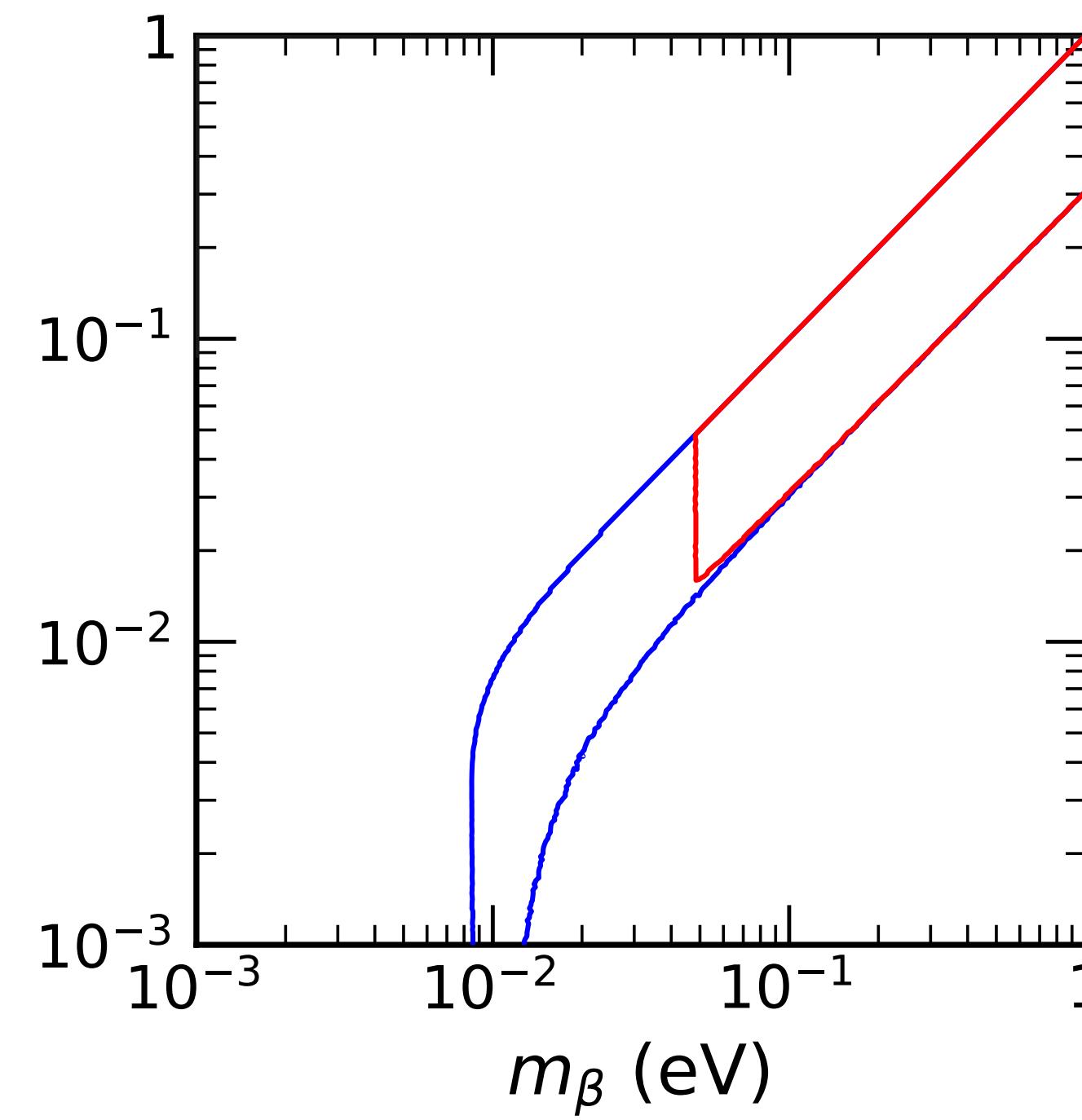
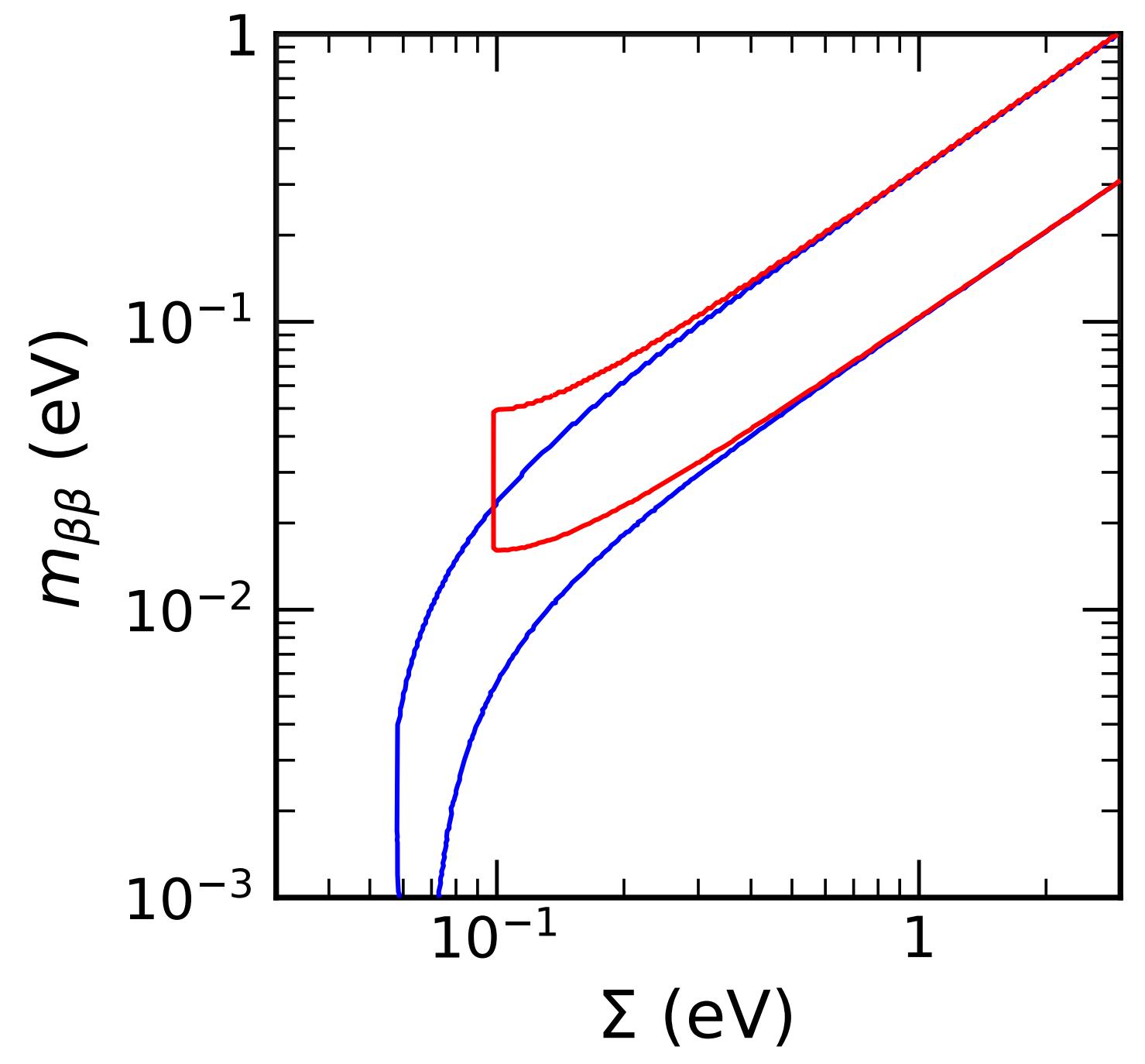


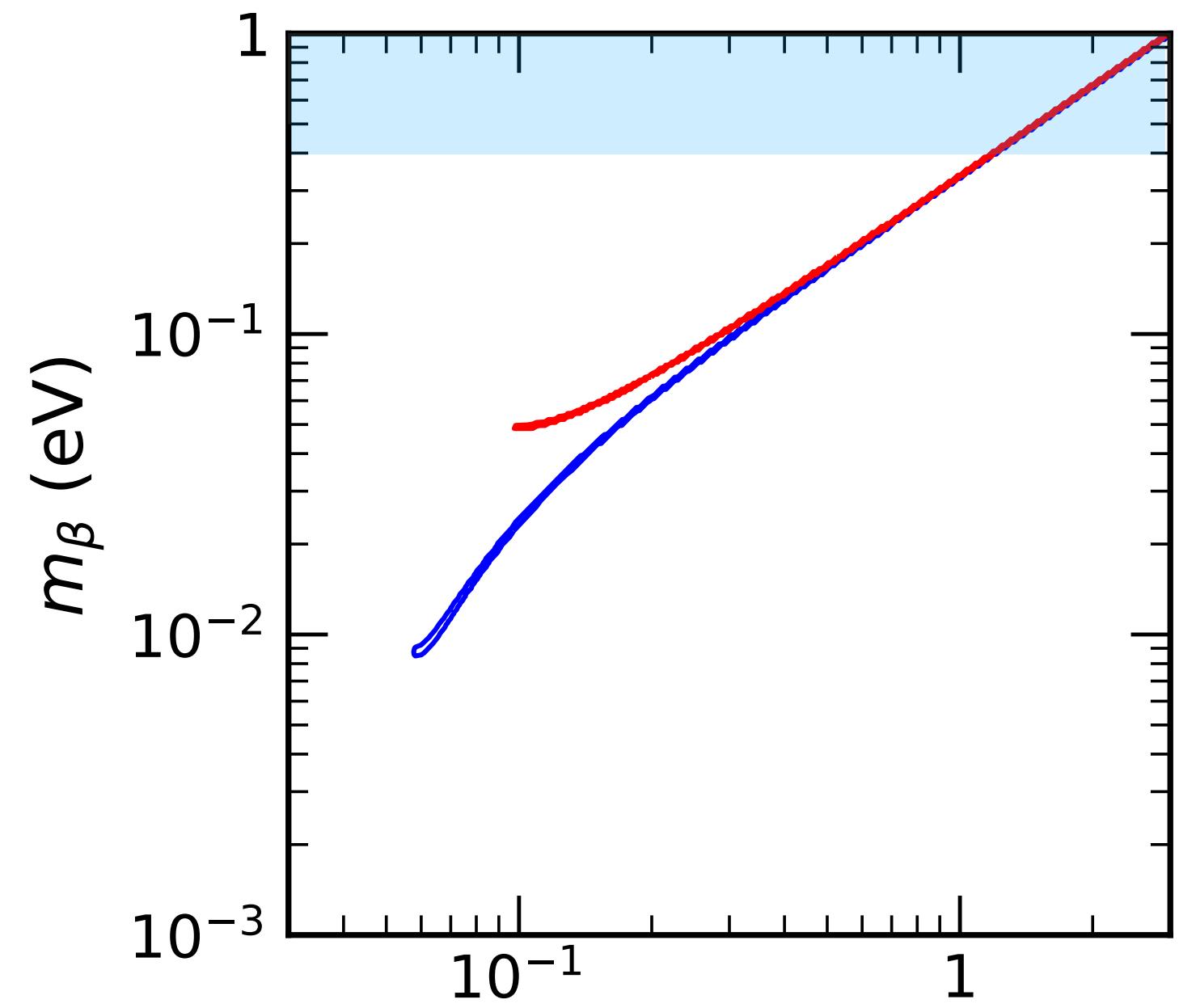
Spread dependent on
the Majorana phases

In principle can be
measured if NME under
control

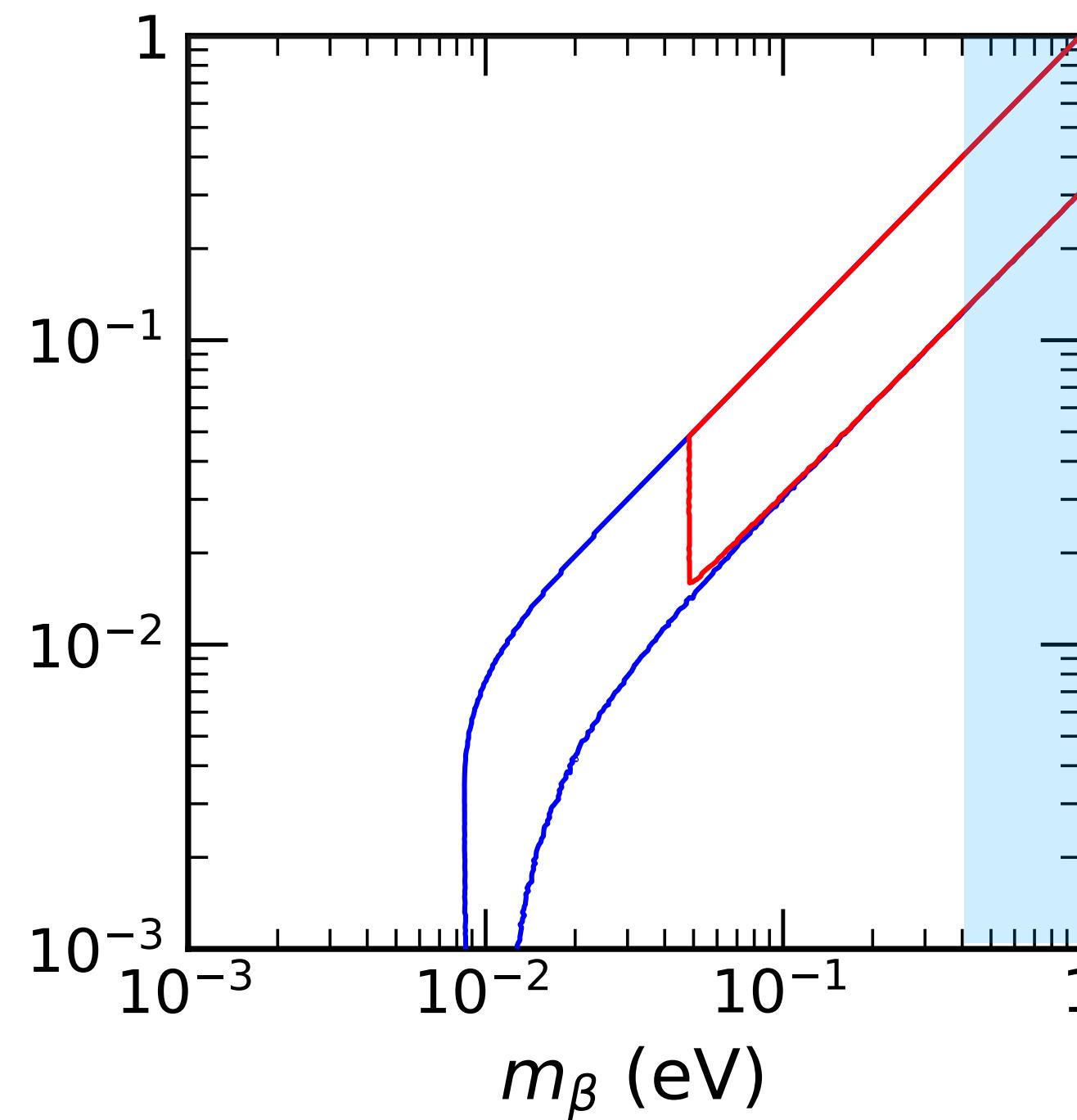
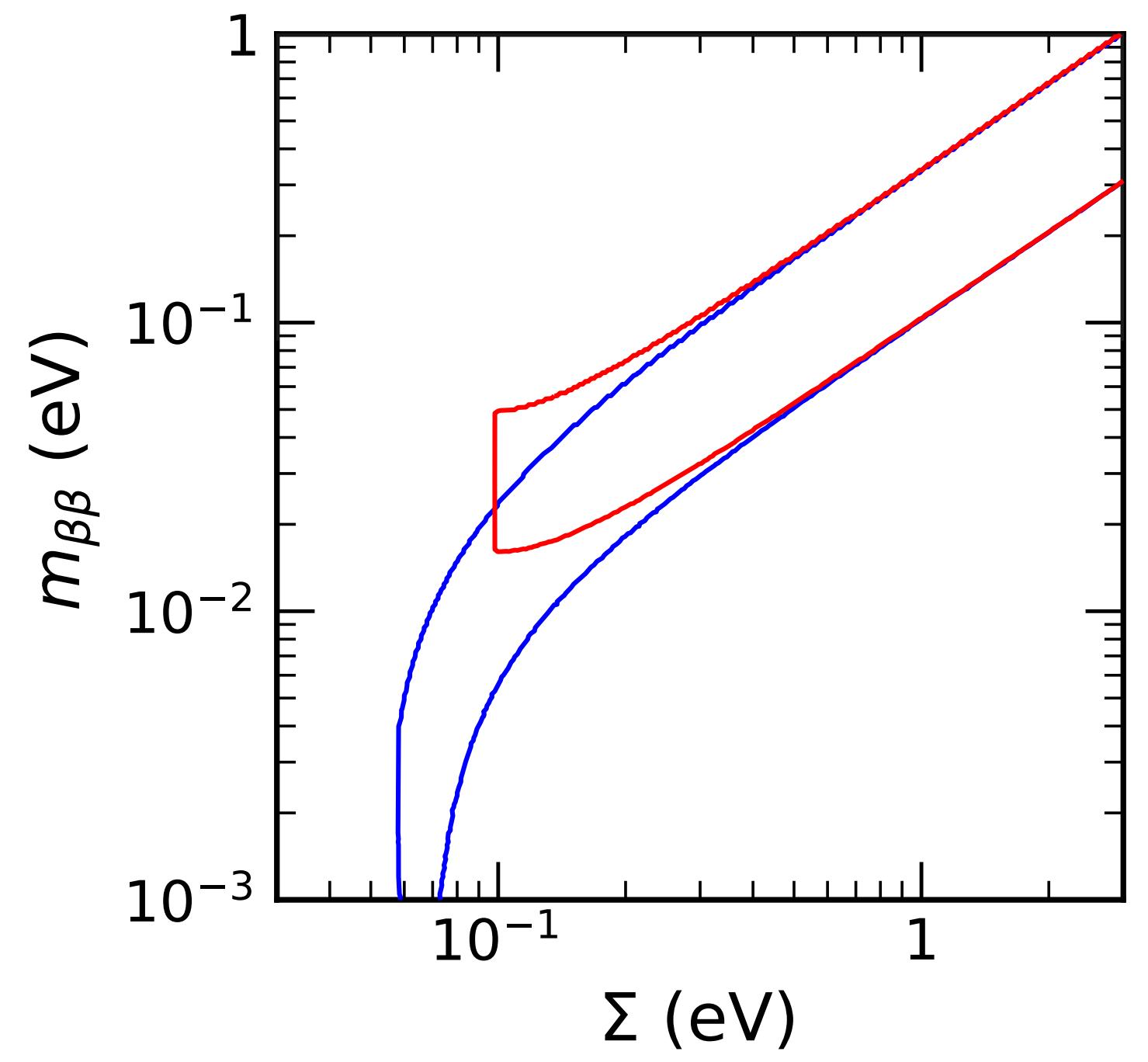


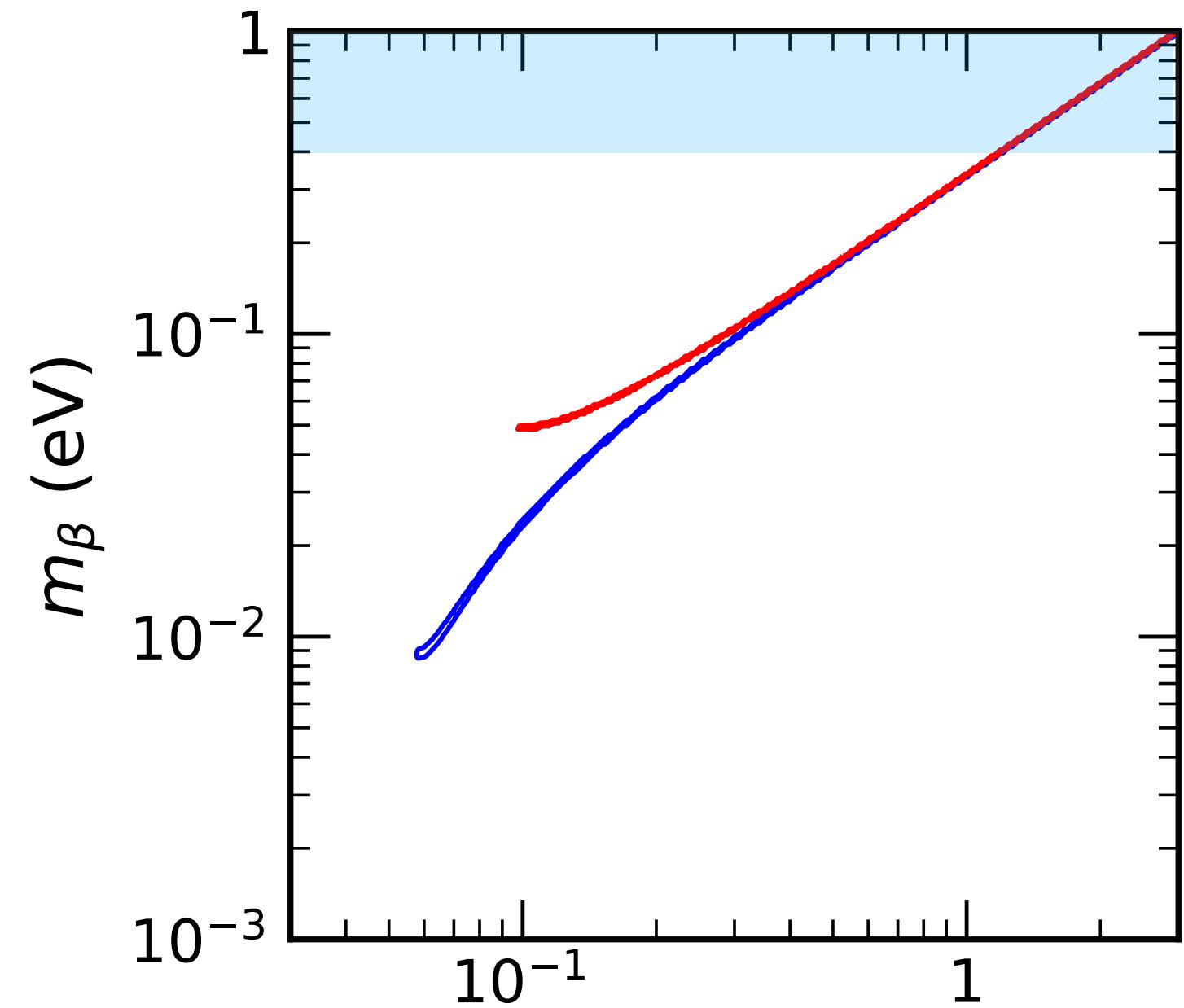
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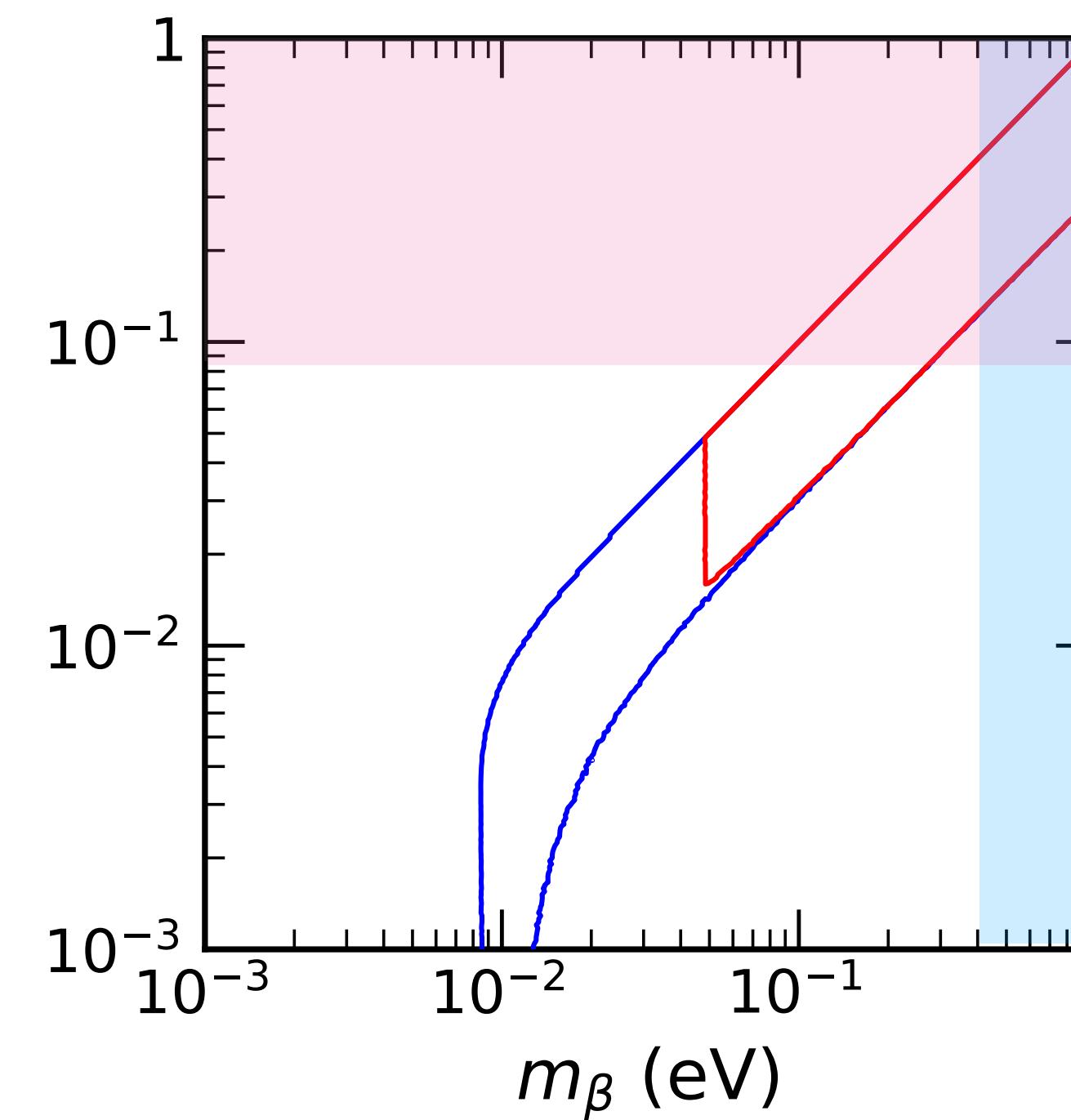
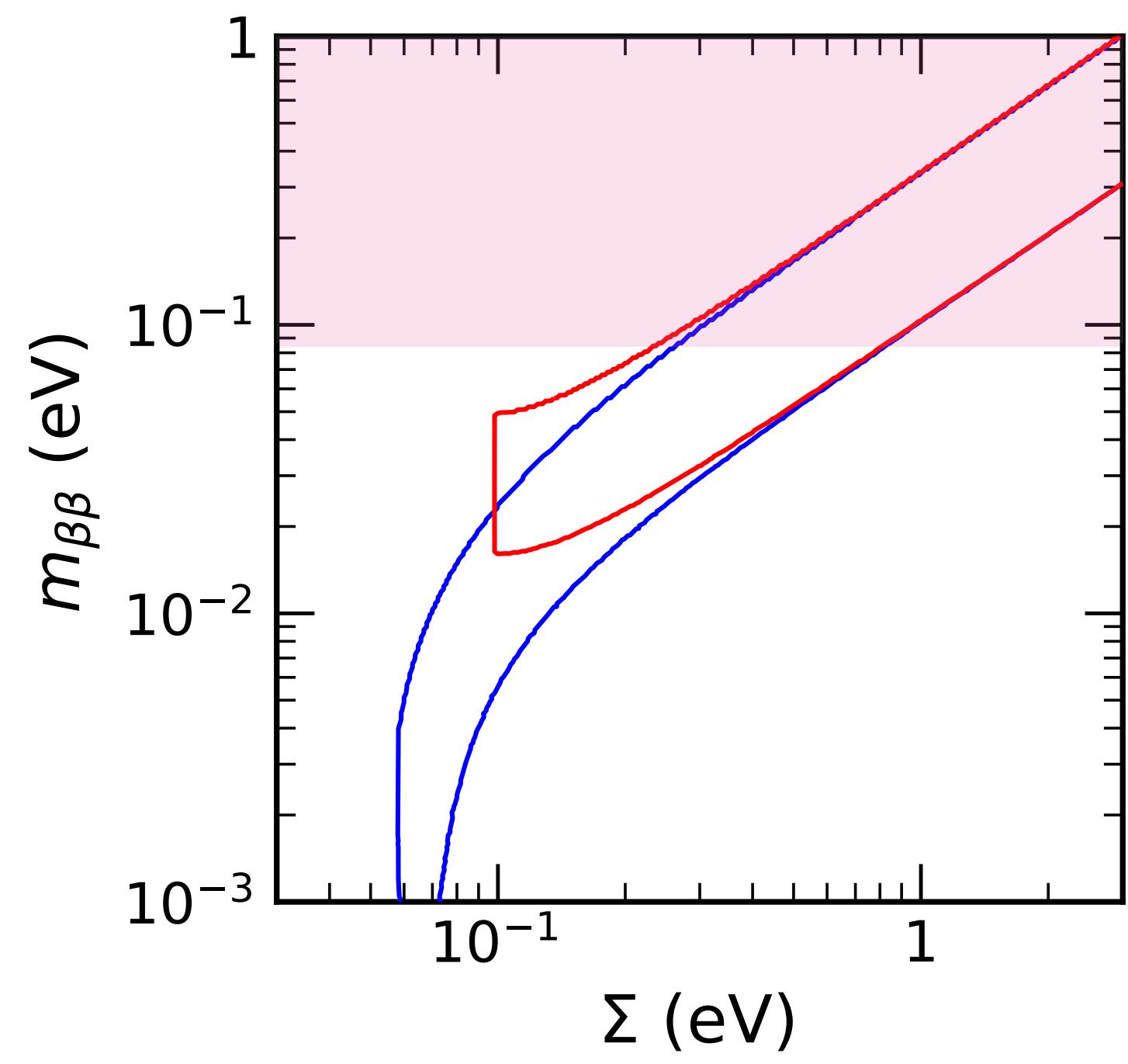
β decay - KATRIN



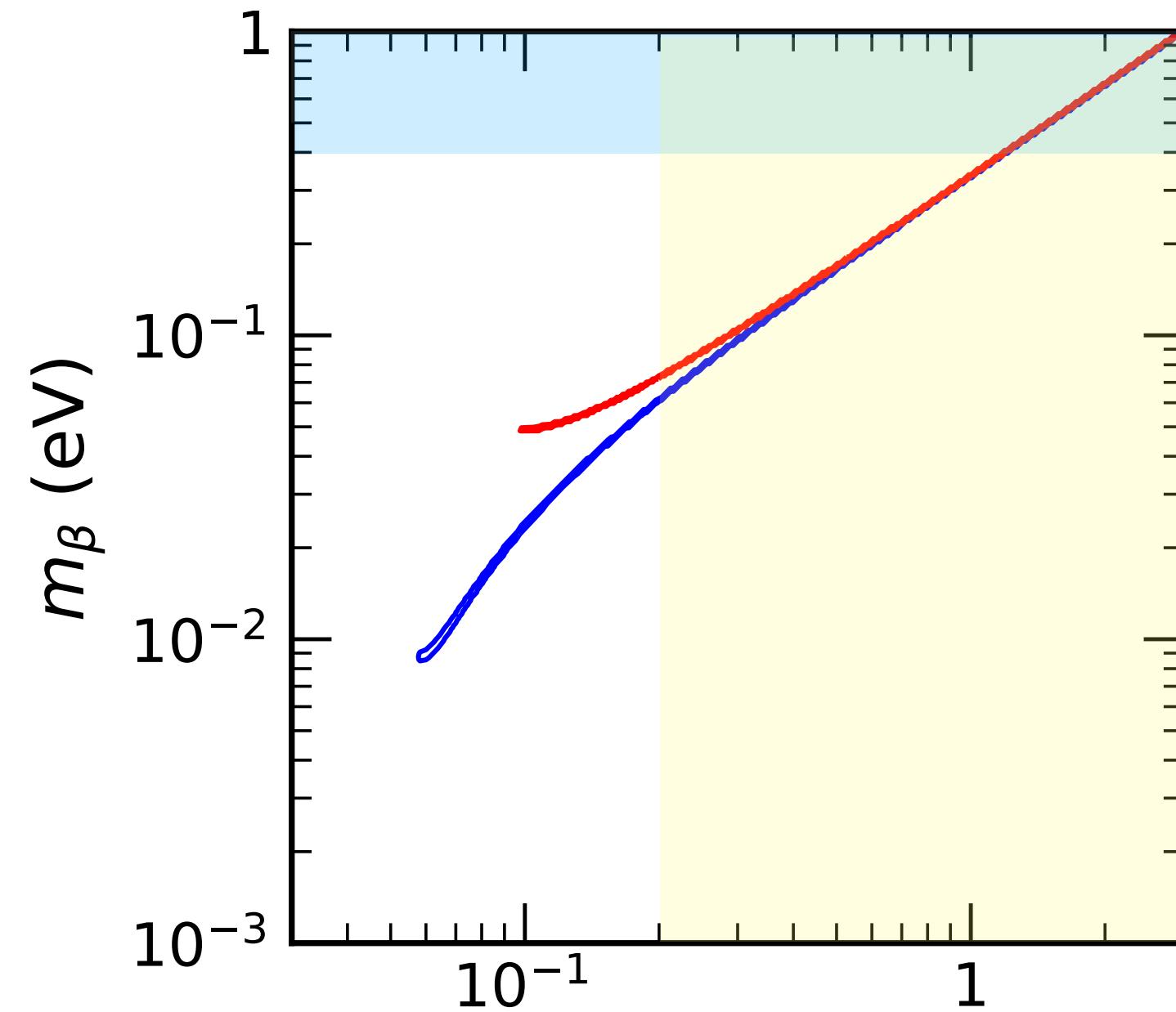


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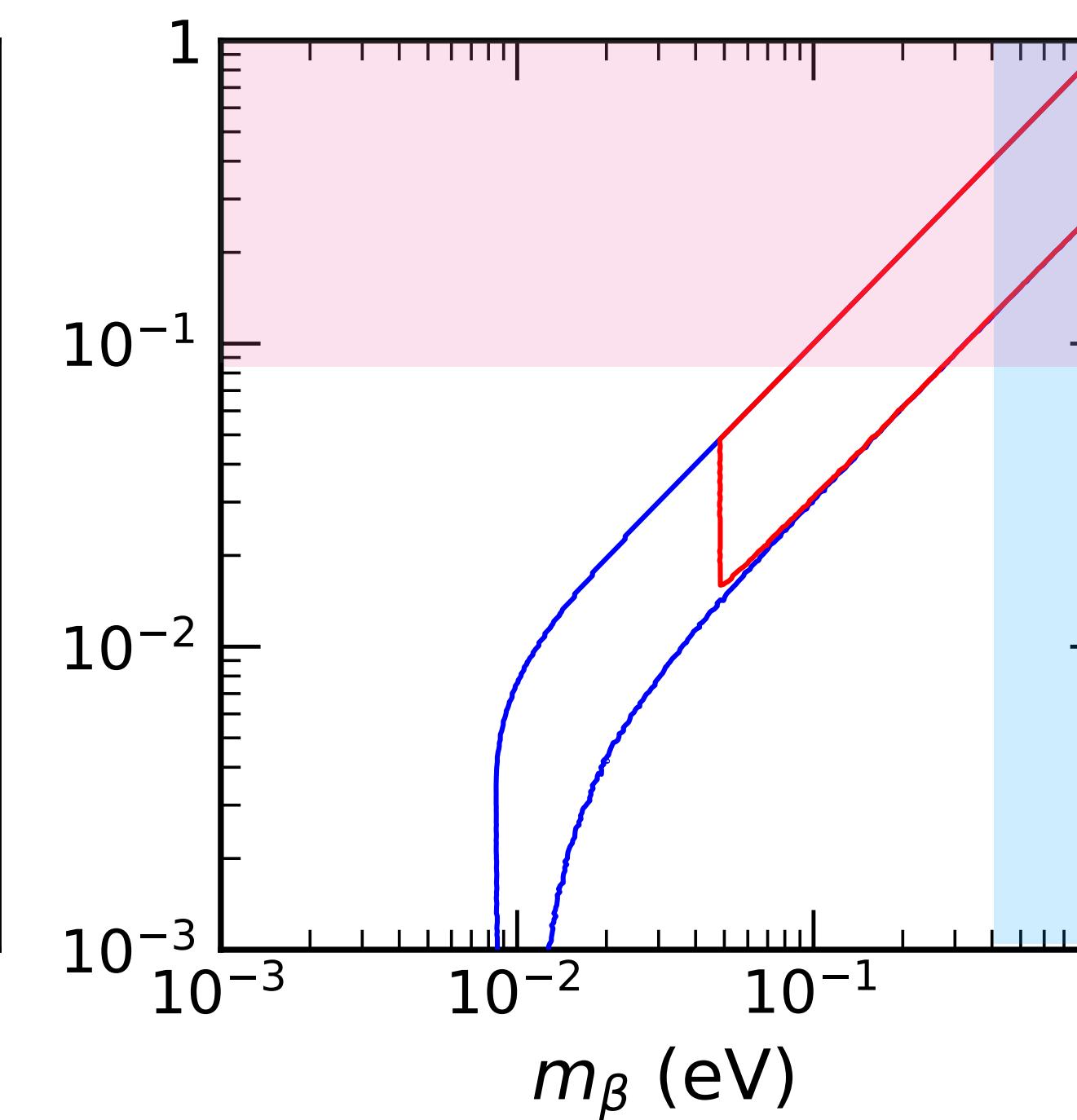
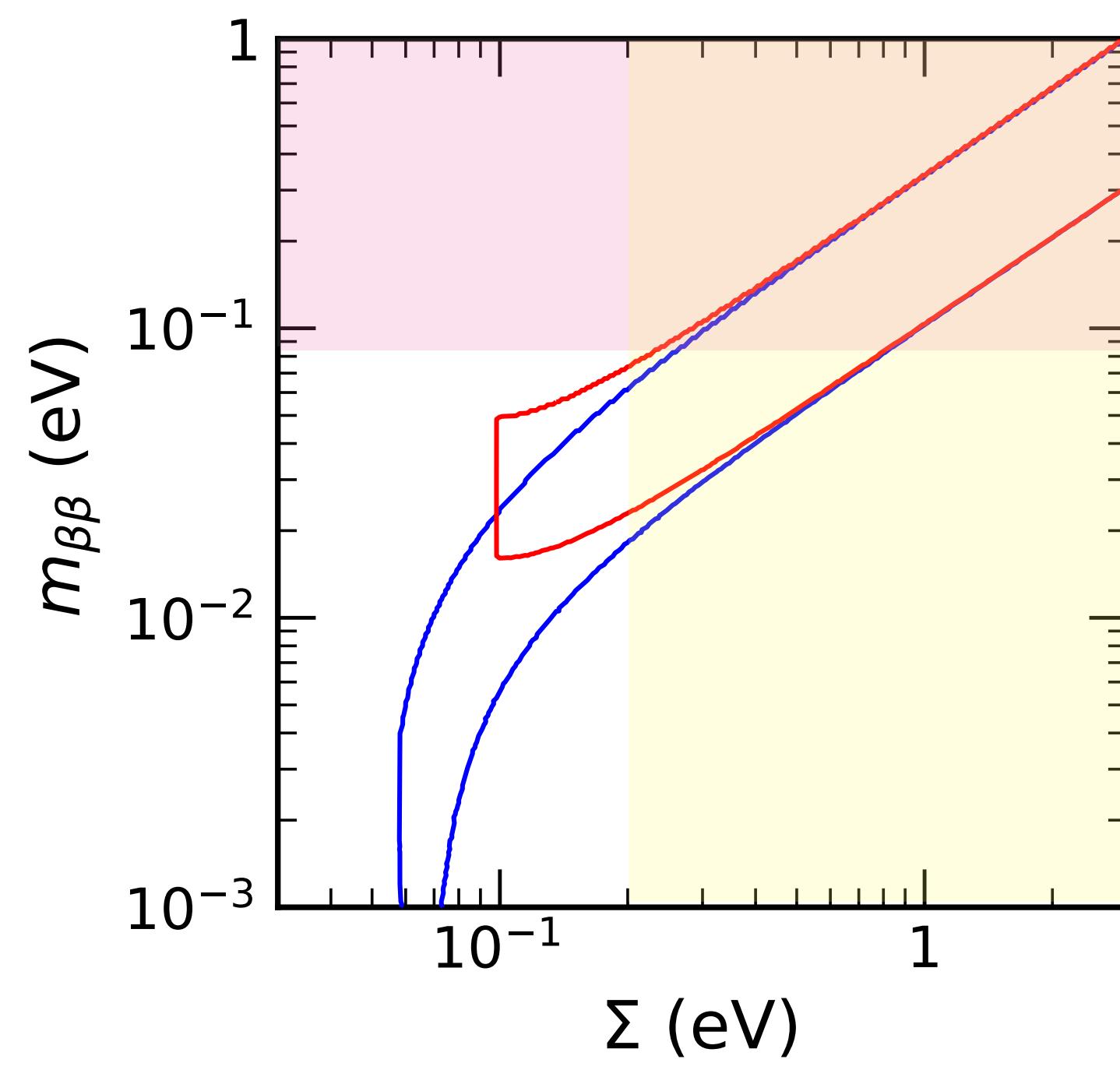


$0\nu\beta\beta$ decay
KamLAND-Zen, EXO, CUORE, GERDA



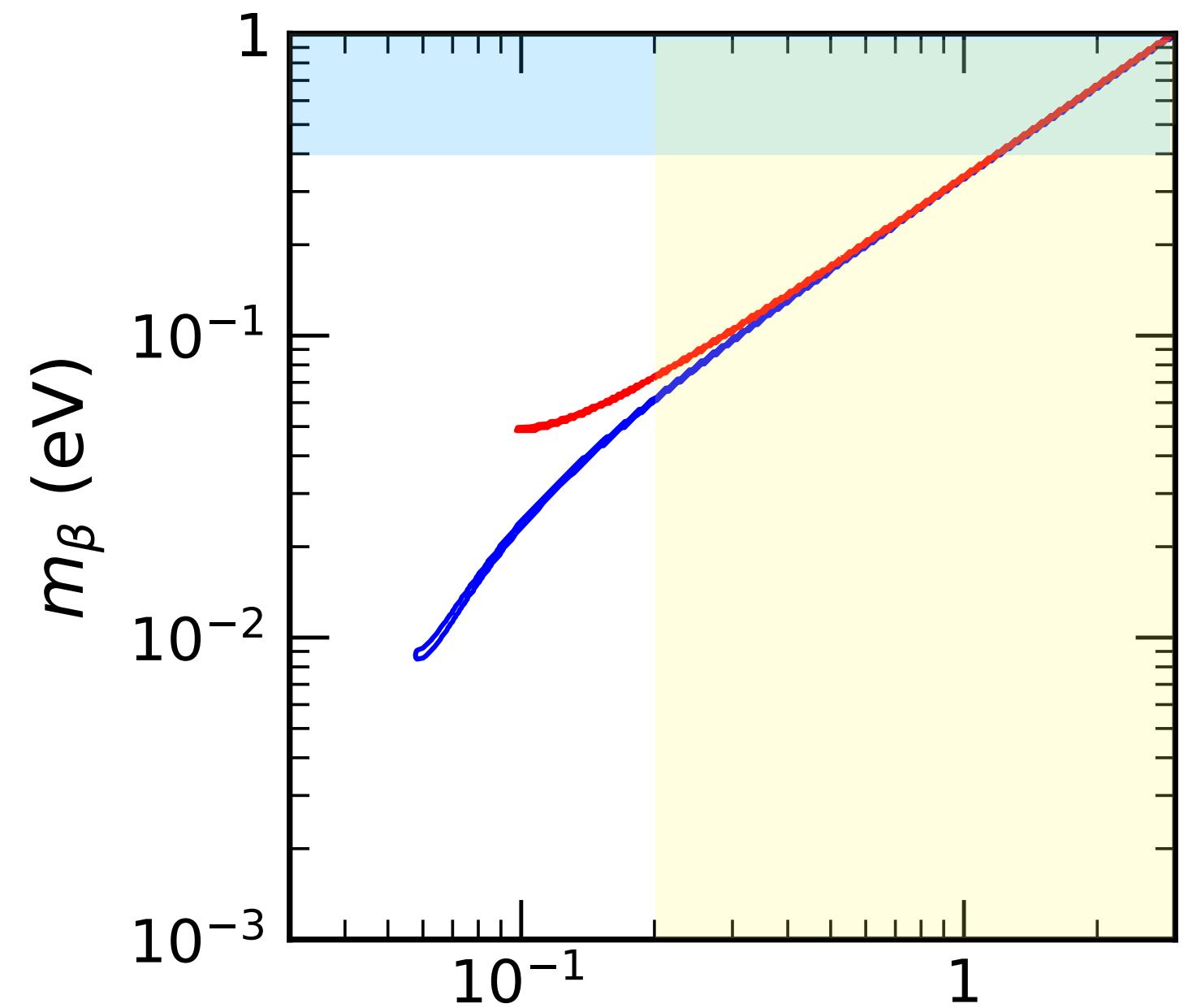
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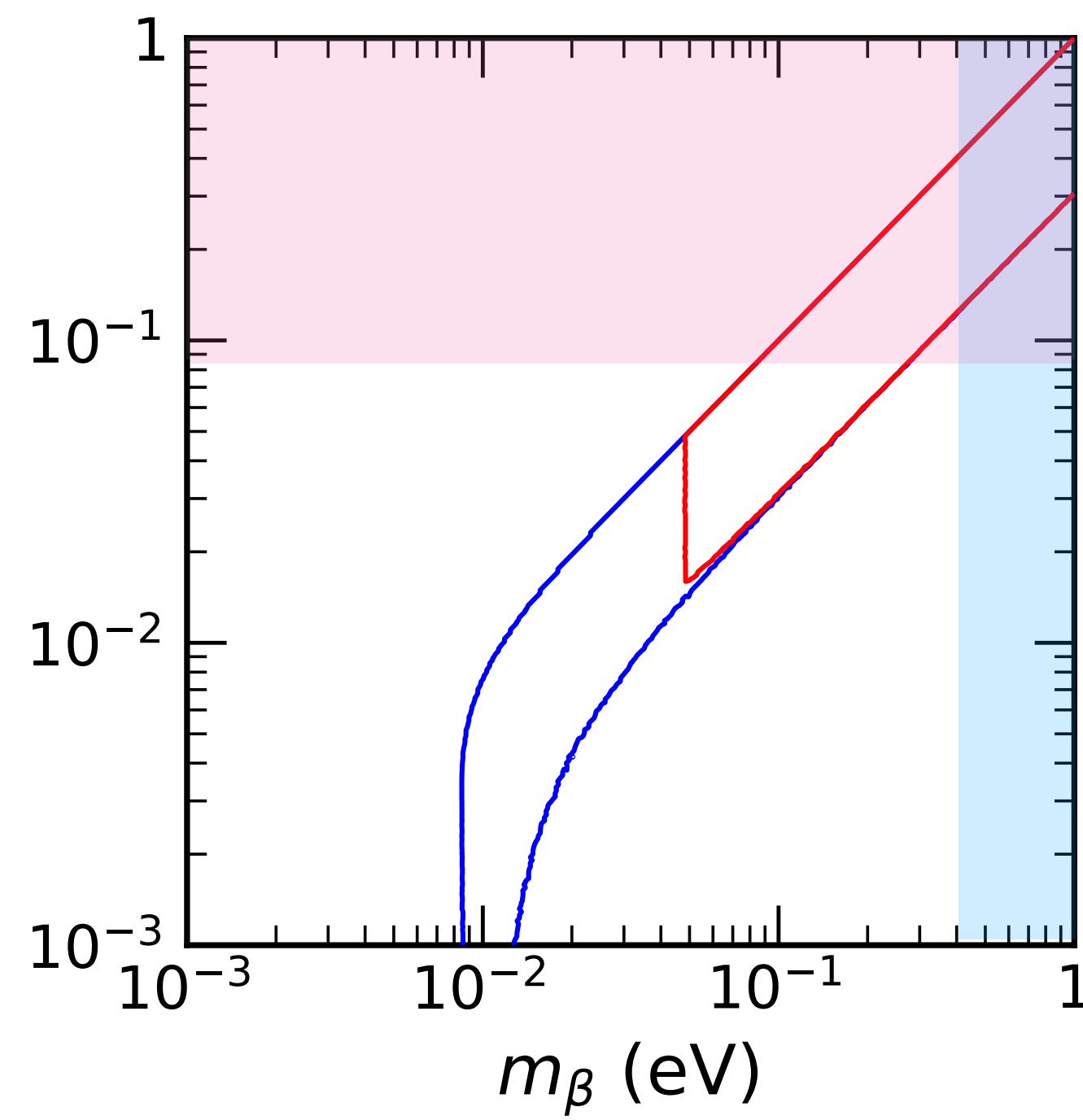
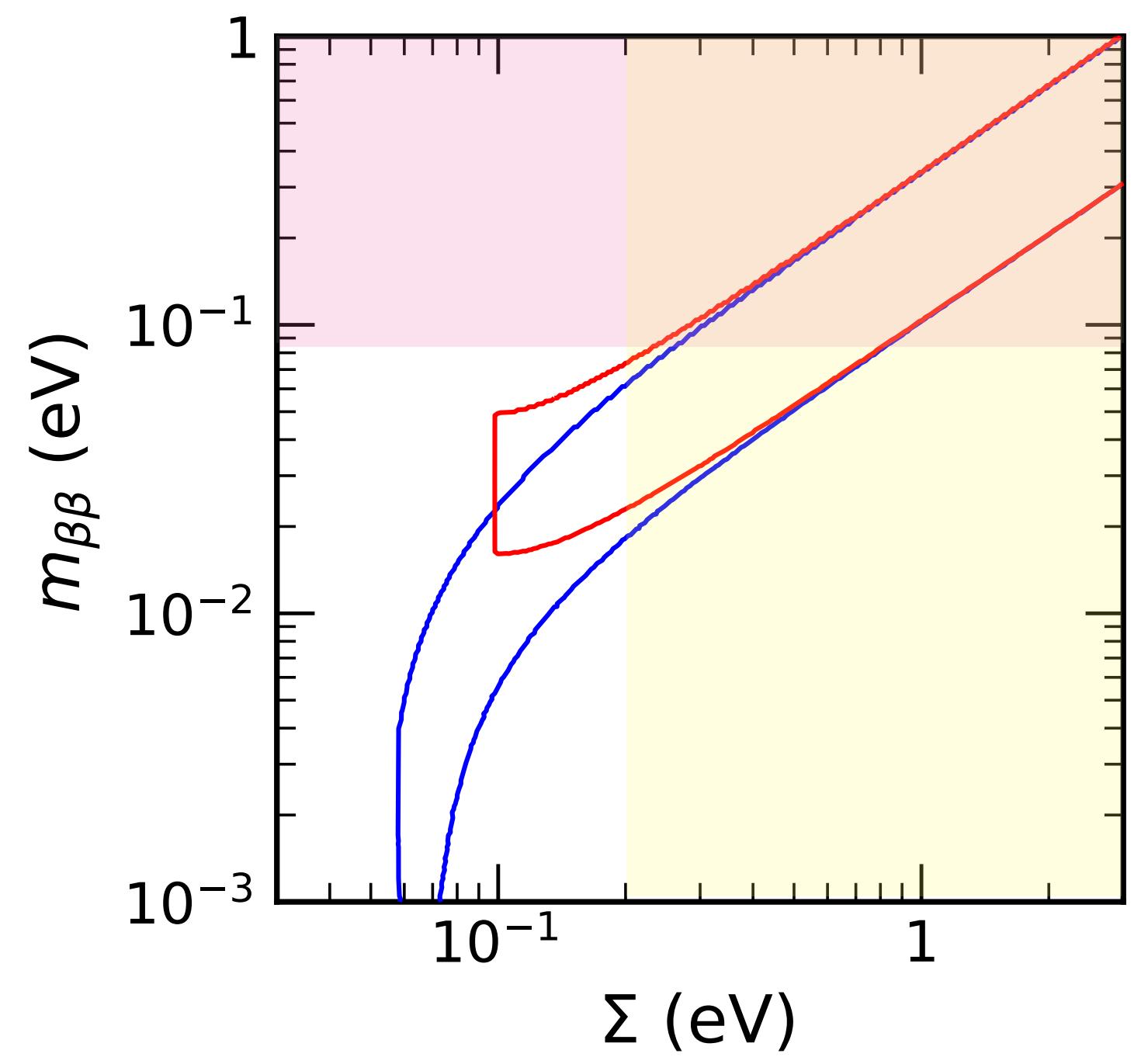


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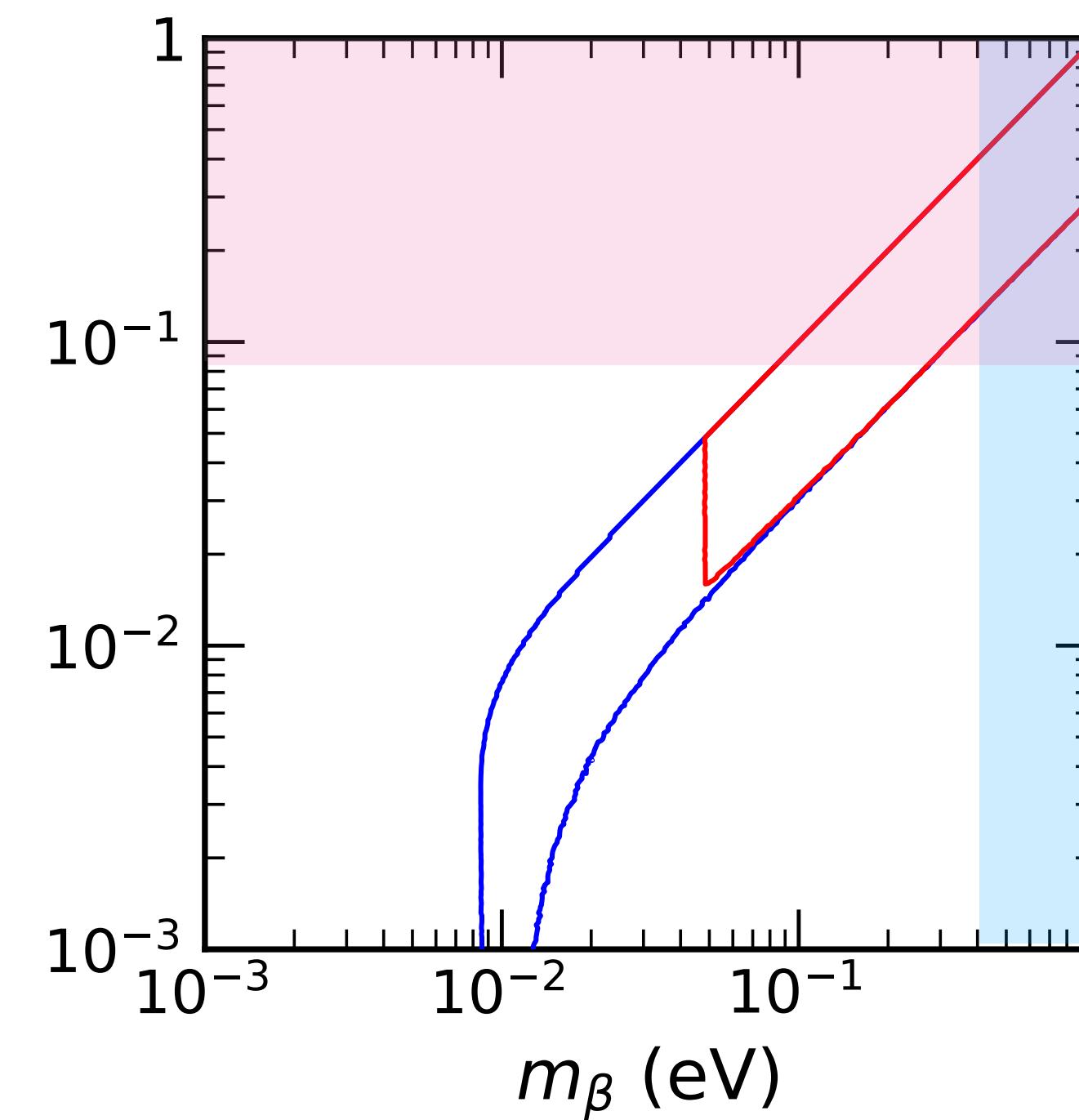
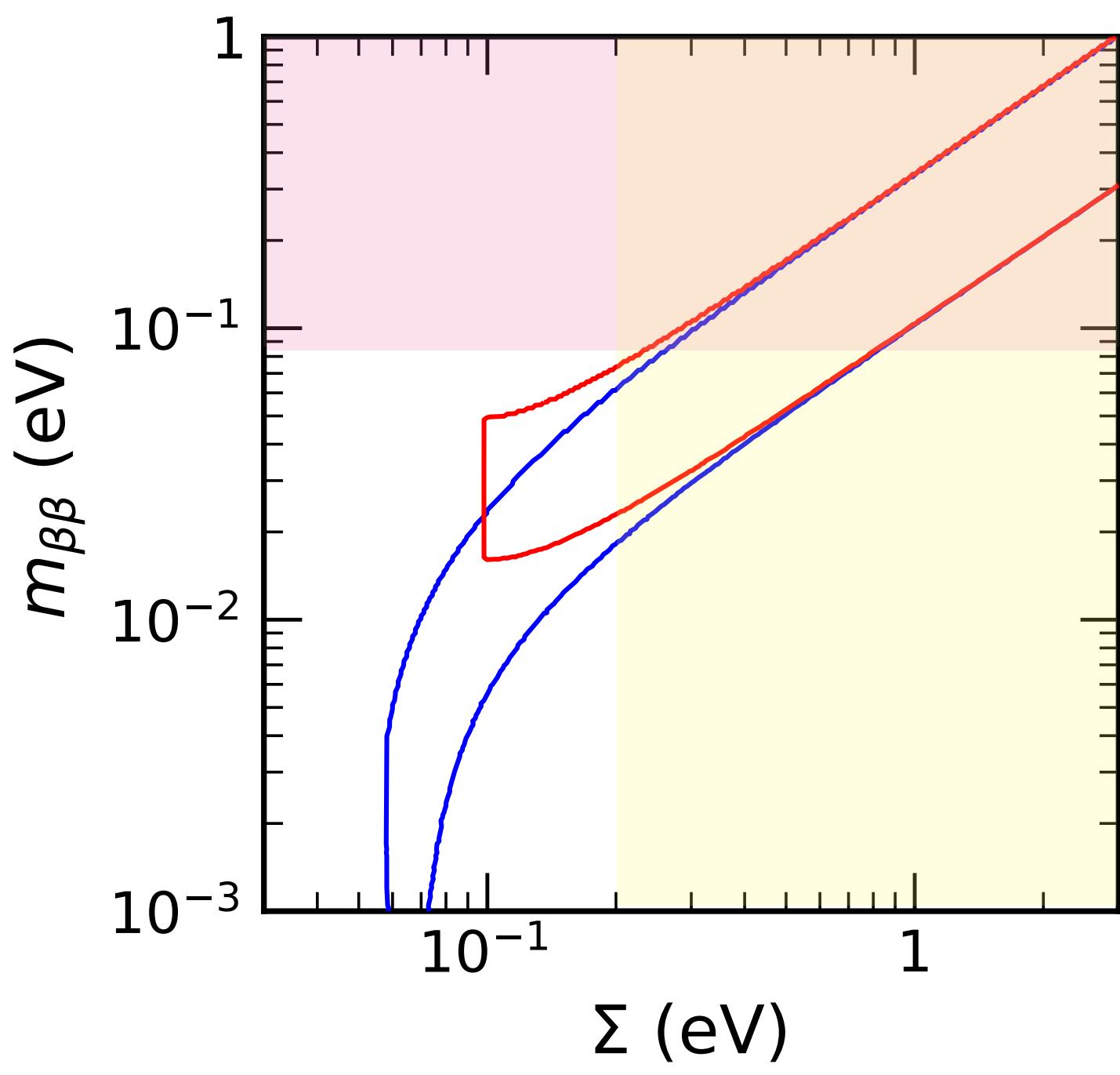
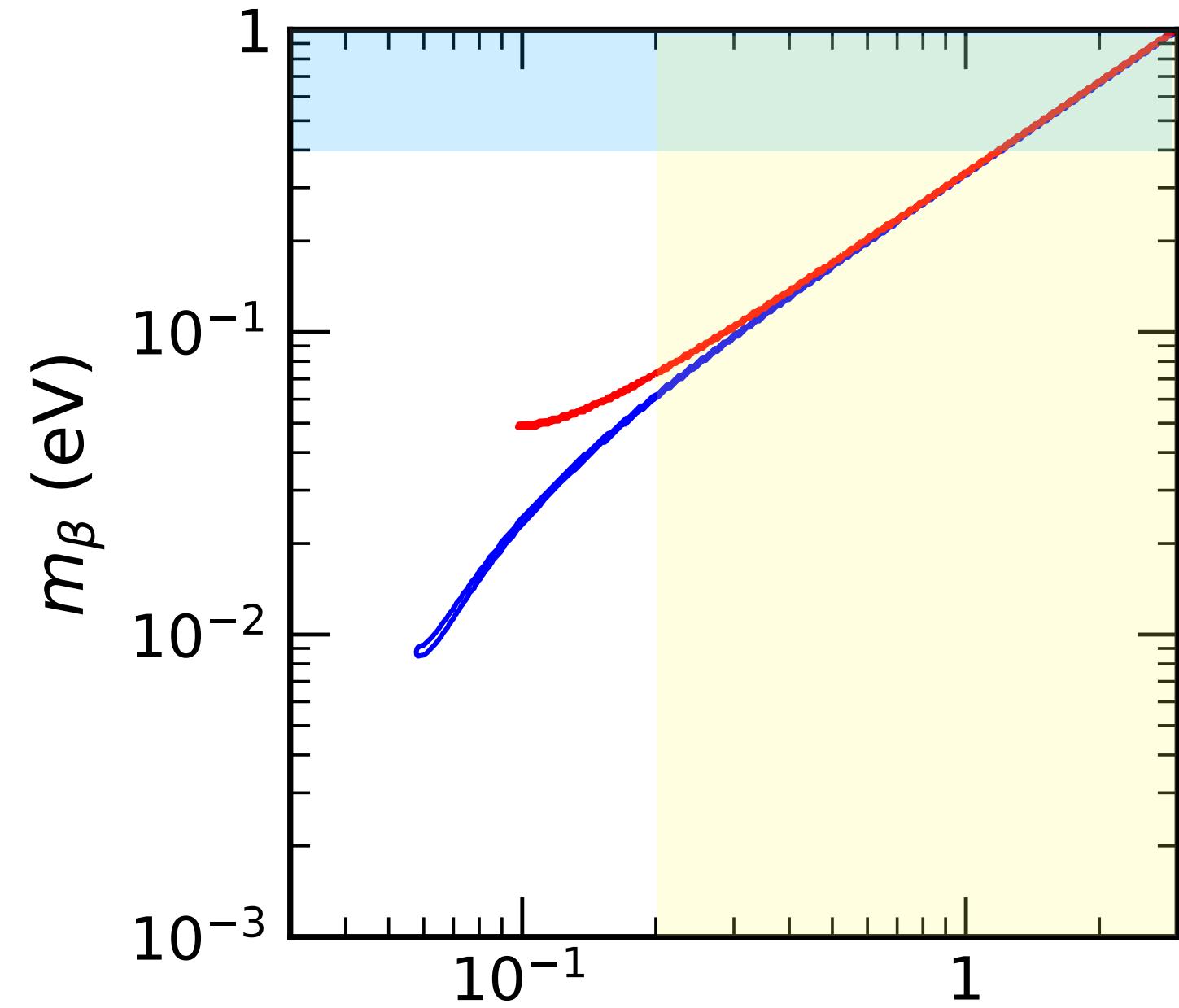
Astrophysics and Cosmology
CMB, BAO, lensing, ...



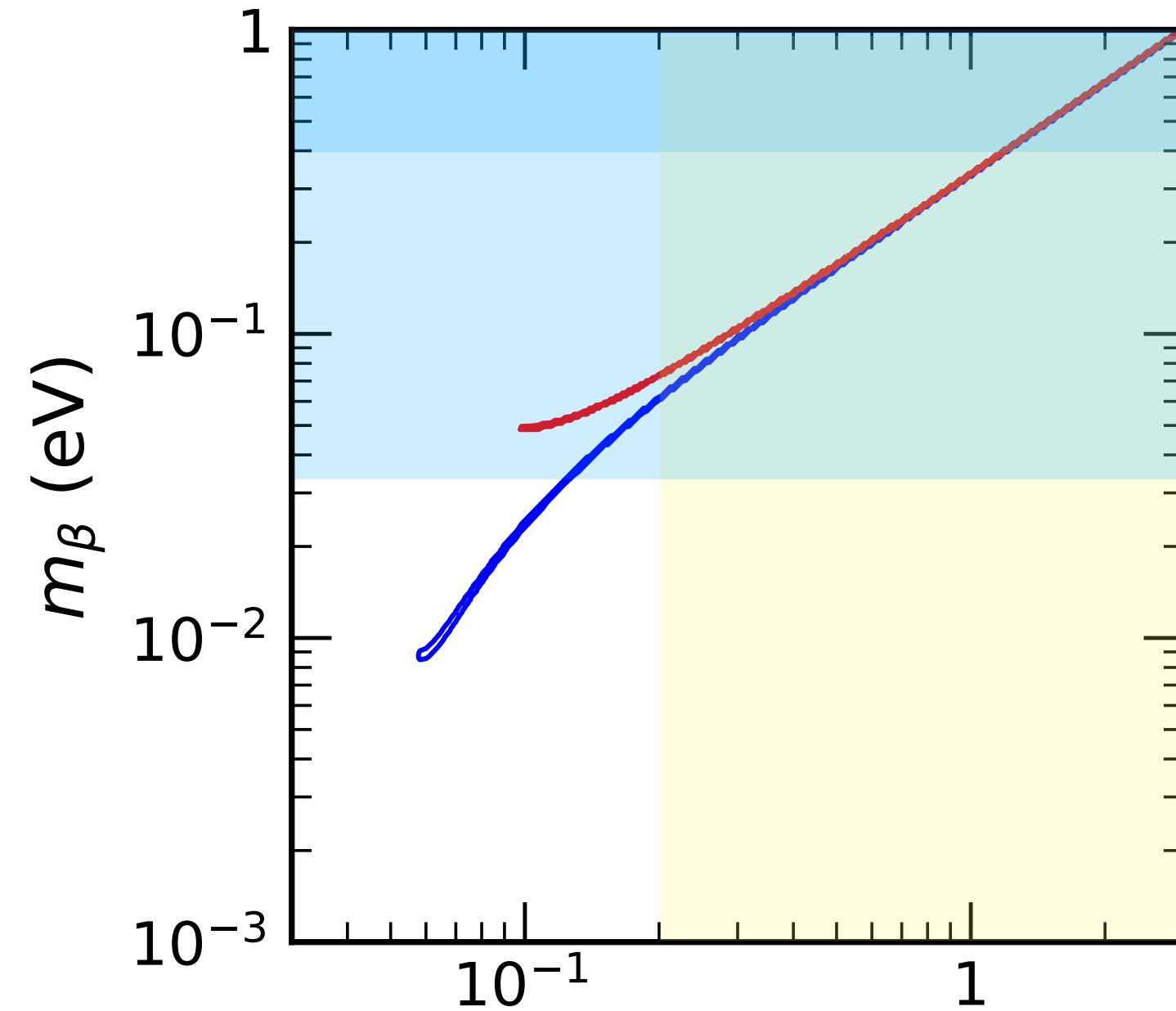
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Next-generation Projects ($\gtrsim 10$ years)

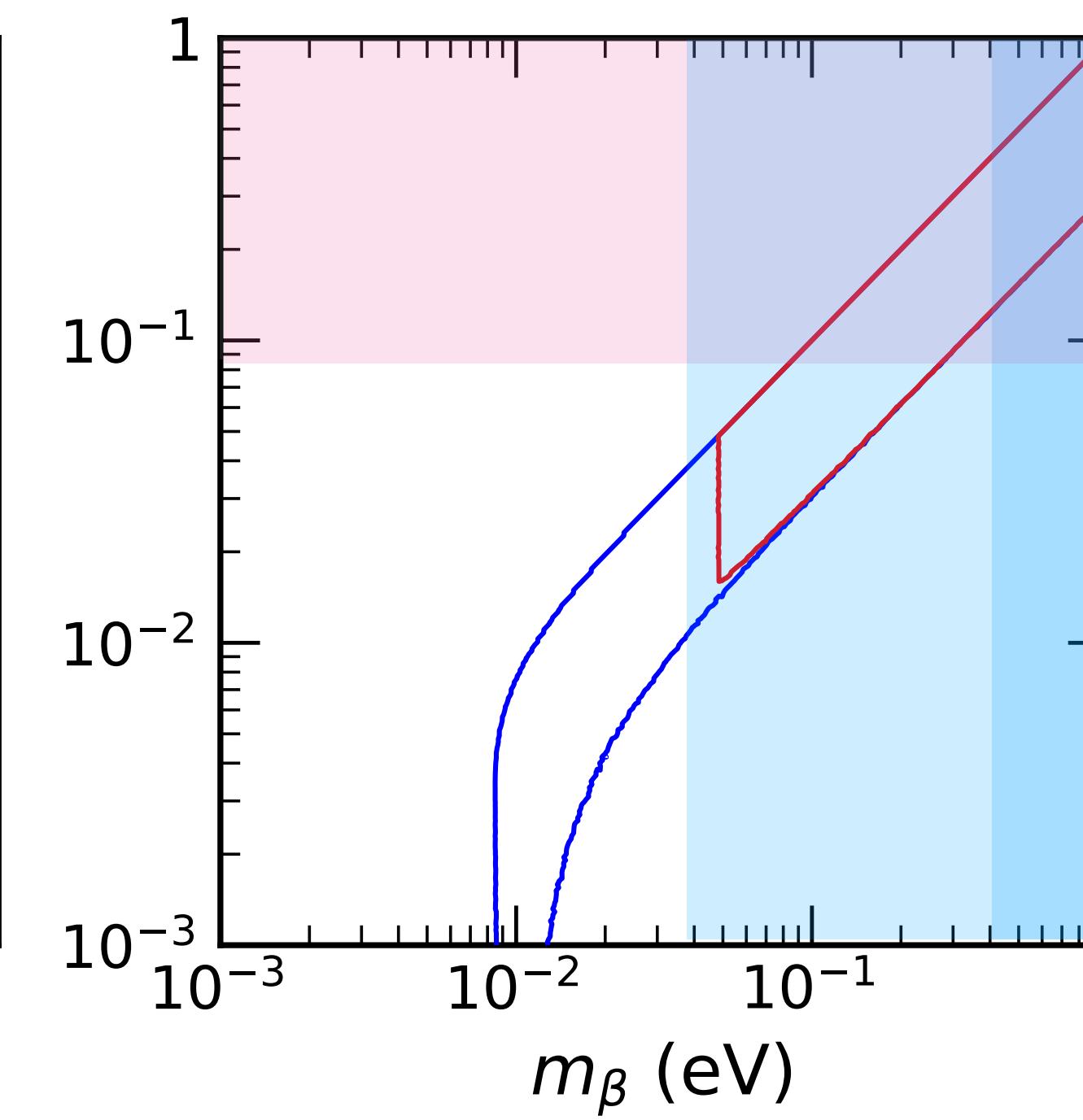
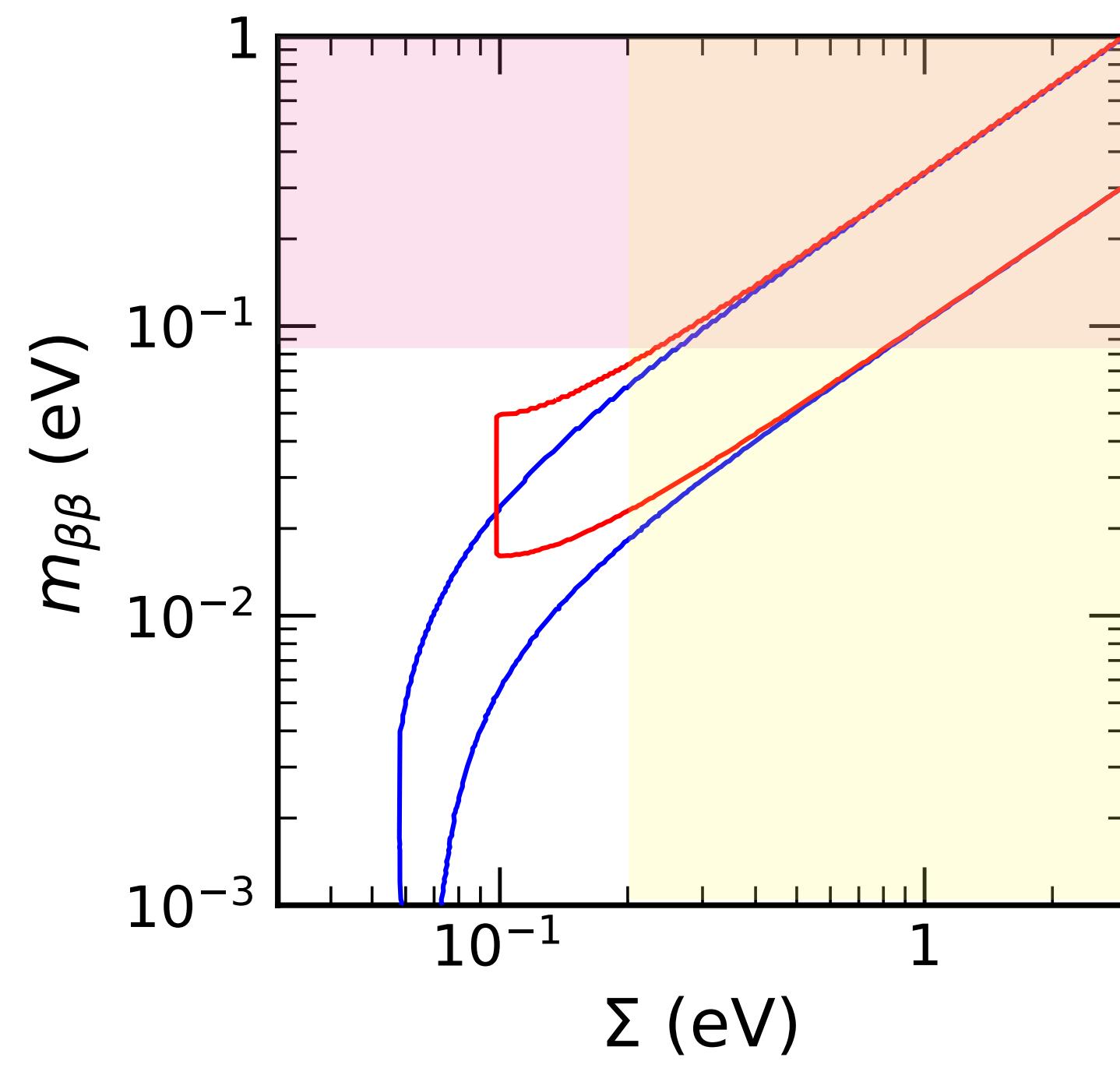


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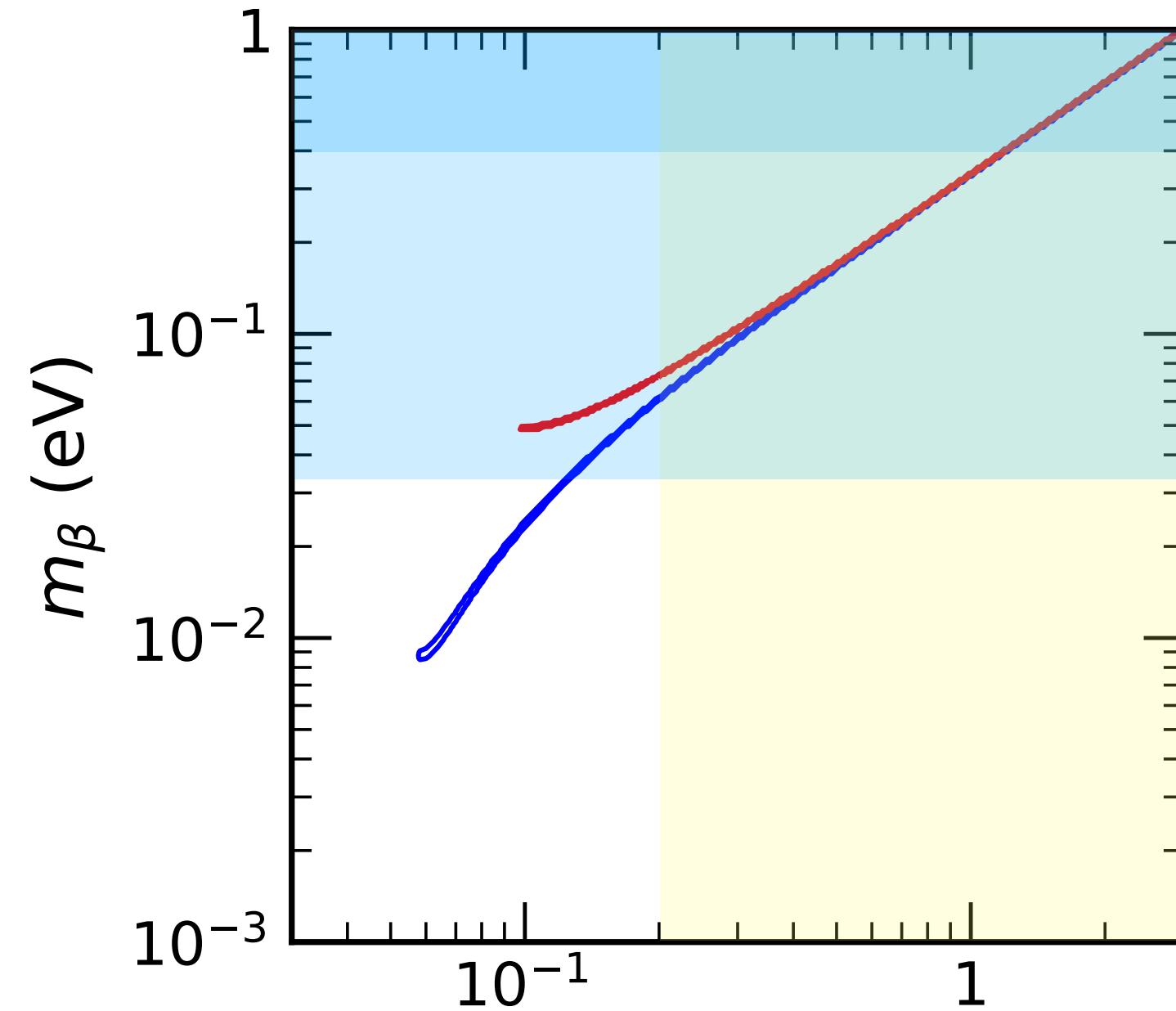


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β decay - Project-8, ...

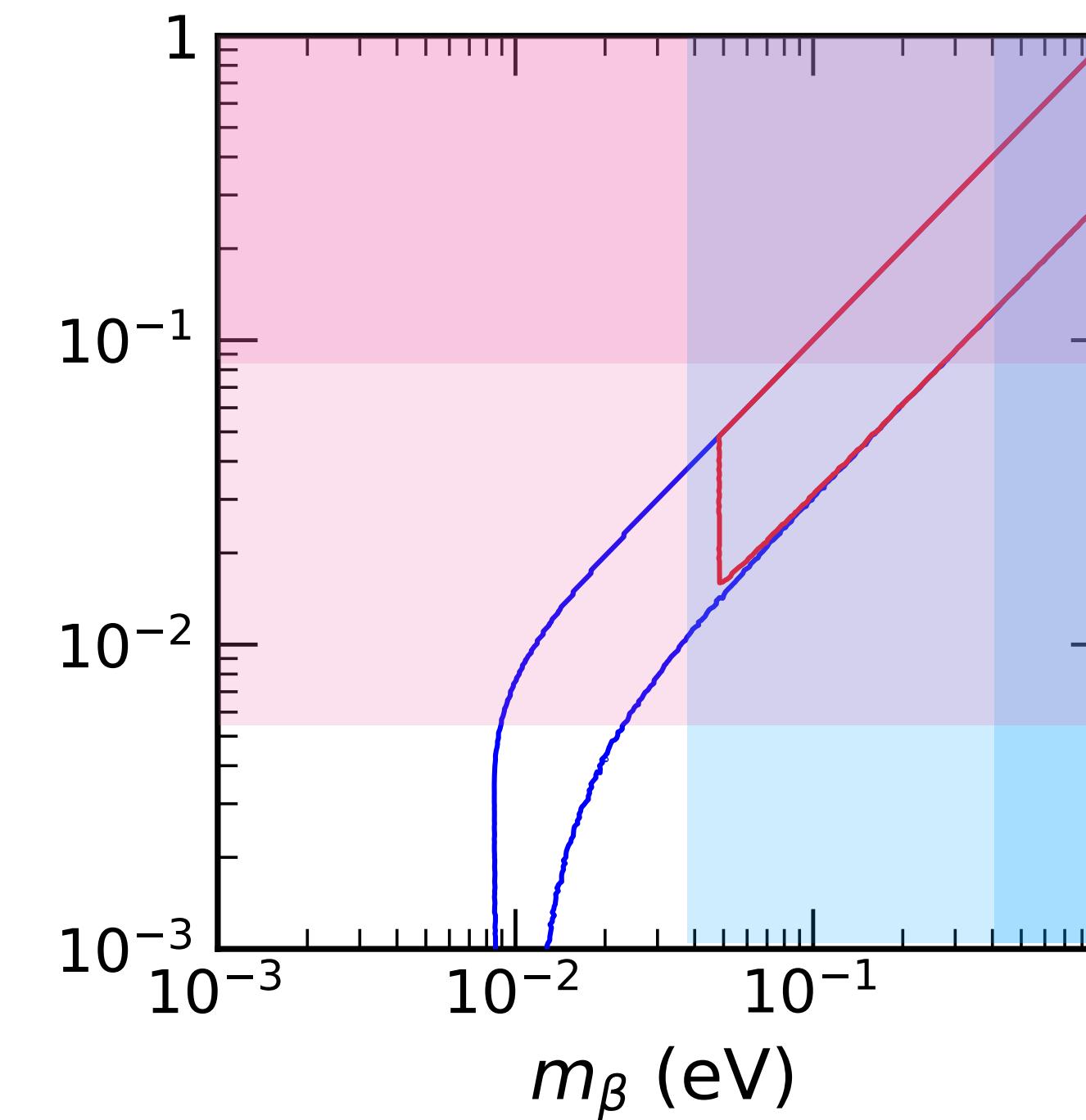
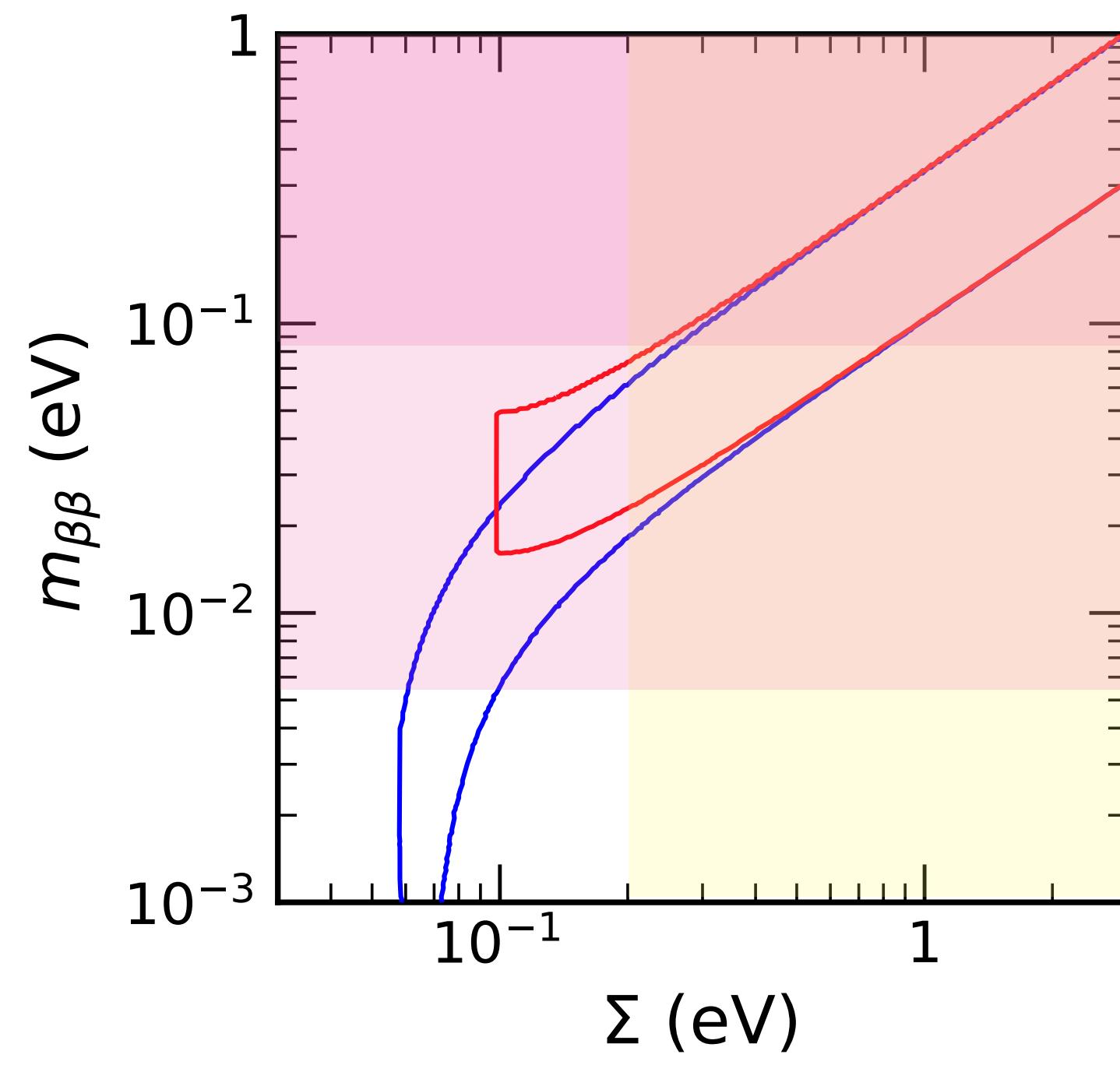


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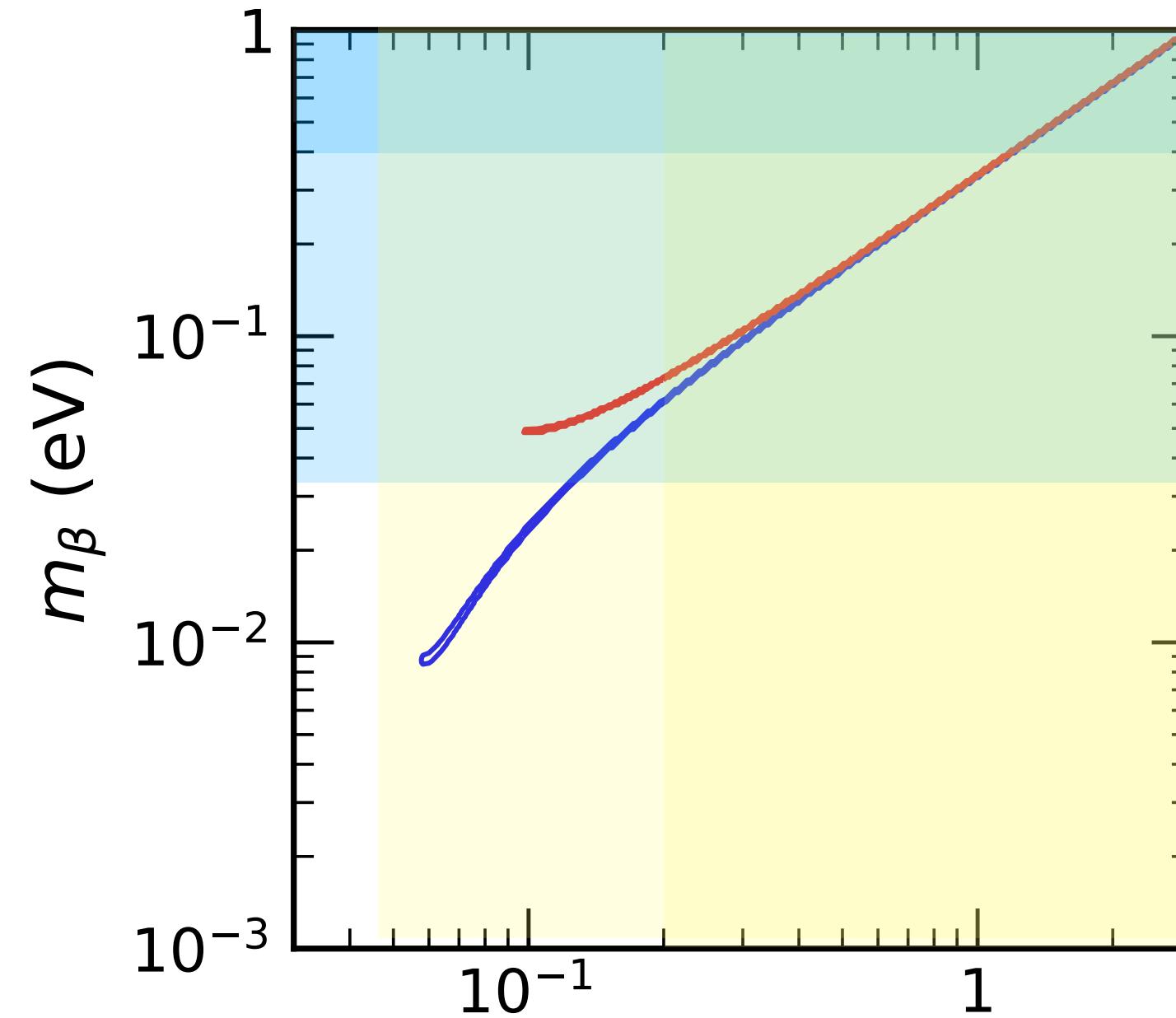
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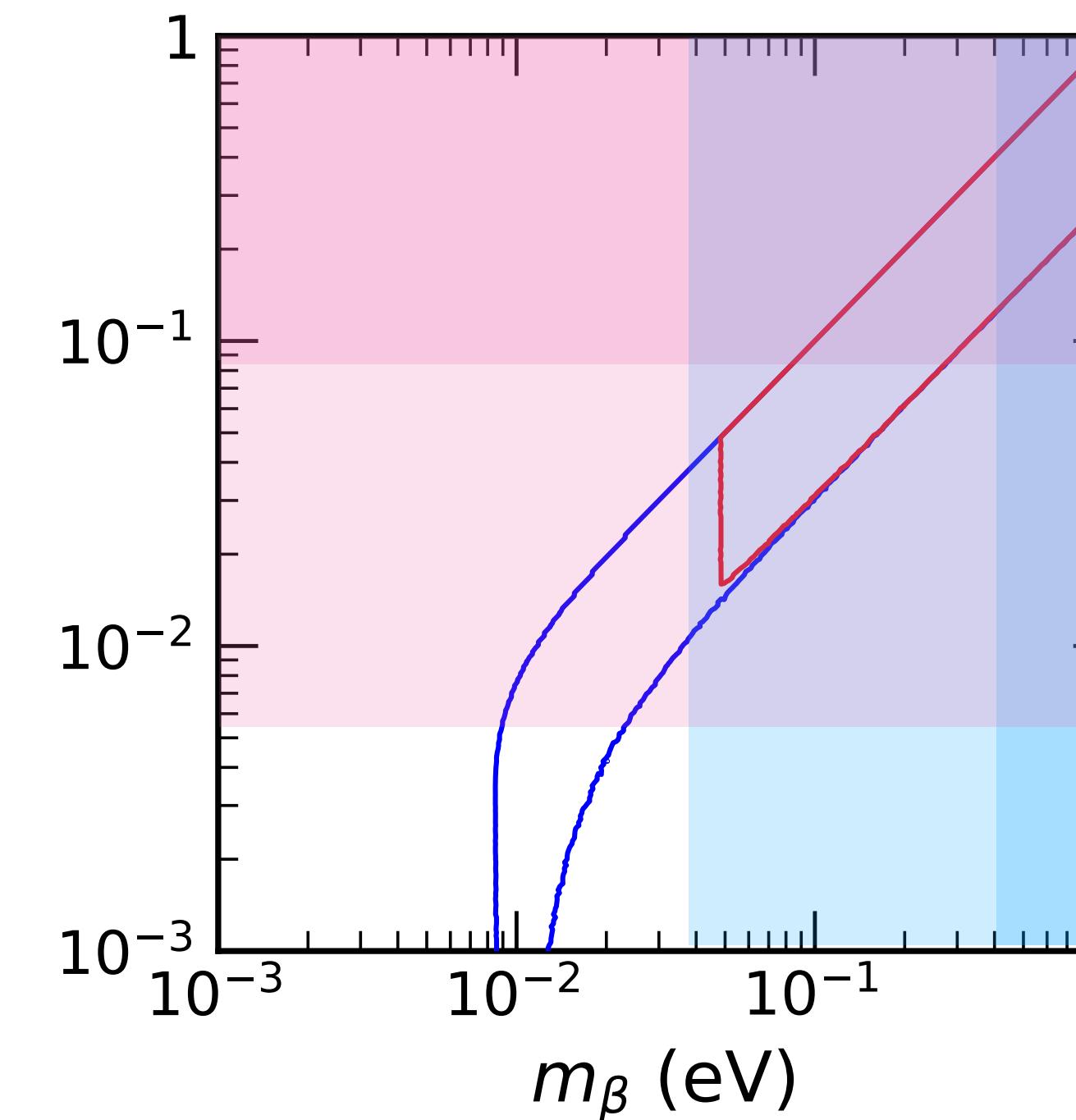
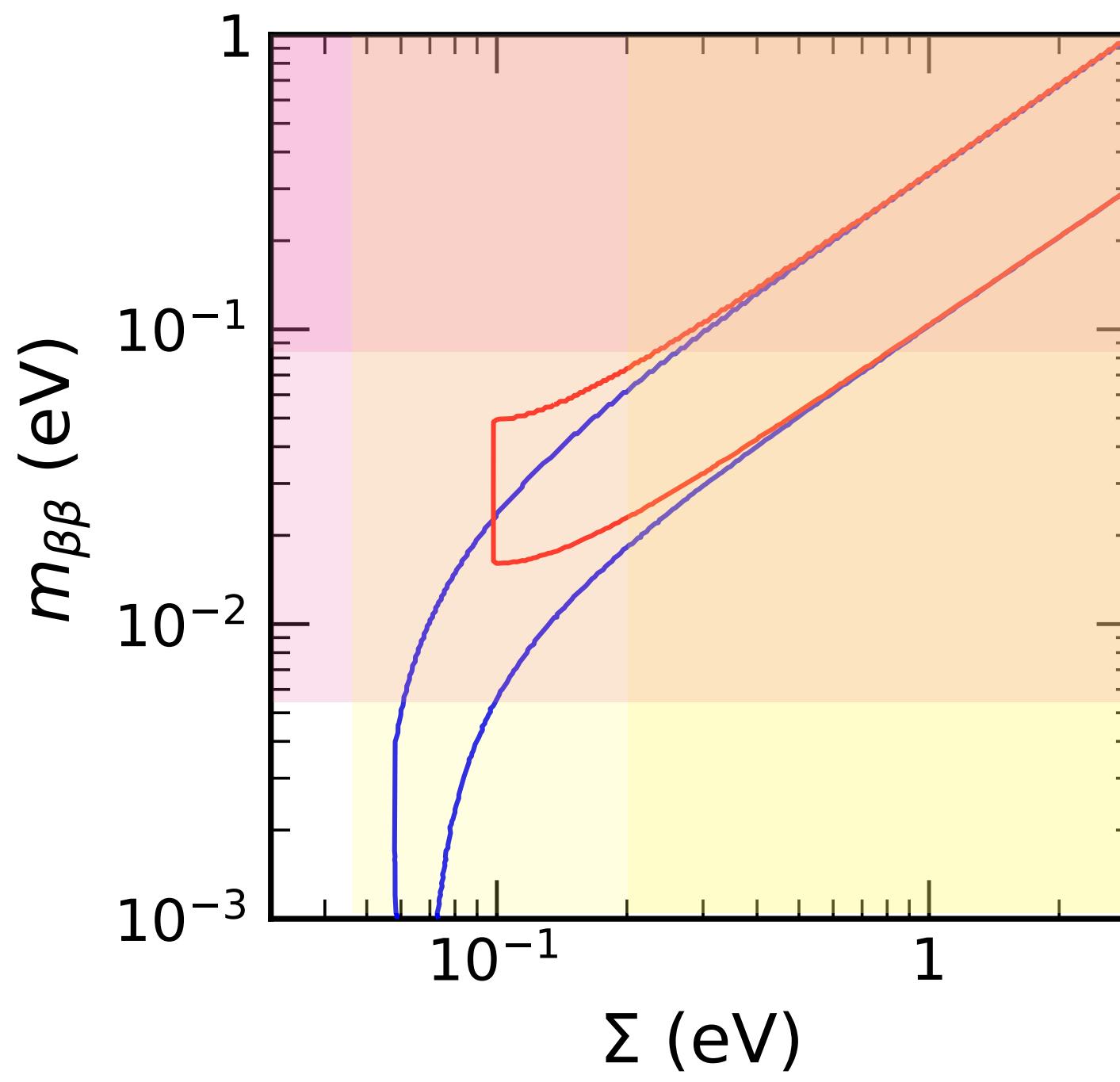


$0\nu\beta\beta$ decay
LEGEND, NEXO, CUPID, ...

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EUCLID, ...

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- **Outlook**

The 3ν framework is at a turning point: future synergies (or tensions) across oscillation, β-decay, 0νββ, cosmology will be decisive