3-Dimensional WIMP Effective Velocity Distribution

Chung-Lin Shan

TAUP 2025, Xichang, Sichuan, China August 26, 2025

Based on arXiv:2103.06485, 2103.06883



Questions

Arguments

3-D Monte Carlo elastic WIMP-nucleus scattering simulation

Numerical results

Radial component (magnitude)

Angular component (direction)

Angular distribution of the 3-D average kinetic energy

Forward-backward asymmetry

Summary





Q1: Does the subgroup of WIMPs scattering off target nuclei have the same 3-D velocity distribution as the main group of the entire halo WIMPs (impinging on a (directional) direct Dark Matter detector but not necessarily scattering off target nuclei)?



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A1: Yes?



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Q2: Does the WIMPs scattering off Ar or Xe nuclei have the same 3-D velocity distribution as the WIMPs scattering off Si or Ge nuclei?



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A1: Yes?

Q2: Does the WIMPs scattering off Ar or Xe nuclei have the same 3-D velocity distribution as the WIMPs scattering off Si or Ge nuclei?

A2: Yes?



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A2: Yes?

Q3: Once one can reconstruct the (3-D) velocity distribution of WIMPs by using (directional) direct detection data, is the reconstructed (3-D) velocity distribution indeed that of the entire halo WIMPs?



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A2: Yes?

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A3: Yes?



Q1: Does the subgroup of WIMPs scattering off target nuclei have the same 3-D velocity distribution as the main group of the entire halo WIMPs (impinging on a (directional) direct Dark Matter detector but not necessarily scattering off target nuclei)?

A1: No...

□ Q2: Does the WIMPs scattering off Ar or Xe nuclei have the same 3-D velocity distribution as the WIMPs scattering off Si or Ge nuclei?

A2: No...

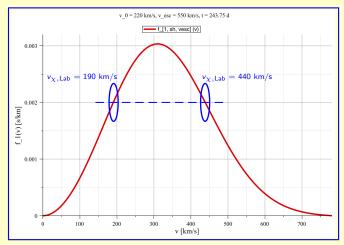
□ Q3: Once one can reconstruct the (3-D) velocity distribution of WIMPs by using (directional) direct detection data, is the reconstructed (3-D) velocity distribution indeed that of the entire halo WIMPs?

A3: Not directly?? \implies Yes??





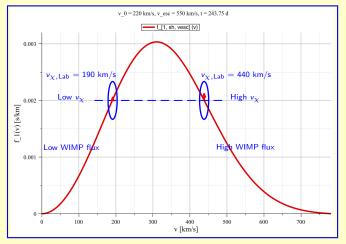
☐ Shifted Maxwellian velocity distribution





☐ Arguments

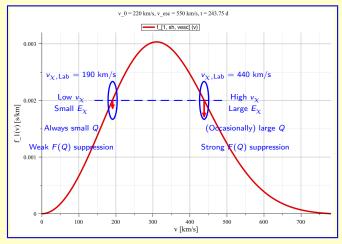
□ Proportionality of the WIMP flux to the incident velocity





☐ Arguments

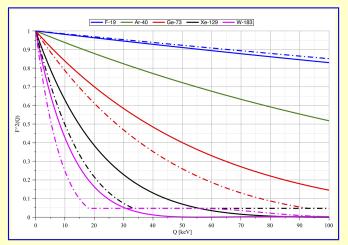
☐ Cross section (nuclear form factor) suppression





Arguments

☐ Recoil-energy dependence of the nuclear form factor

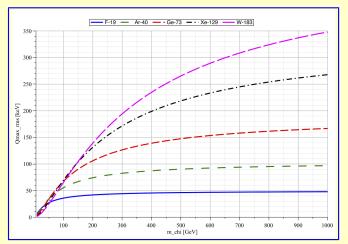


 $[\mathsf{CLS},\ \mathsf{arXiv:}2103.06883\ (2021)]$



☐ Arguments

 \square WIMP-mass dependence of the maximal transferable recoil energy $Q_{\max, rms}$

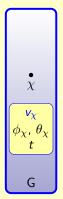




3-D Monte Carlo "scattering-by-scattering" elastic WIMP-nucleus scattering simulation



☐ Simulation workflow



 $[\mathsf{CLS},\ \mathsf{arXiv}{:}2103.06485\ (2021)]$



- □ 3-D velocity distribution of Galactic WIMPs
 - ➤ Simple Maxwellian velocity distribution

$$\mathit{f}_{\chi,\mathsf{G},\mathsf{r}}(\mathit{v}_{\chi,\mathsf{G}}) = \left[\left(\frac{\sqrt{\pi}}{4} \right) \mathsf{erf} \left(\frac{\mathit{v}_{\mathsf{esc}}}{\mathit{v}_0} \right) - \left(\frac{\mathit{v}_{\mathsf{esc}}}{2\mathit{v}_0} \right) e^{-\mathit{v}_{\mathsf{esc}}^2/\mathit{v}_0^2} \right]^{-1} \left(\frac{\mathit{v}_{\chi,\mathsf{G}}^2}{\mathit{v}_0^3} \right) e^{-\mathit{v}_{\chi,\mathsf{G}}^2/\mathit{v}_0^2} \qquad \text{for } \mathit{v}_{\chi,\mathsf{G}} \leq \mathit{v}_{\mathsf{esc}} = 0$$

- □ 3-D velocity distribution of Galactic WIMPs
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$$f_{\chi,\mathsf{G},\mathsf{r}}(\mathsf{v}_{\chi,\mathsf{G}}) = \left[\left(\frac{\sqrt{\pi}}{4} \right) \operatorname{erf} \left(\frac{\mathsf{v}_{\mathsf{esc}}}{\mathsf{v}_0} \right) - \left(\frac{\mathsf{v}_{\mathsf{esc}}}{2\mathsf{v}_0} \right) \operatorname{e}^{-\mathsf{v}_{\mathsf{esc}}^2/\mathsf{v}_0^2} \right]^{-1} \left(\frac{\mathsf{v}_{\chi,\mathsf{G}}^2}{\mathsf{v}_0^3} \right) \operatorname{e}^{-\mathsf{v}_{\chi}^2,\mathsf{G}/\mathsf{v}_0^2} \qquad \text{for } \mathsf{v}_{\chi,\mathsf{G}} \leq \mathsf{v}_{\mathsf{esc}} + \mathsf{v}_{\mathsf{esc}} + \mathsf{v}_{\mathsf{G}} + \mathsf{$$

Angular distribution

$$f_{\chi,\mathsf{G},\phi}(\phi_{\chi,\mathsf{G}}) = 1$$
 $\phi_{\chi,\mathsf{G}} \in (-\pi, \pi]$

$$f_{\chi,\mathsf{G}, heta}(heta_{\chi,\mathsf{G}}) = 1$$
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> Angular distribution

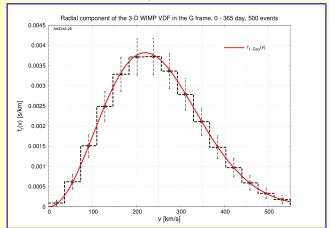
$$\begin{split} f_{\chi,\mathsf{G},\phi}(\phi_{\chi,\mathsf{G}}) &= 1 & \phi_{\chi,\mathsf{G}} \in (-\pi,\ \pi] \\ f_{\chi,\mathsf{G},\theta}(\theta_{\chi,\mathsf{G}}) &= 1 & \theta_{\chi,\mathsf{G}} \in [-\pi/2,\ \pi/2] \end{split}$$

> Time dependence

$$f_t(t) = 1$$
 $t \in [t_{\mathsf{start}}, \ t_{\mathsf{end}}]$



□ Radial component (magnitude) of the 3-D WIMP velocity distribution (Galactic frame, 0 - 365 day, 500 events)

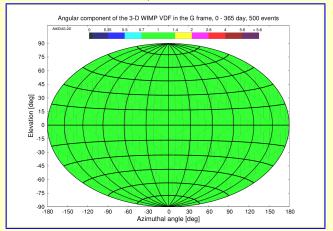


[CLS, arXiv:2103.06485 (2021)]

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☐ Angular component (direction) of the 3-D WIMP velocity distribution (Galactic frame, 0 - 365 day, 500 events)

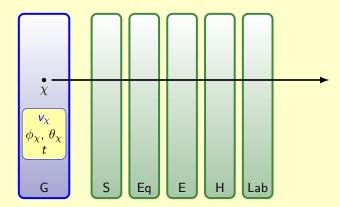


[CLS, arXiv:2103.06485 (2021)]

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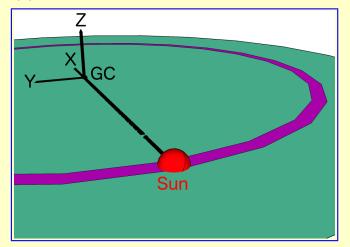


□ Simulation workflow



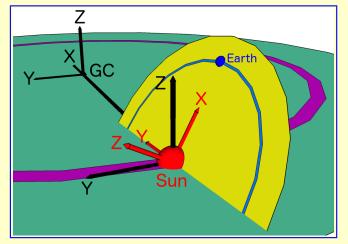


□ Galactic (G) coordinate system



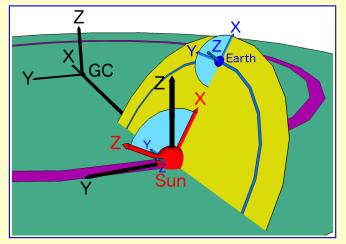


□ Ecliptic (S) coordinate system



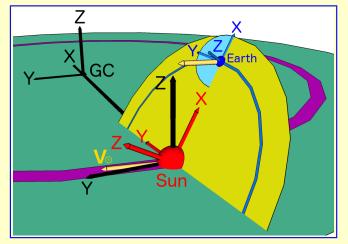


□ Equatorial (Eq) coordinate system



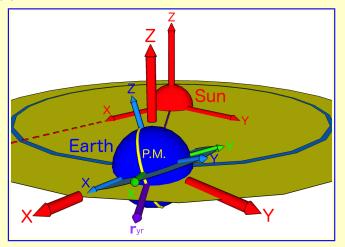


□ Equatorial (Eq) coordinate system



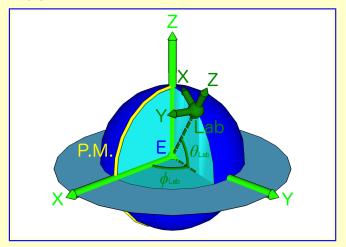


□ Earth (E) coordinate system





☐ Horizontal (H) coordinate system

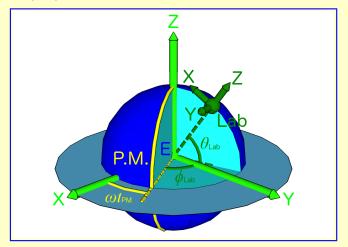


[CLS, arXiv:1905.11279 (2019)]

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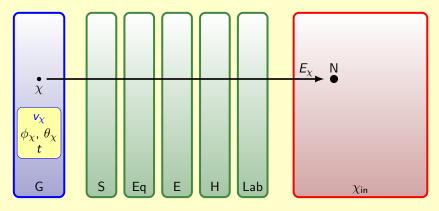


□ Laboratory (Lab) coordinate system



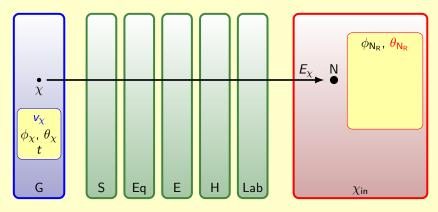


□ Simulation workflow



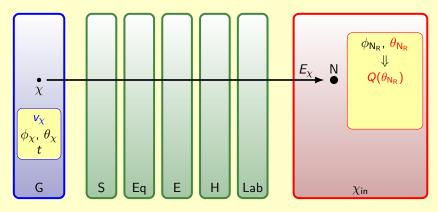


■ Simulation workflow



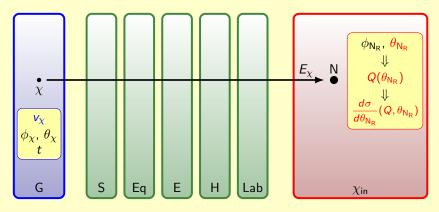


□ Simulation workflow



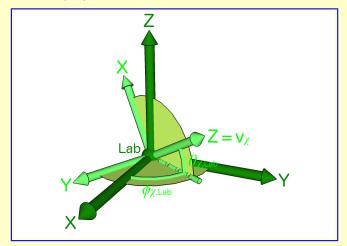


■ Simulation workflow



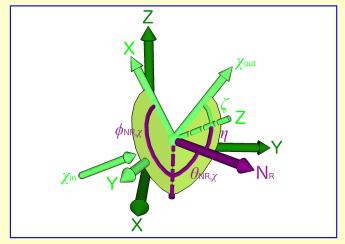


 \Box Incoming-WIMP (χ_{in}) coordinate system





☐ Orientation of the scattering plane and the (equivalent) recoil angle





- Scattering simulation
 - > Azimuthal distribution

$$f_{\mathsf{NR},\chi_{\mathsf{in}},\phi}(\phi_{\mathsf{NR},\chi_{\mathsf{in}}})=1$$

$$\phi_{\mathsf{N}_\mathsf{R},\chi_\mathsf{in}} \in (-\pi,\;\pi]$$



- Scattering simulation
 - Azimuthal distribution

$$f_{\mathsf{NR},\chi_{\mathsf{in}},\phi}(\phi_{\mathsf{NR},\chi_{\mathsf{in}}}) = 1$$
 $\phi_{\mathsf{NR},\chi_{\mathsf{in}}} \in (-\pi, \pi]$

> Recoil energy of the scattered target nucleus

$$Q(\theta_{\mathsf{N}_{\mathsf{R}},\chi_{\mathsf{in}}}) = \left[\frac{4m_{\chi} m_{\mathsf{N}}}{(m_{\chi} + m_{\mathsf{N}})^2} E_{\chi}\right] \sin^2(\theta_{\mathsf{N}_{\mathsf{R}},\chi_{\mathsf{in}}}) \qquad E_{\chi} = \frac{1}{2} m_{\chi} v_{\chi,\mathsf{Lab}}^2 \qquad \theta_{\mathsf{N}_{\mathsf{R}},\chi_{\mathsf{in}}} \in [0, \ \pi/2]$$



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 Cross section (nuclear form factor) suppression on the equivalent recoil angle

$$\begin{split} d\sigma &= \frac{1}{v_{\chi, \text{Lab}}^2} \left(\frac{\sigma_0}{4m_{\text{r}, \text{N}}^2} \right) F^2(q) \, dq^2 = \frac{1}{v_{\chi, \text{Lab}}^2} \left(\frac{m_{\text{N}}}{2m_{\text{r}, \text{N}}^2} \right) \sigma_0 F^2(Q) \, dQ \qquad \qquad q = \sqrt{2m_{\text{N}}Q} \\ \frac{d\sigma}{d\theta_{\text{N}_{\text{P}, \text{Y}in}}} &= \left[\sigma_0^{\text{SI}} F_{\text{SI}}^2 \left(Q(\theta_{\text{N}_{\text{R}}, \chi_{\text{in}}}) \right) + \sigma_0^{\text{SD}} F_{\text{SD}}^2 \left(Q(\theta_{\text{N}_{\text{R}}, \chi_{\text{in}}}) \right) \right] \sin(2\theta_{\text{N}_{\text{R}}, \chi_{\text{in}}}) \end{split}$$



- Scattering simulation
 - Azimuthal distribution

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Cross section (nuclear form factor) suppression on the equivalent recoil angle

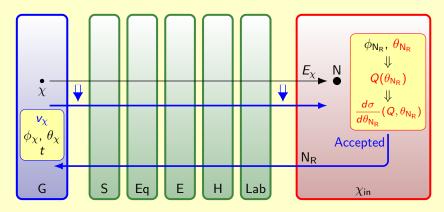
$$\begin{split} d\sigma &= \frac{1}{v_{\chi,\text{Lab}}^2} \left(\frac{\sigma_0}{4m_{r,N}^2} \right) F^2(q) dq^2 = \frac{1}{v_{\chi,\text{Lab}}^2} \left(\frac{m_\text{N}}{2m_{r,N}^2} \right) \sigma_0 F^2(Q) dQ \qquad q = \sqrt{2m_\text{N}Q} \\ \frac{d\sigma}{d\theta_{\text{N}_\text{R}},\chi_{\text{in}}} &= \left[\sigma_0^{\text{SI}} F_{\text{SI}}^2 \left(Q(\theta_{\text{N}_\text{R}},\chi_{\text{in}}) \right) + \sigma_0^{\text{SD}} F_{\text{SD}}^2 \left(Q(\theta_{\text{N}_\text{R}},\chi_{\text{in}}) \right) \right] \sin(2\theta_{\text{N}_\text{R}},\chi_{\text{in}}) \end{split}$$

> Generating probability distribution of the equivalent recoil angle

$$f_{\mathsf{N}_{\mathsf{R}},\chi_{\mathsf{in}},\theta}(\theta_{\mathsf{N}_{\mathsf{R}},\chi_{\mathsf{in}}}) = \left(\frac{v_{\chi,\mathsf{Lab}}}{v_{\chi,\mathsf{cutoff}}}\right) \left[\sigma_0^{\mathsf{SI}} F_{\mathsf{SI}}^2\left(Q(\theta_{\mathsf{N}_{\mathsf{R}},\chi_{\mathsf{in}}})\right) + \sigma_0^{\mathsf{SD}} F_{\mathsf{SD}}^2\left(Q(\theta_{\mathsf{N}_{\mathsf{R}},\chi_{\mathsf{in}}})\right)\right] \sin(2\theta_{\mathsf{N}_{\mathsf{R}},\chi_{\mathsf{in}}})$$
[CLS, arXiv:2103.06485 (2021)]

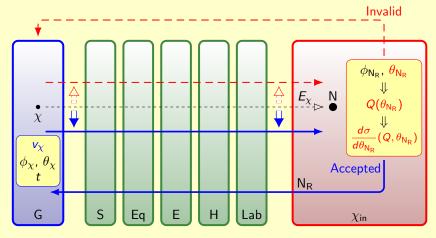


□ Simulation workflow



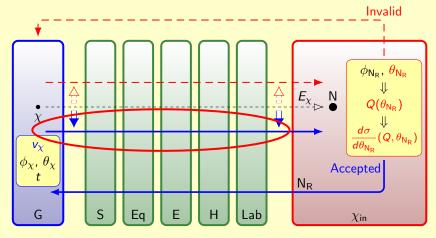


■ Simulation workflow





■ Simulation workflow





Numerical results

-Numerical results

Radial component (magnitude) in the Galactic coordinate system

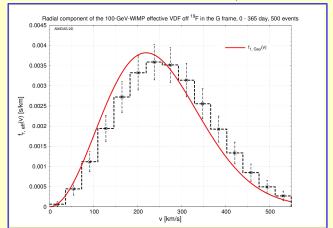


Radial component (magnitude) in the Galactic coordinate system



Radial component

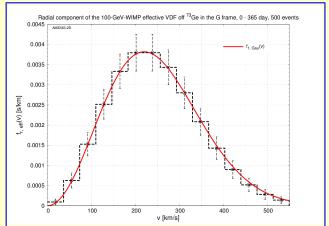
(100 GeV, off ¹⁹F, Galactic frame, 0 - 365 day, 500 events)





Radial component

(100 GeV, off 73 Ge, Galactic frame, 0 - 365 day, 500 events)



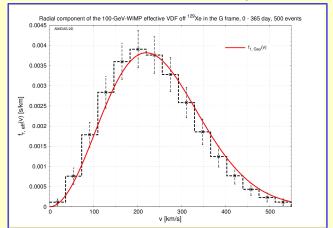
[CLS, arXiv:2103.06883 (2021)]

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Radial component

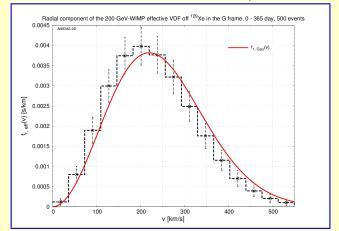
(100 GeV, off ¹²⁹Xe, Galactic frame, 0 - 365 day, 500 events)





Radial component

(200 GeV, off ¹²⁹Xe, Galactic frame, 0 - 365 day, 500 events)





Radial component (magnitude) in the Galactic coordinate system

3-D WIMP effective velocity distribution in the Galactic frame

☐ Annual modulation of the radial component			
(100 GeV, off ⁷³ Ge, Galactic frame,	day, 500 events)		

 $[\mathsf{CLS},\ \mathsf{arXiv}{:}2103.06883\ (2021)]$

Numerical results



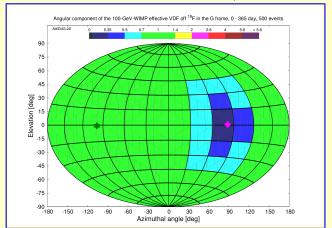


Angular component (direction) in the Galactic coordinate system



Angular component

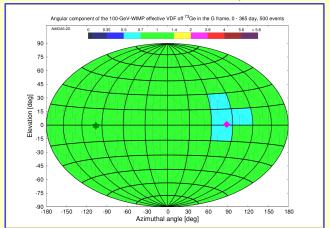
(100 GeV, off ¹⁹F, Galactic frame, 0 - 365 day, 500 events)





Angular component

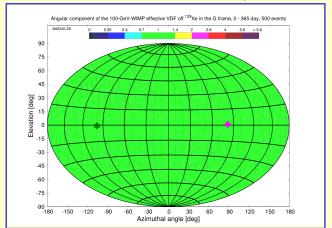
(100 GeV, off ⁷³Ge, Galactic frame, 0 - 365 day, 500 events)





Angular component

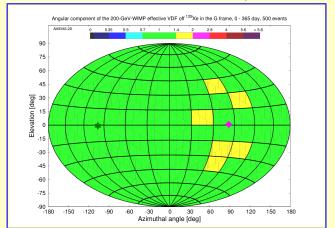
(100 GeV, off ¹²⁹Xe, Galactic frame, 0 - 365 day, 500 events)





Angular component

(200 GeV, off ¹²⁹Xe, Galactic frame, 0 - 365 day, 500 events)





Angular component (direction) in the Galactic coordinate system

3-D WIMP effective velocity distribution in the Galactic frame

□ Annual modulation of the angular component			
(<mark>100</mark> GeV,	off ⁷³ Ge, Galactic frame,	day, 500 events)	

 $[\mathsf{CLS},\ \mathsf{arXiv:}2103.06883\ (2021)]$

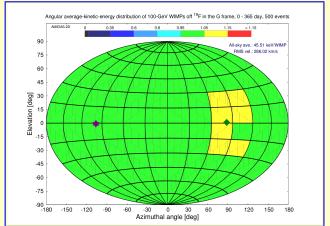


Angular distribution of the 3-D average kinetic energy in the Galactic coordinate system



3-D WIMP effective velocity distribution in the Galactic frame

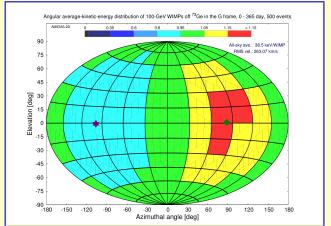
Angular distribution of the 3-D average kinetic energy (100 GeV, off ¹⁹F, Galactic frame, 0 - 365 day, 500 events)





3-D WIMP effective velocity distribution in the Galactic frame

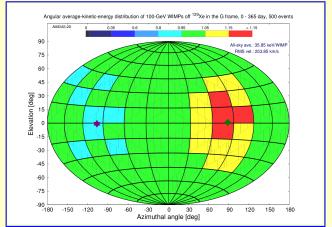
Angular distribution of the 3-D average kinetic energy (100 GeV, off ⁷³Ge, Galactic frame, 0 - 365 day, 500 events)





3-D WIMP effective velocity distribution in the Galactic frame

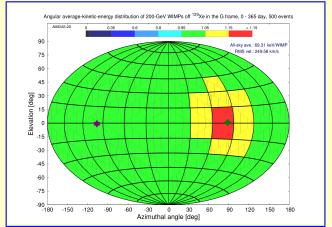
Angular distribution of the 3-D average kinetic energy (100 GeV, off ¹²⁹Xe, Galactic frame, 0 - 365 day, 500 events)





3-D WIMP effective velocity distribution in the Galactic frame

□ Angular distribution of the 3-D average kinetic energy (200 GeV, off ¹²⁹Xe, Galactic frame, 0 - 365 day, 500 events)





3-D WIMP effective velocity distribution in the Galactic frame

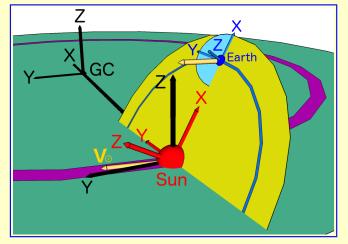
		average-kinetic-energy distribu	tion
(100 GeV,	off ⁷³ Ge, Galactic frame,	day, 500 events)	



Forward-backward asymmetry of the 3-D WIMP Galactic effective velocity distribution



□ Solar movement in the Dark Matter halo

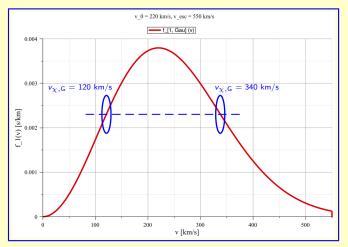


[CLS, arXiv:1905.11279 (2019)]



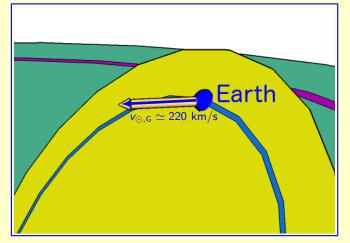


□ Simple Maxwellian velocity distribution





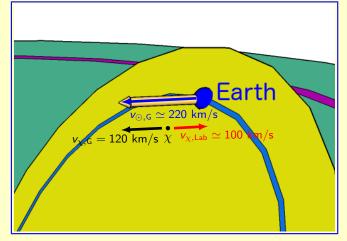
□ Forward-backward asymmetry



└─ Forward-backward asymmetry

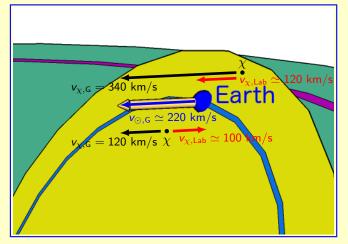
Forward-backward asymmetry of the 3-D WIMP G. eff. vel. dist.

☐ Forward-backward asymmetry



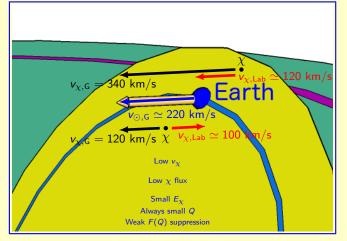


☐ Forward-backward asymmetry



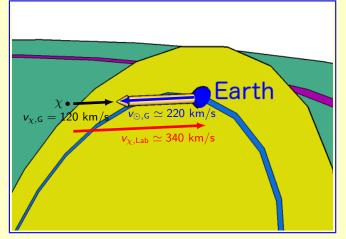


□ Forward-backward asymmetry





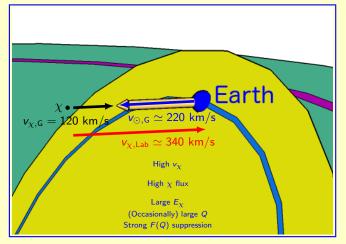
□ Forward-backward asymmetry







□ Forward-backward asymmetry



[CLS, arXiv:2103.06883 (2021)]

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□ We developed our full Monte Carlo "scattering-by-scattering" simulation for the "3-dimensional" elastic WIMP-nucleus scattering process



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The forward-moving and scattering WIMPs would always have larger average velocity/kinetic energy than the backward-moving WIMPs