

# Muon lifetime in $^{76}\text{Se}$

Benchmarking  $0\nu\beta\beta$  NMEs with the MONUMENT experiment

Elizabeth Mondragón on behalf of the  
MONUMENT Collaboration

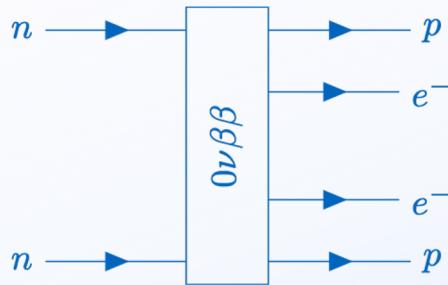
August 26<sup>th</sup> 2025





# M o t i v a t i o n

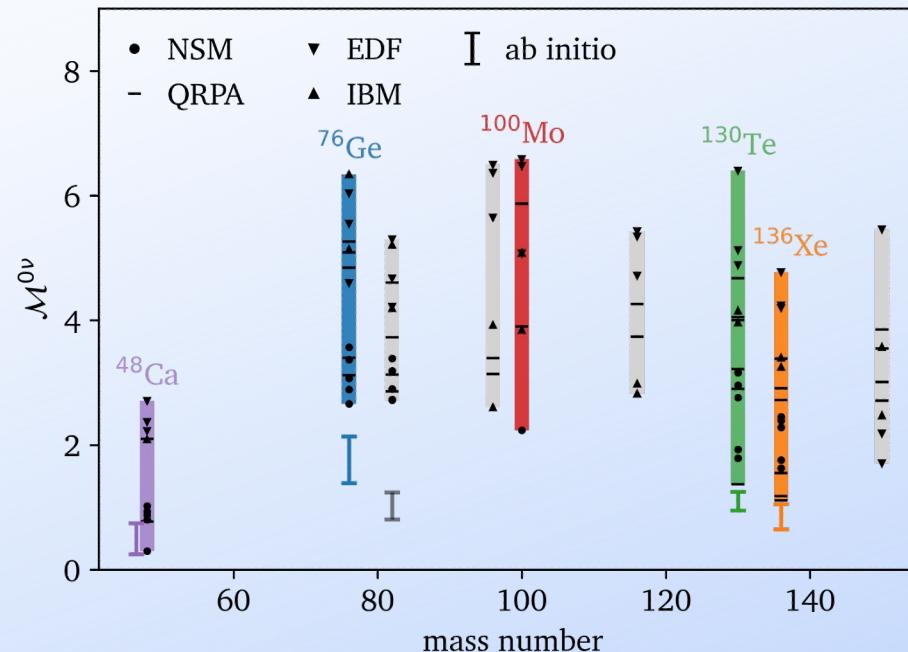
# $0\nu\beta\beta$ decay



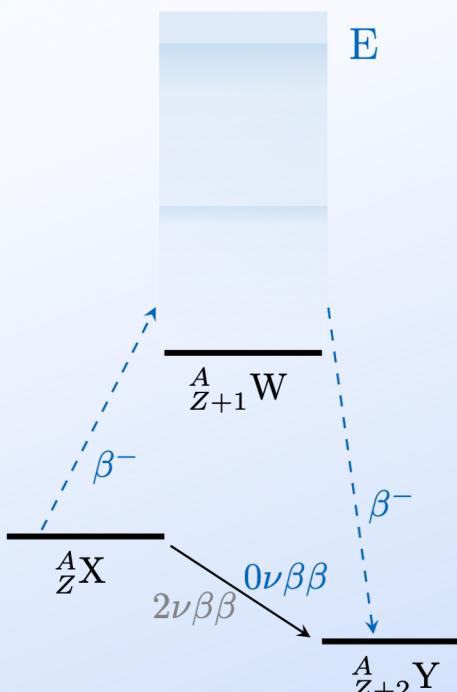
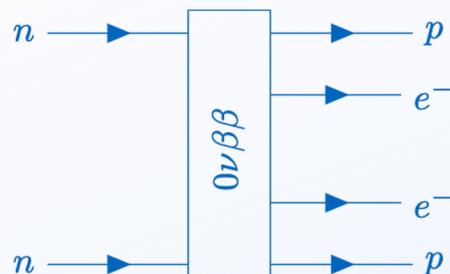
- Beyond the SM physics
- Majorana nature of neutrinos<sup>[1]</sup>

observable      kinematics      nuclear physics      particle physics

$$\frac{\Gamma^{0\nu}}{\ln 2} = \frac{1}{T_{1/2}^{0\nu}} = \sum_i G_i^{0\nu}(Q_{\beta\beta}, Z) \cdot |\tilde{\mathcal{M}}_i^{0\nu}|^2 \cdot \eta_i^2$$



# $0\nu\beta\beta$ decay

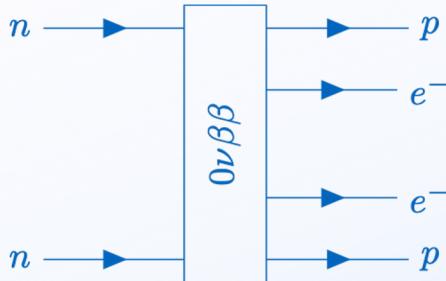


- Beyond the SM physics
- Majorana nature of neutrinos<sup>[1]</sup>

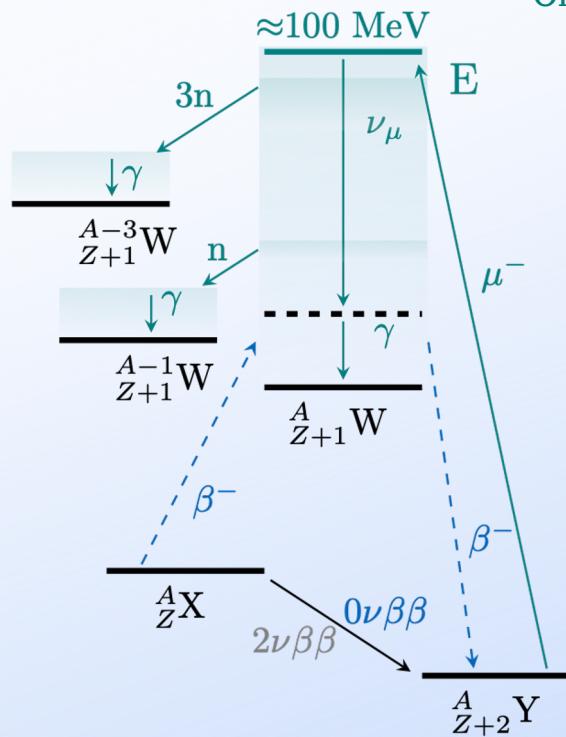


- [2] M. Kortelainen and J. Suhonen, Ordinary muon capture as a probe of virtual transitions of double-beta decay, EPL, vol. 58, pp. 666–672, (2002).  
[3] M. Kortelainen and J. Suhonen, Nuclear muon capture as a powerful probe of double-beta decays in light nuclei, J. Phys. G, vol. 30, no. 12, p. 2003, (2004).

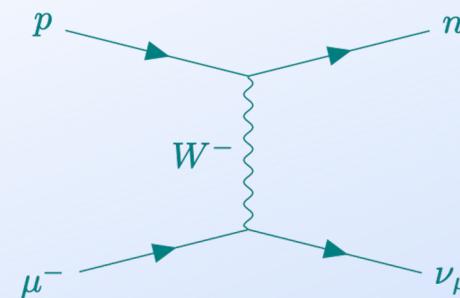
## $0\nu\beta\beta$ decay



- Beyond the SM physics
- Majorana nature of neutrinos<sup>[1]</sup>



## Ordinary Muon Capture [2,3]



- Similar momentum transfer
- Probe intermediate states
- Benchmark nuclear matrix element calculations



# Measurement

# Collaboration



ETH Zurich, Switzerland

IEAP, CTU, Prague, Czech Republic

CIFRA, Romania

JINR, Dubna, Russia

KU Leuven, Belgium

Osaka University, Japan

PSI, Switzerland

**TU Munich, Germany**

The University of Alabama, USA

Universiti Teknologi Malaysia, Malaysia

University of Jyväskylä, Finland

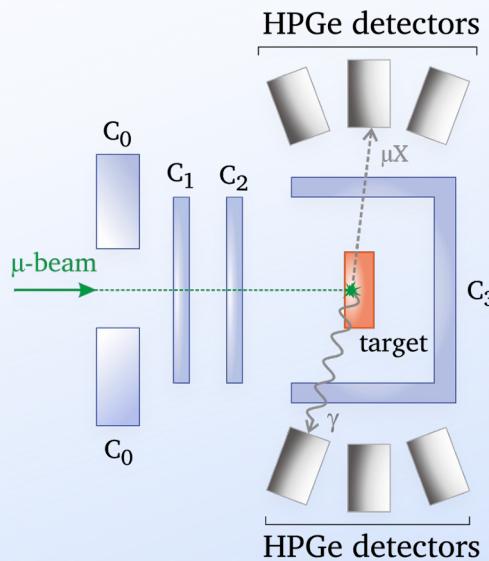
University of Zurich, Switzerland



# Measurement



- Beam momentum  
 $\sim 40 \text{ MeV}/c$



- **Tag muon trajectory from beam to target**

$$\mu_{\text{stop}} = \hat{C}_0 \wedge C_1 \wedge C_2 \wedge \hat{C}_3$$

rate of stopped muons  $\mathcal{O}(10^4) \text{ Hz}$



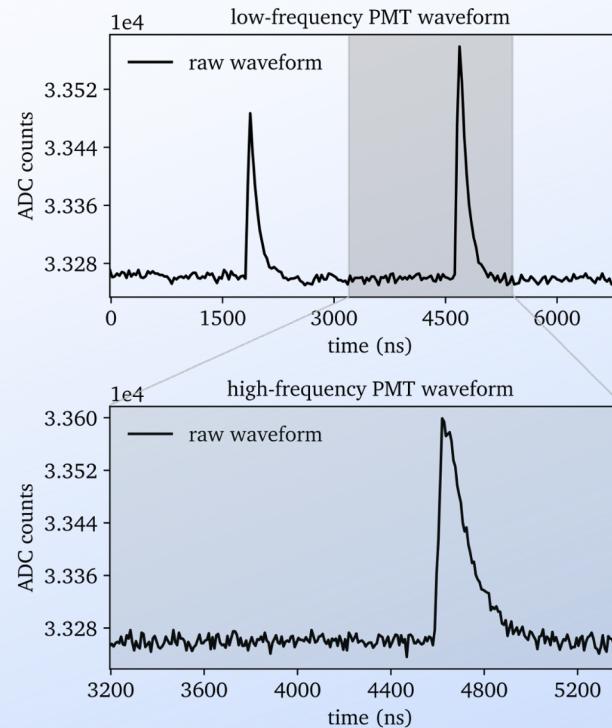
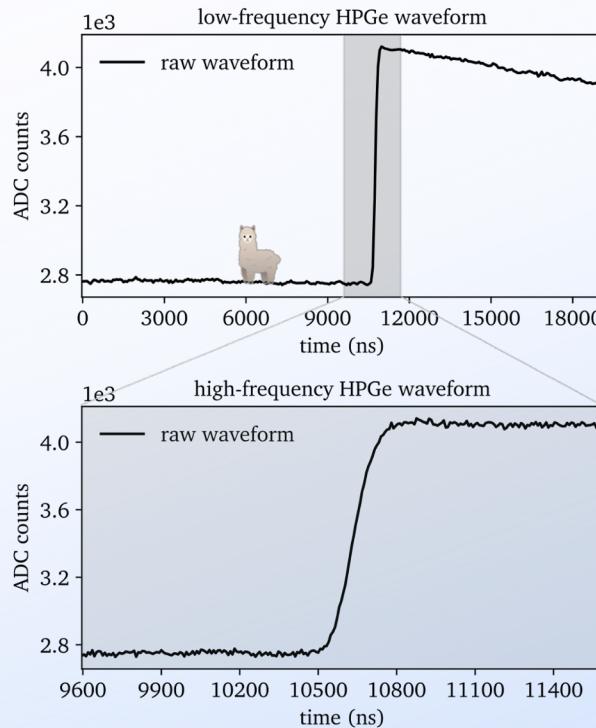
- **$\gamma$ -spectroscopy with HPGe detectors,**  
 typical rates of  $\mathcal{O}(10^3) \text{ Hz}$

- **Coincident measurement,**

$$\Delta t = t_{\text{HPGe}} - t_{\mu\text{stop}}$$

- Two parallel DAQ systems,  
**ALPACA** developed at Technical University  
 of Munich<sup>[4]</sup>

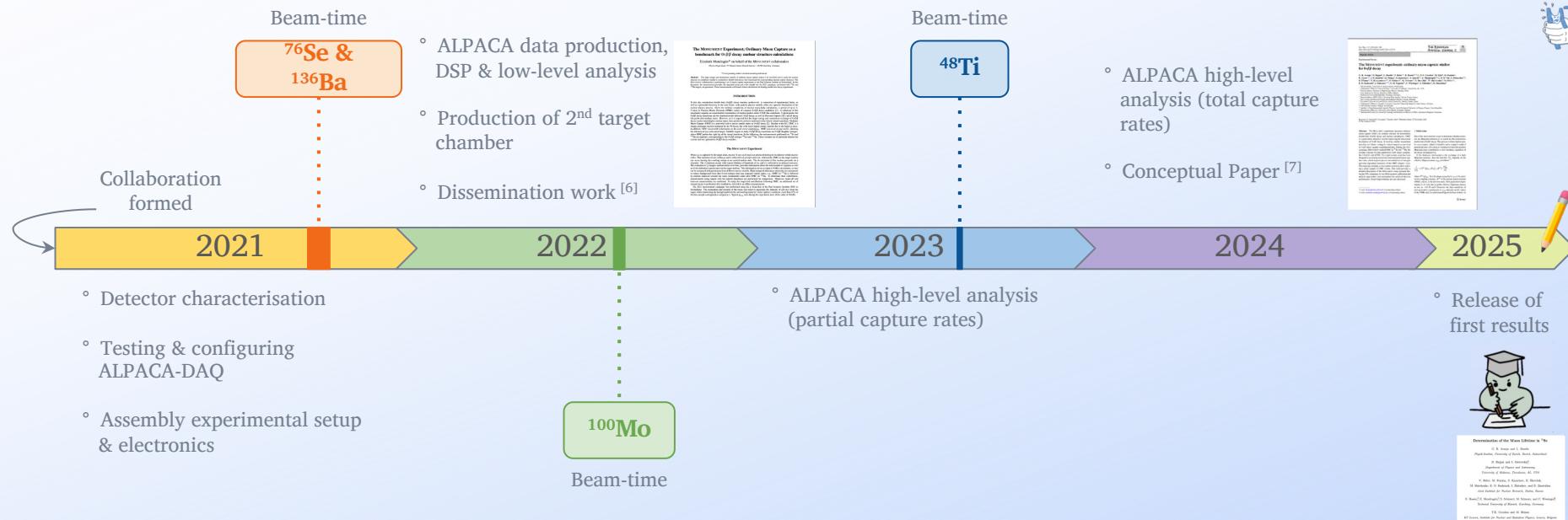
# ALPACA [4]



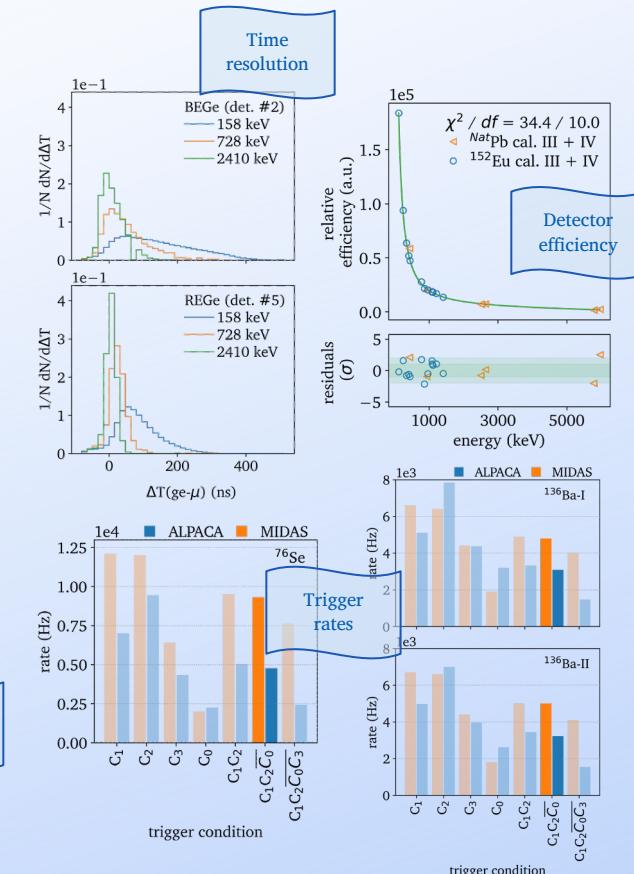
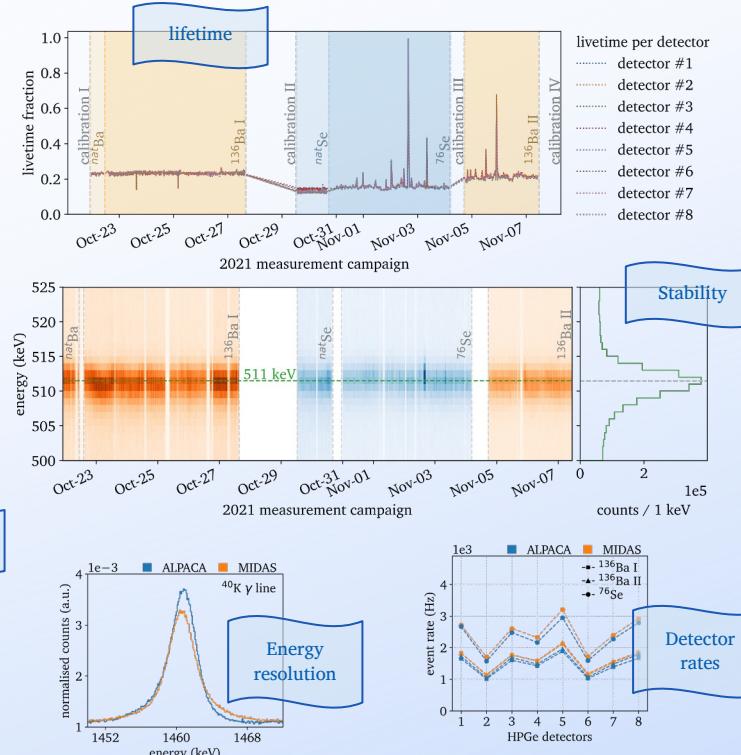
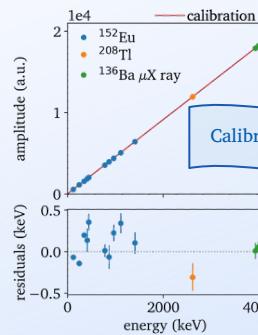
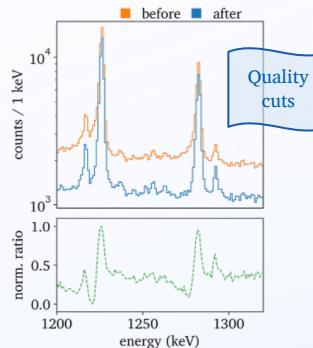
- **Full waveform**  
digitisation, low and high frequency windows
- **Offline analysis**
- $> 150$  TB data
- Analysis routines **based on GERDA**<sup>[5]</sup>



# Timeline



# Low-level analysis

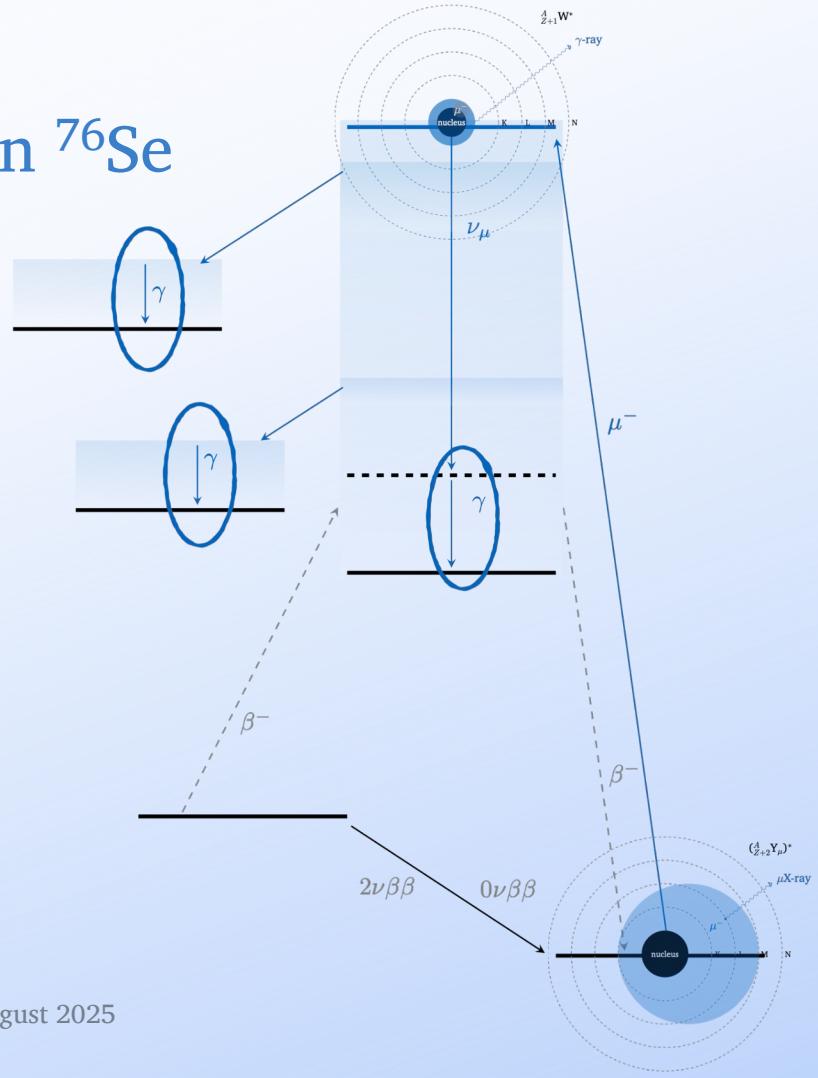




# R e s u l t s

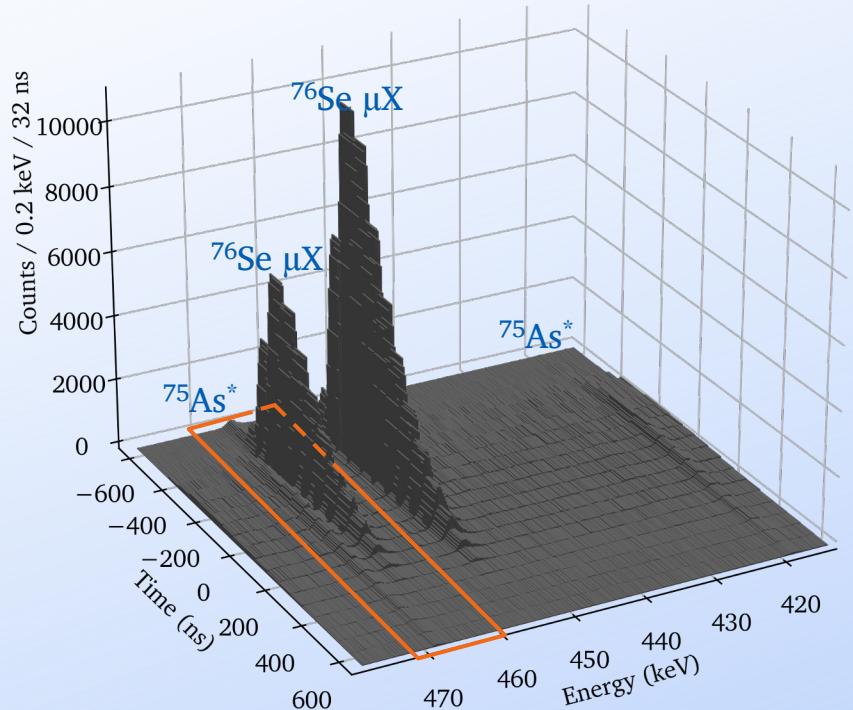
# High-level analysis: $\mu$ lifetime in $^{76}\text{Se}$

- Muon stopped at target atom  $\rightarrow \mu\text{X-rays}$
- After OMC, de-excitation via  $\gamma$ -ray emission
- $\Delta t = t_{\gamma\text{-rays}} - t_{\mu\text{stop}}$  tell about the muon lifetime
- Related to **total capture strength** which can be calculated by nuclear structure theorists



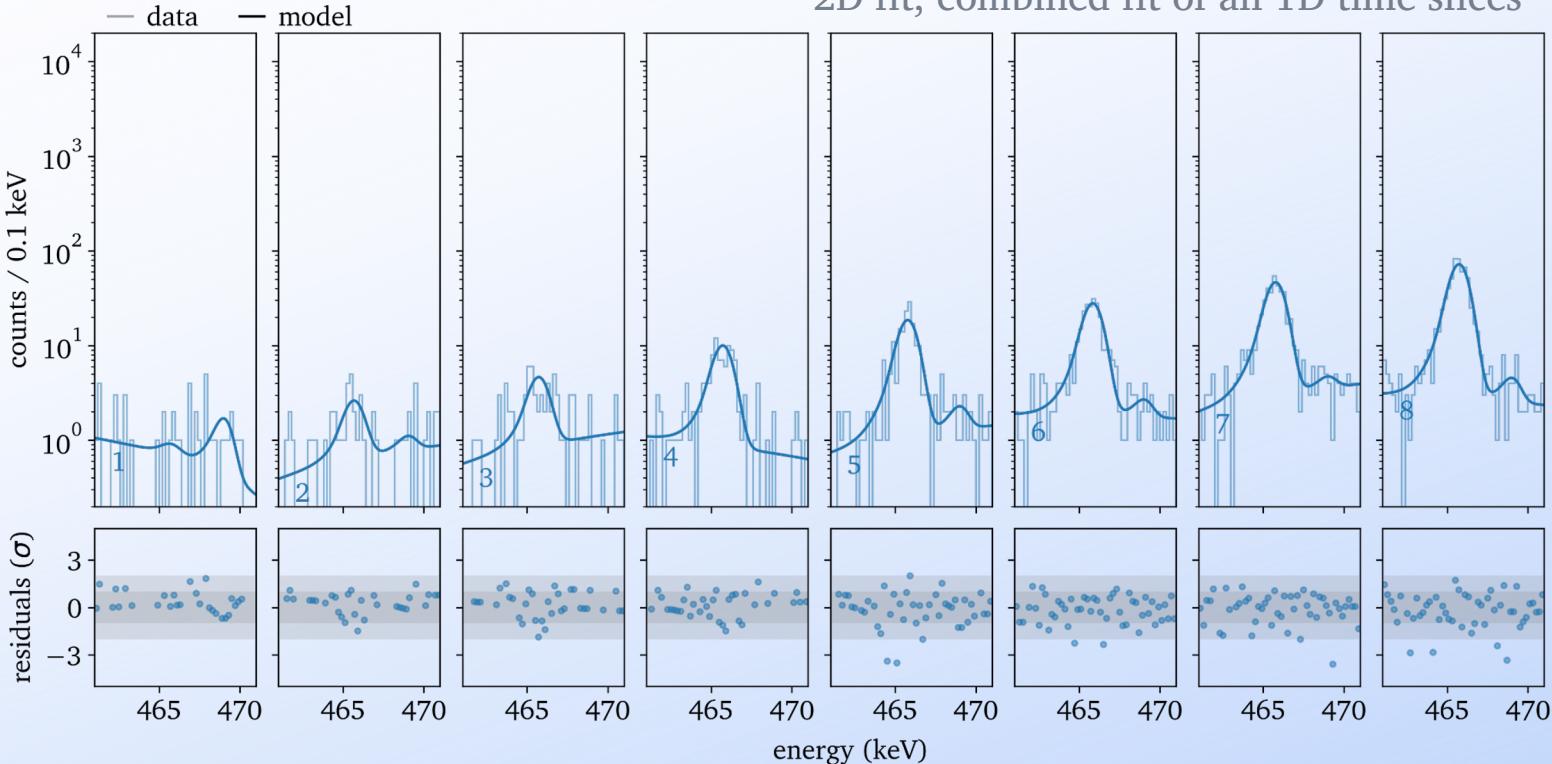
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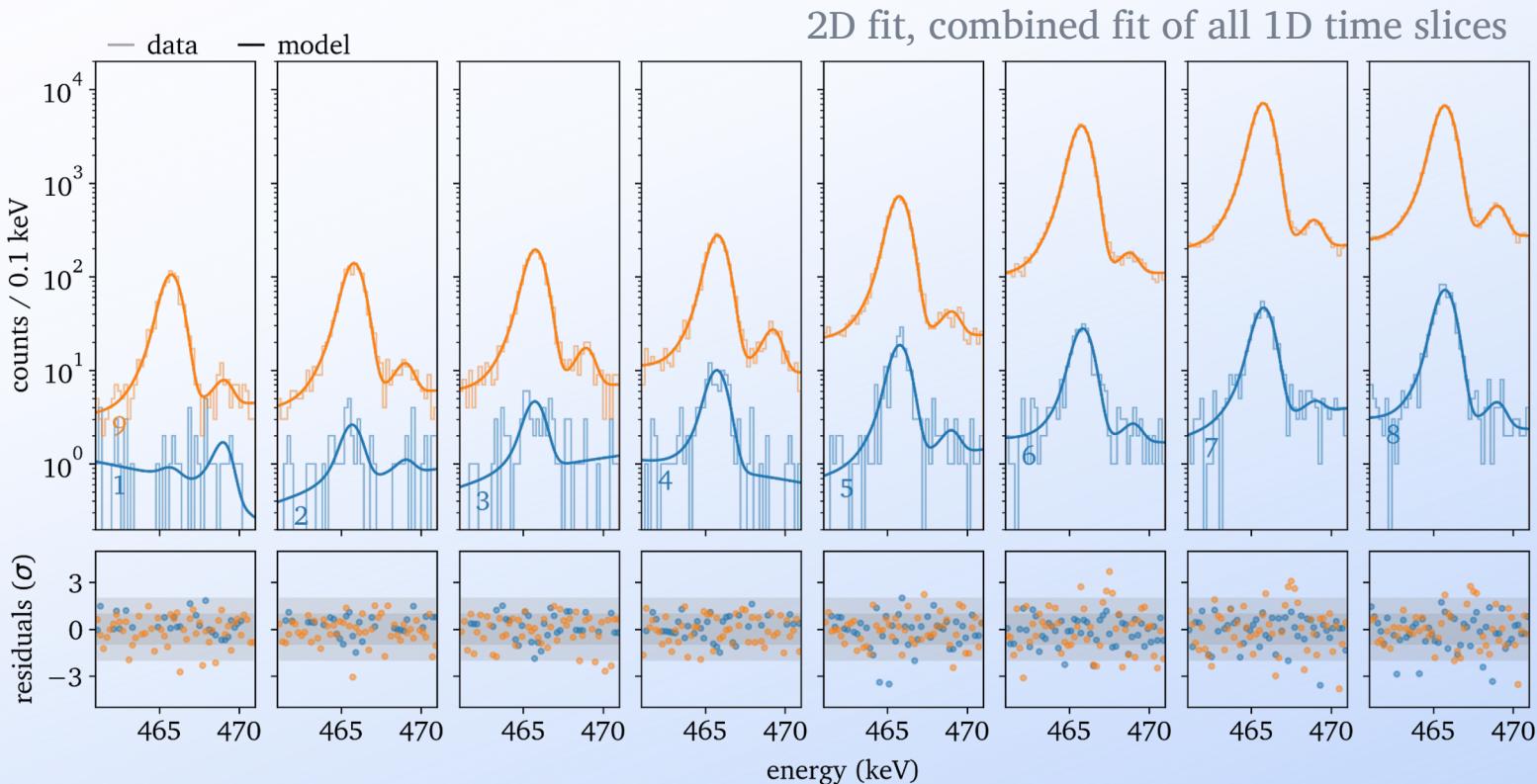


# ① Time profile extraction (intensities over time)

2D fit, combined fit of all 1D time slices

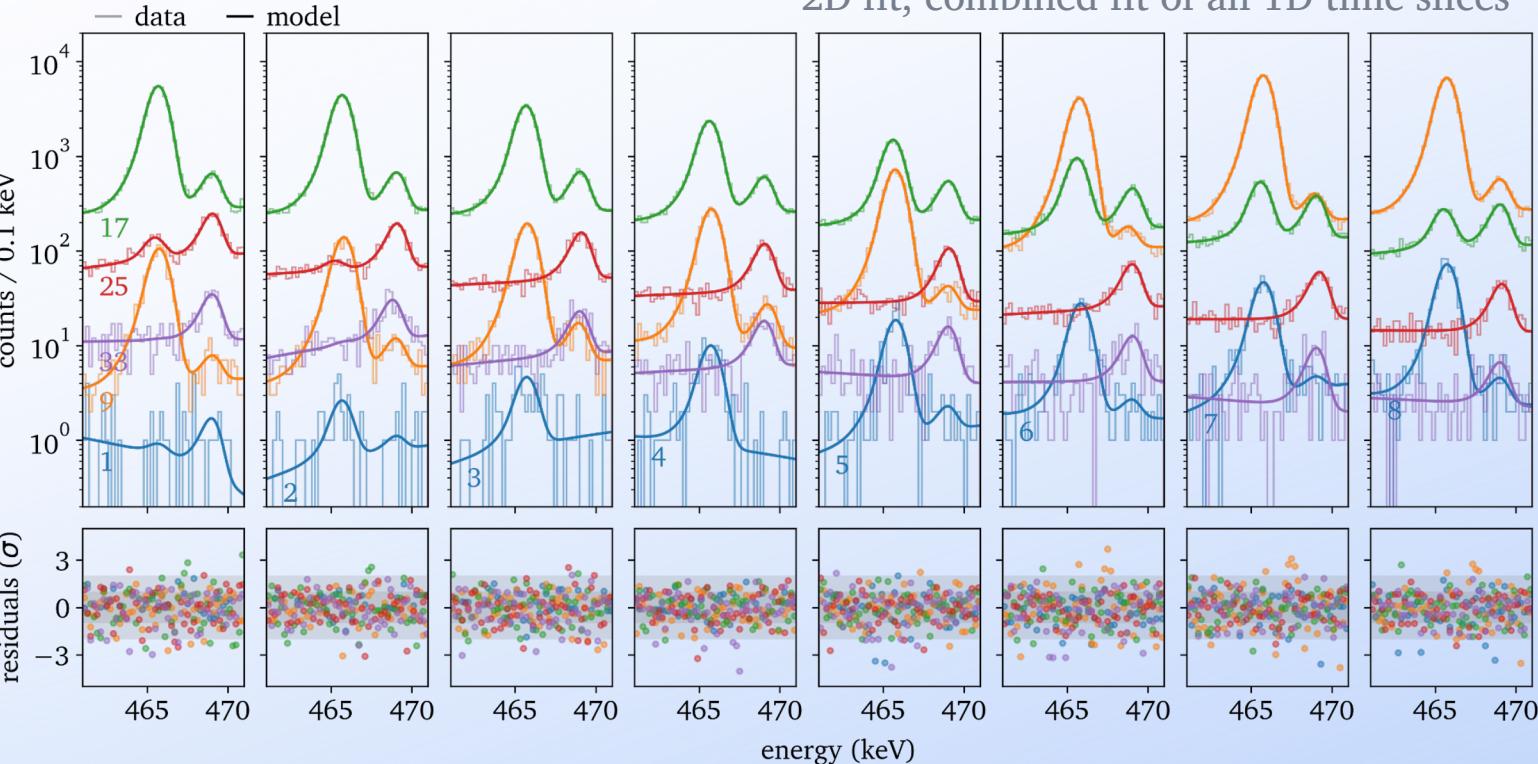


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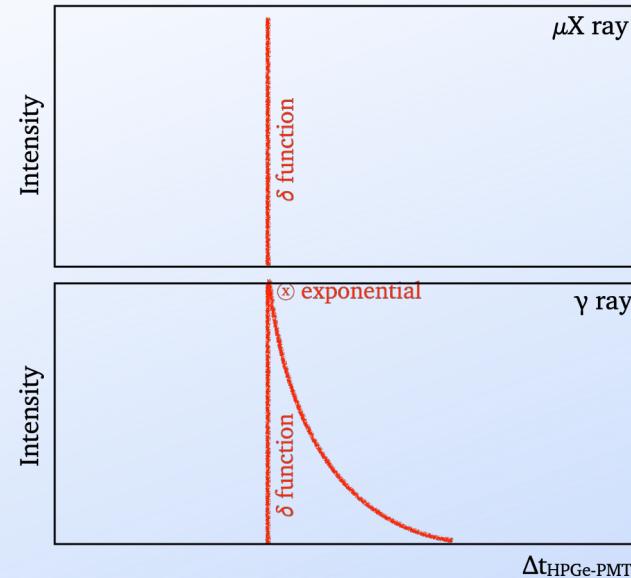
2D fit, combined fit of all 1D time slices



## ② Lifetime fit (muon lifetime $\tau$ )

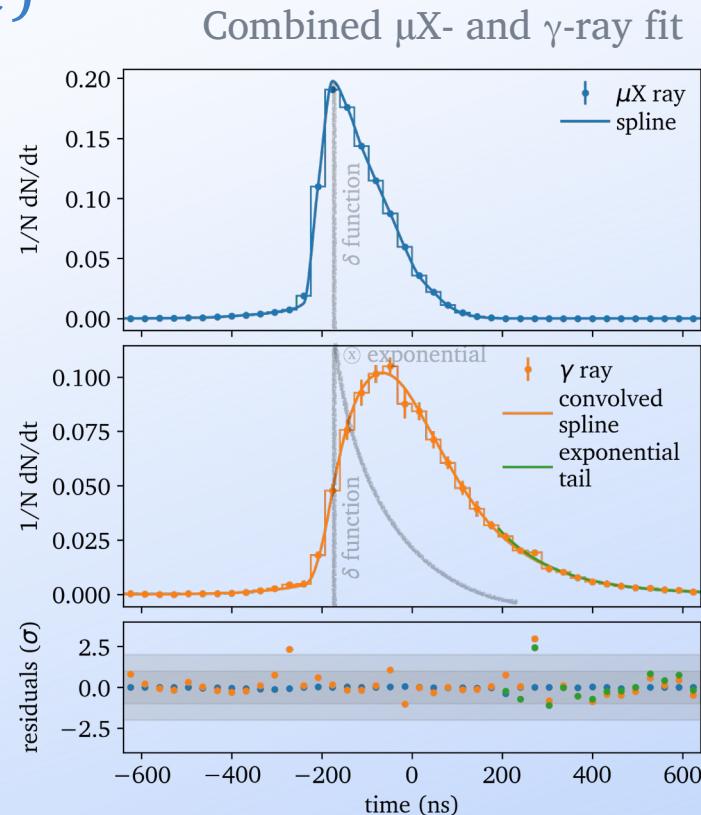
- $\mu X$  ray provides prompt response of the detector system,  $\gamma$  is convolution with exponential decay due to muon lifetime
- Prompt profile not trivial, use monotonic cubic spline
- Combined shape-only  $\chi^2$  fit using covariance matrix from ①
$$(138.9 \pm 1.3_{\text{stat}} \pm 3.5_{\text{syst}}) \text{ ns}$$
- Tail fit for comparison

Combined  $\mu X$ - and  $\gamma$ -ray fit



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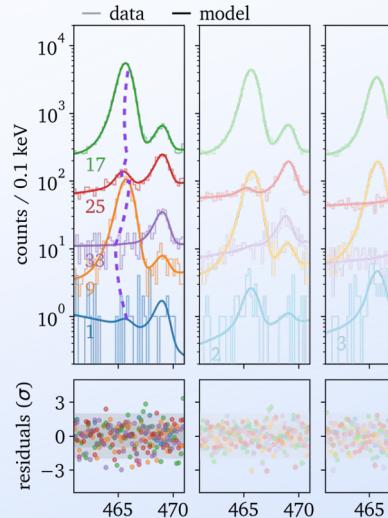


# Systematics

## A. Line position drift

Charge collection effect due to drift time selection

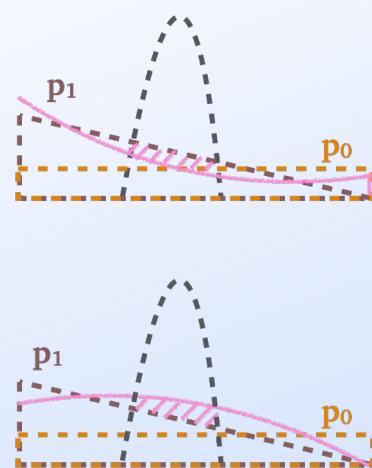
$\pm 0.7 \text{ ns}$



## B. Background shape

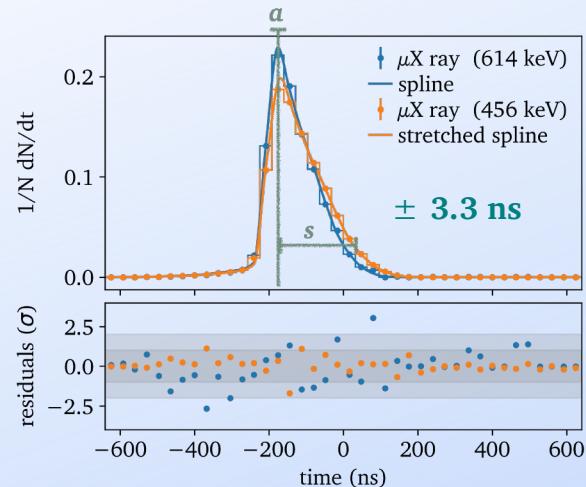
Over/under estimation of intensity due to background model insufficiencies

$\pm 0.9 \text{ ns}$



## C. Prompt timing energy-dependence

Stretched time response due to energy dependence

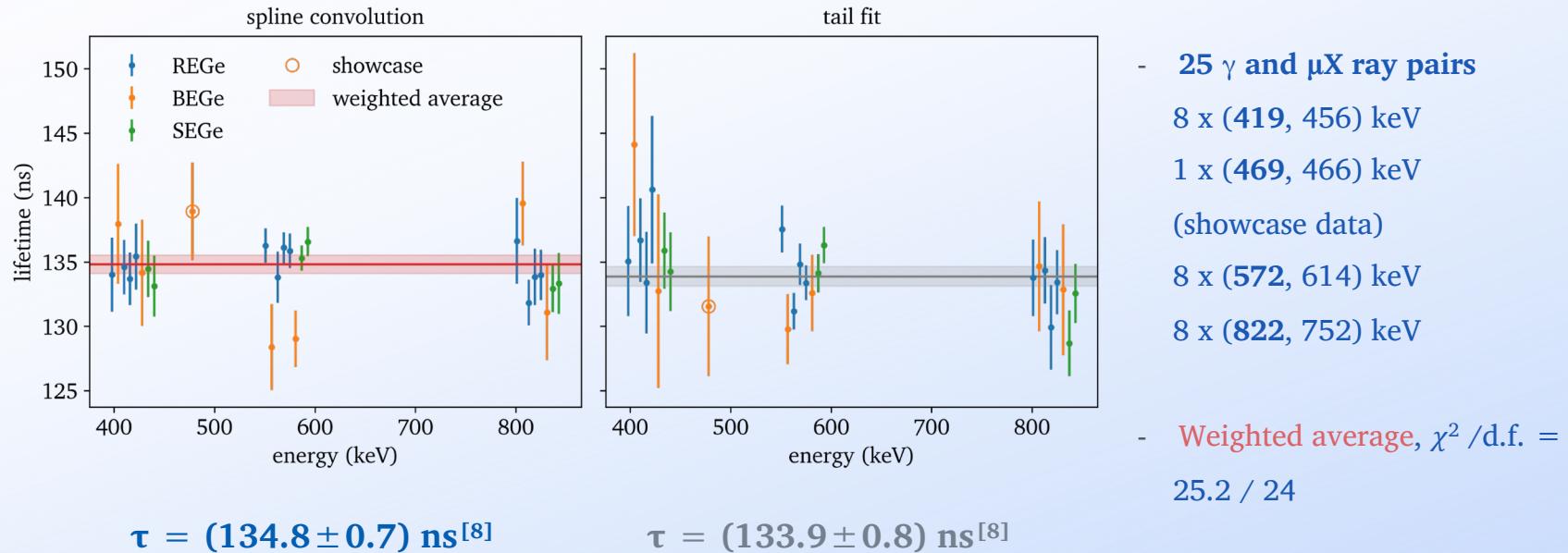


## D. Method uncertainty

$\pm 0.6 \text{ ns}$

Evaluated with toy Monte Carlo simulations

# Muon lifetime in $^{76}\text{Se}$ : new result!



\* This are models used to calculate  $\beta\beta$ -decay NMEs

\*\* Consistent with earlier capture-rate studies, where calculations match experiment without quenching [14, 15].

# Discussion

$$\frac{1}{\tau} = \mathcal{H}\Lambda_{dec} + \Lambda_{cap}$$



Experimental		Semi-empirical			Theoretical*		
This work <sup>[8]</sup>	Other work <sup>[9]</sup>	Primakoff <sup>[10, 12]</sup>	Goulard- Primakoff <sup>[11, 12]</sup>	Fujii- Primakoff <sup>[12]</sup>	QRPA <sup>[12]</sup>	pnQRPA <sup>[13]</sup>	
<b>134.8 ± 0.7</b>	148.5 ± 0.1	<b>135.1</b>	<b>115.0–135.2</b>	196.2	254.1	59.4	$g_A = 0.8$
					<b>134.5</b>	-	$g_A^{\text{free}} = 1.27^{**}$

[8] E. Mondragón, The MONUMENT Experiment: Ordinary Muon Capture for  $0\nu\beta\beta$ -decay Nuclear Matrix Elements, PhD Thesis, Technical University of Munich (2025)

[9] D. Zinatulina et al., Ordinary muon capture studies for the matrix elements in  $\beta\beta$  decay, Phys. Rev. C, vol. 99, no. 2, p. 024 327, (2019).

[10] H. Primakoff. Theory of muon capture. Rev. Mod. Phys., 31:802–822, (1959).

[11] B. Goulard and H. Primakoff, Nuclear muon-capture sum rules and mean nuclear excitation energies, Phys. Rev., C, v. 10, no. 5, pp. 2034–2044, (1974).

[12] F. Šimkovic, R. Dvornický, and P. Vogel, Muon capture rates: Evaluation within the quasiparticle random phase approximation, Phys. Rev. C, vol. 102, p. 034 301, 3 (2020).

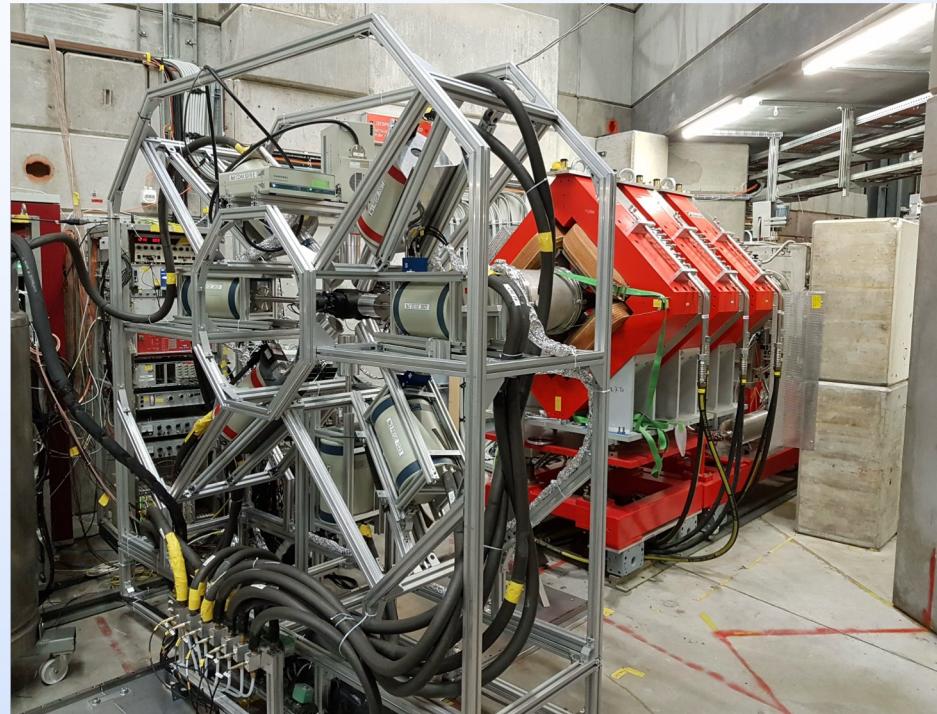
[13] L. Jokiniemi and J. Suhonen, Muon-capture strength functions in intermediate nuclei of  $0\nu\beta\beta$  decays, Phys. Rev. C, vol. 100, no. 1, p. 014 619, (2019).

[14] N. T. Zinner, K. Langanke, and P. Vogel, Muon capture on nuclei: Random phase approximation evaluation versus data for  $6 \leq Z \leq 94$  nuclei, Phys. Rev. C 74, 024326 (2006).

[15] T. Marketin, N. Paar, T. Niksic, and D. Vretenar, Relativistic QRPA calculation of muon capture rates, Phys. Rev. C 79, 054323 (2009).

# Conclusions

- MONUMENT measures OMC on  $\beta\beta$ -decay daughter isotopes to inform  $0\nu\beta\beta$ -decay NME calculations
- New experimental result for  $^{76}\text{Se}$  muon lifetime based on novel analysis method  
 $(134.8 \pm 0.7) \text{ ns}^{[8]}$
- Comparison with QRPA calculations indicate **no need for quenching**



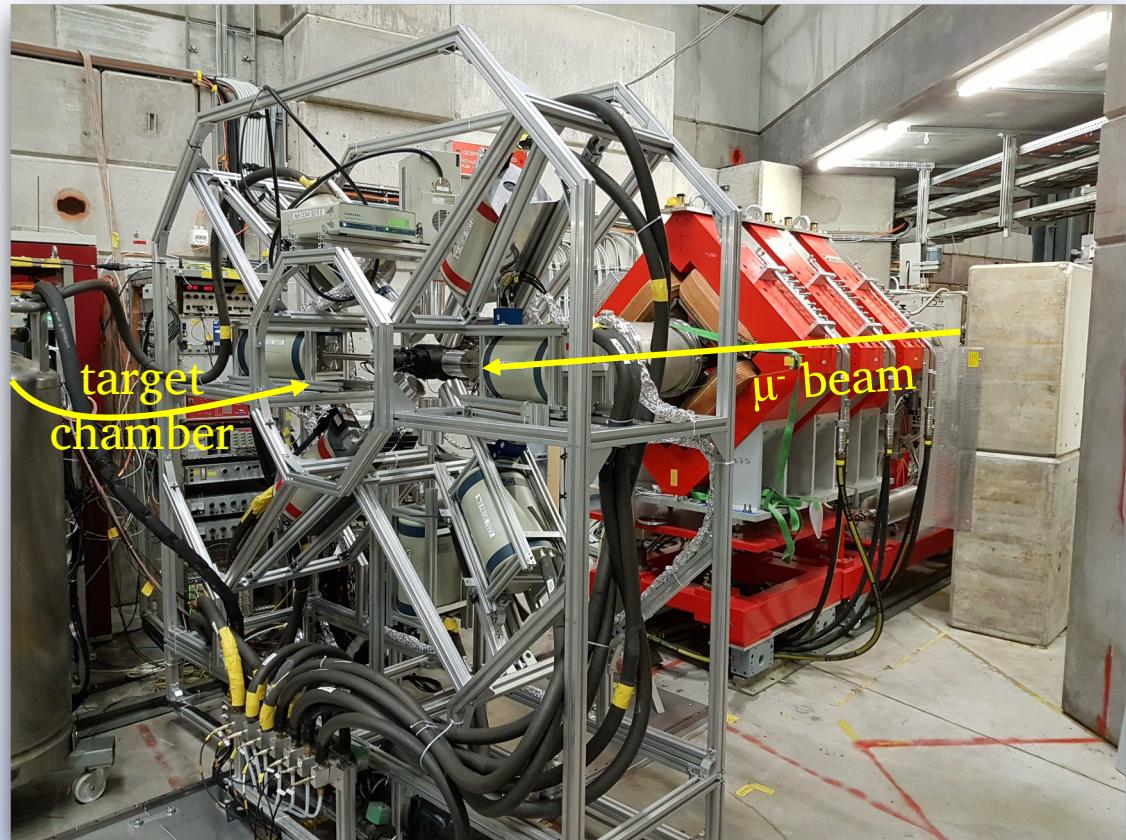
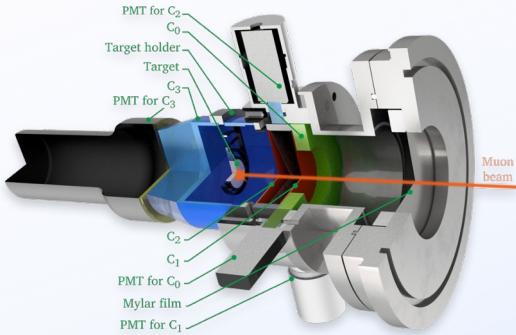
# Thanks !



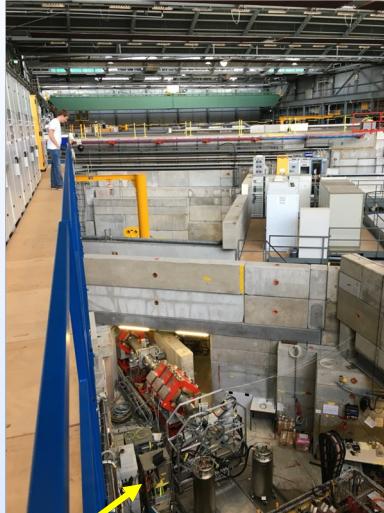
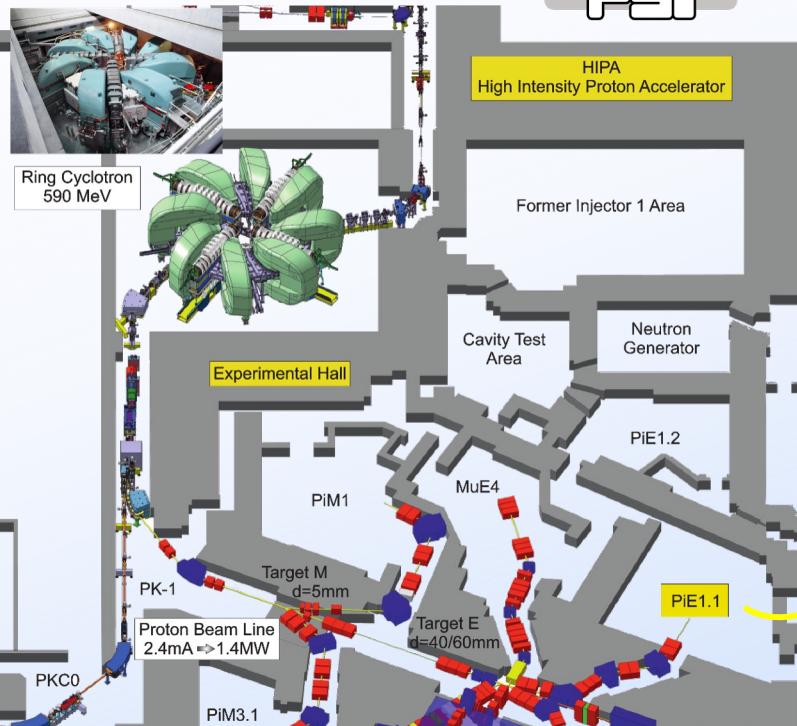


# B a c k u p

# Measurement



# Measurement

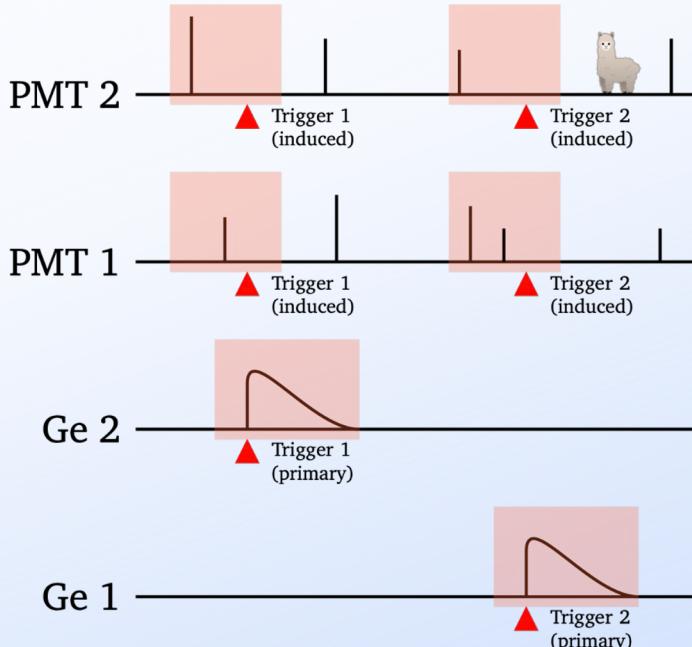


- Muon-beam momentum  
 $\sim 40 \text{ MeV}/c$
- Rate of stopped muons  
 $\mathcal{O}(10^4) \text{ Hz}$
- Rate in HPGe detectors  
 $\mathcal{O}(10^3) \text{ Hz}$

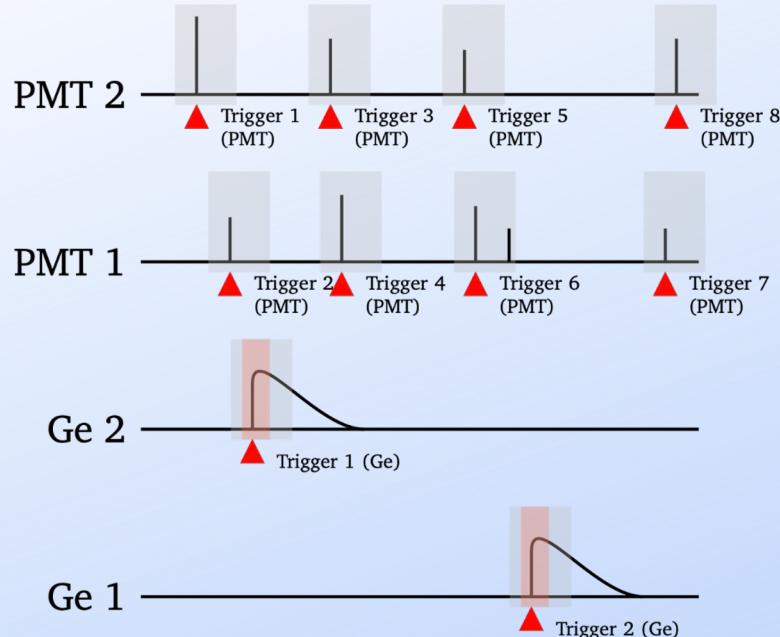


# DAQ

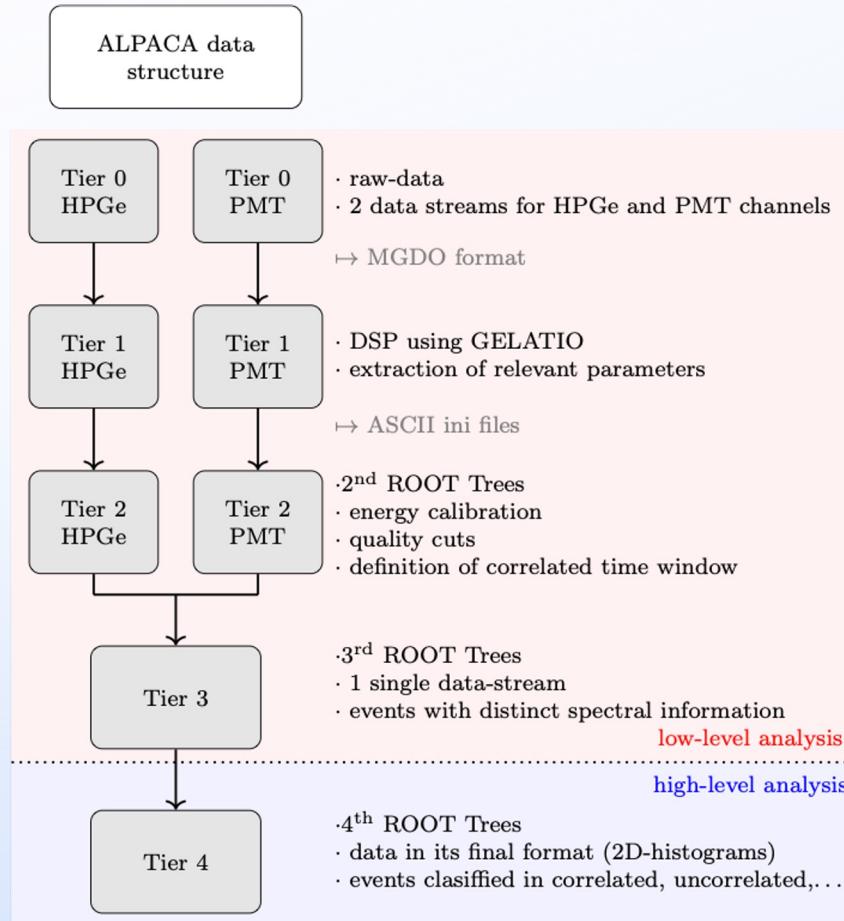
ALPACA



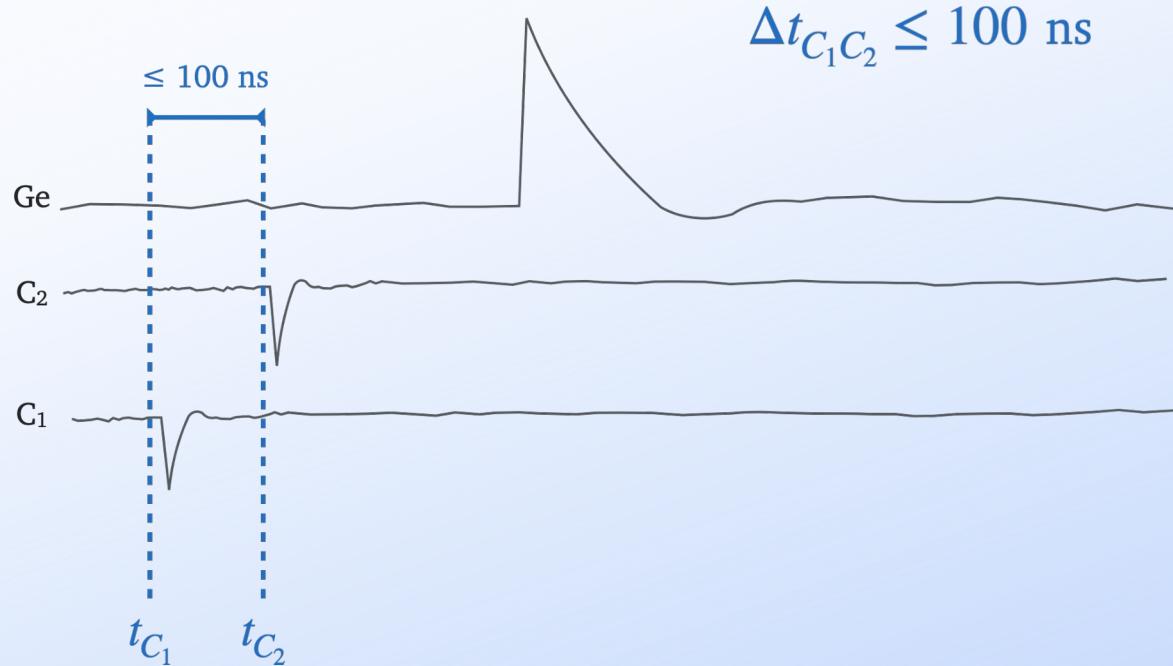
MIDAS



# ALPACA



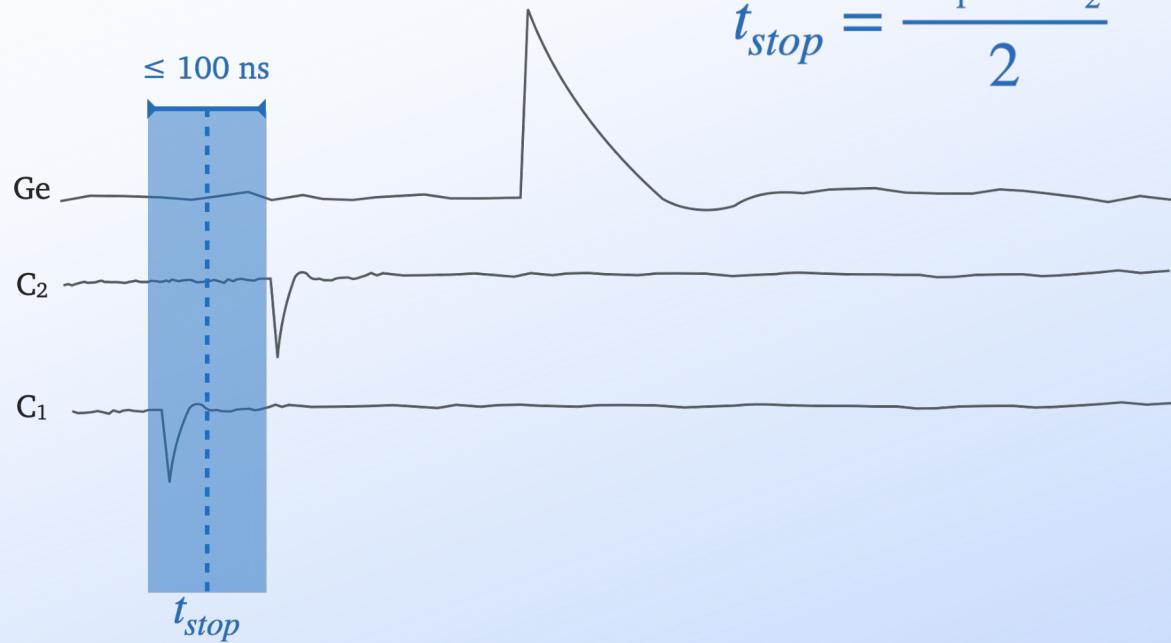
# ALPACA



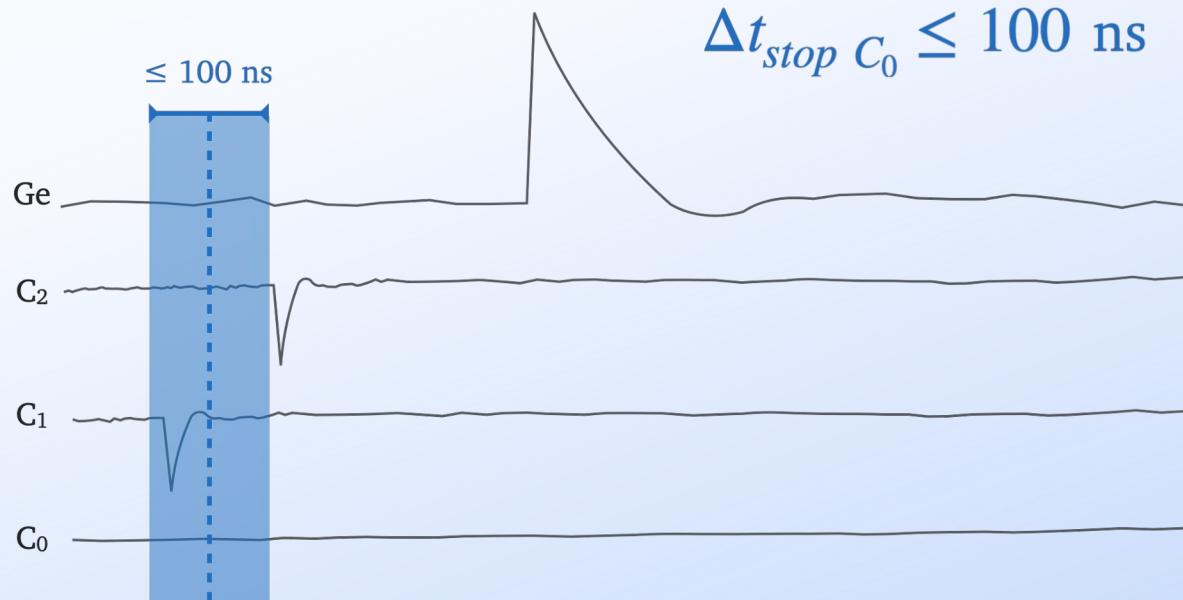
# ALPACA



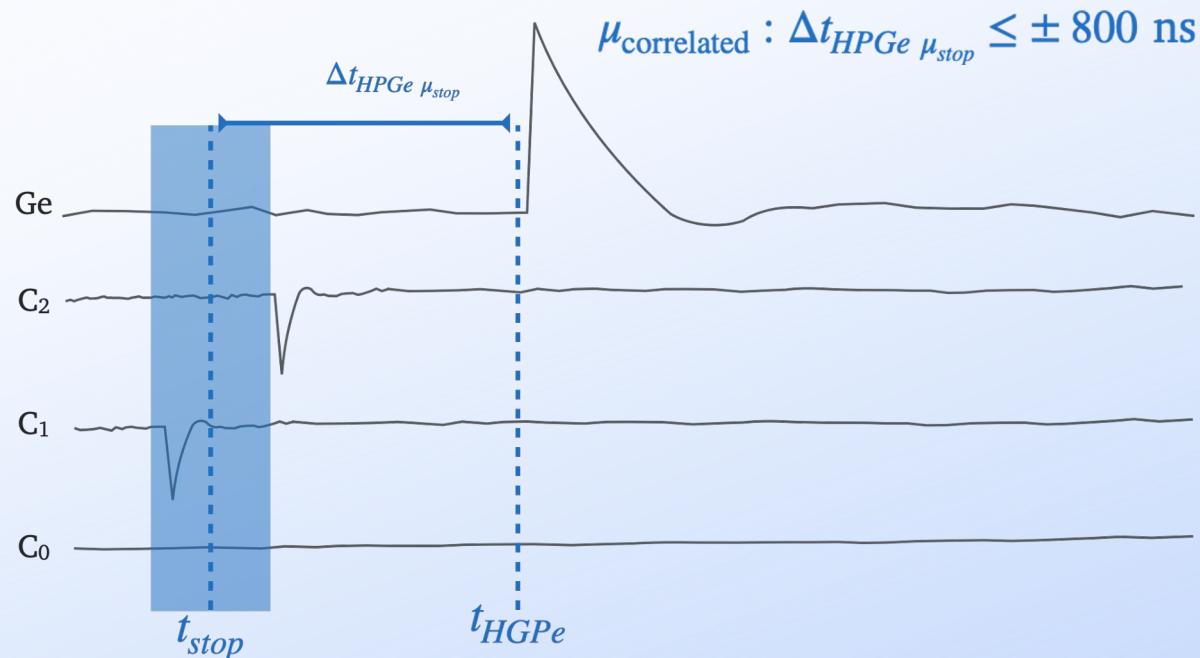
$$t_{stop} = \frac{t_{C_1} + t_{C_2}}{2}$$



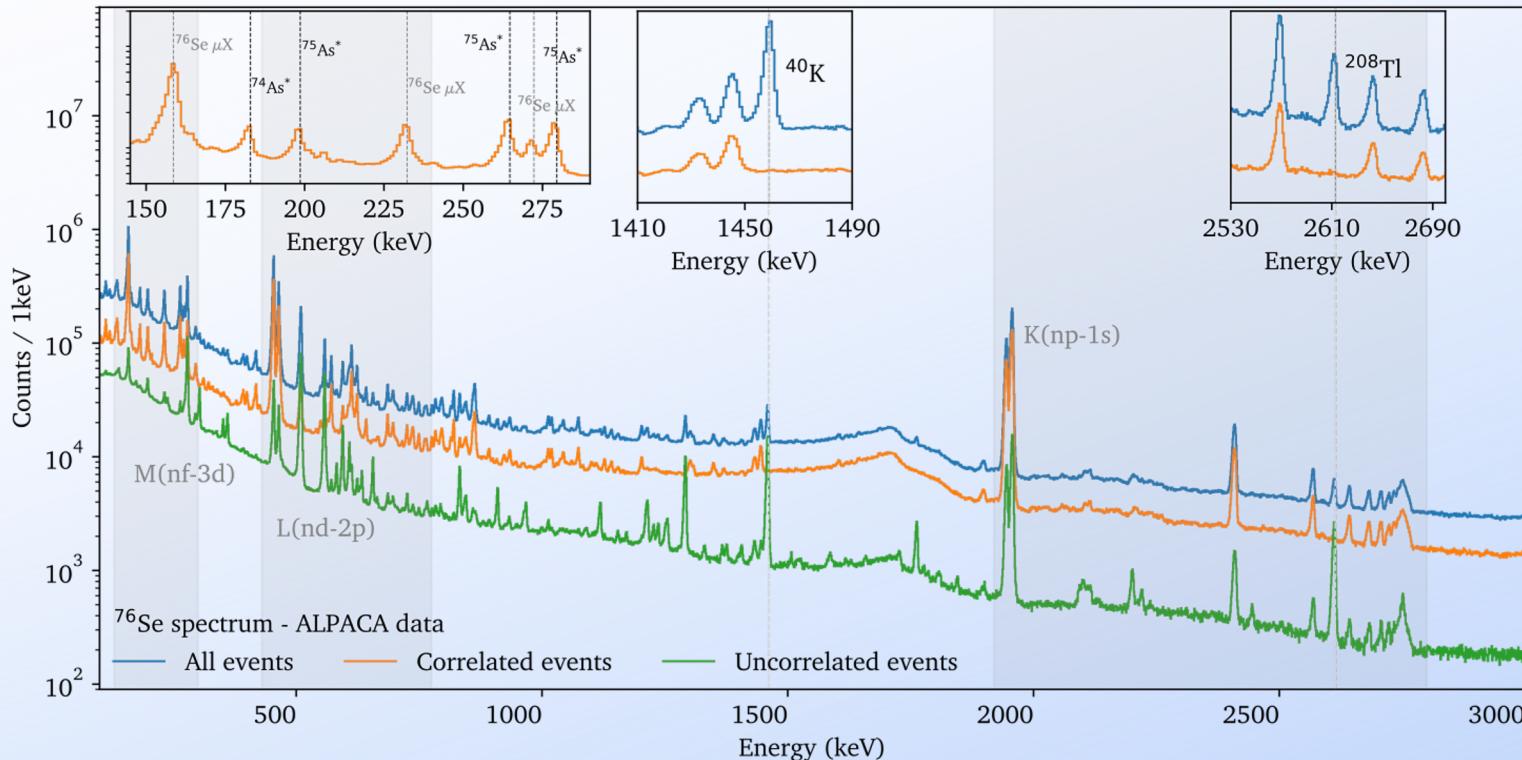
# ALPACA



# ALPACA



# Energy spectrum

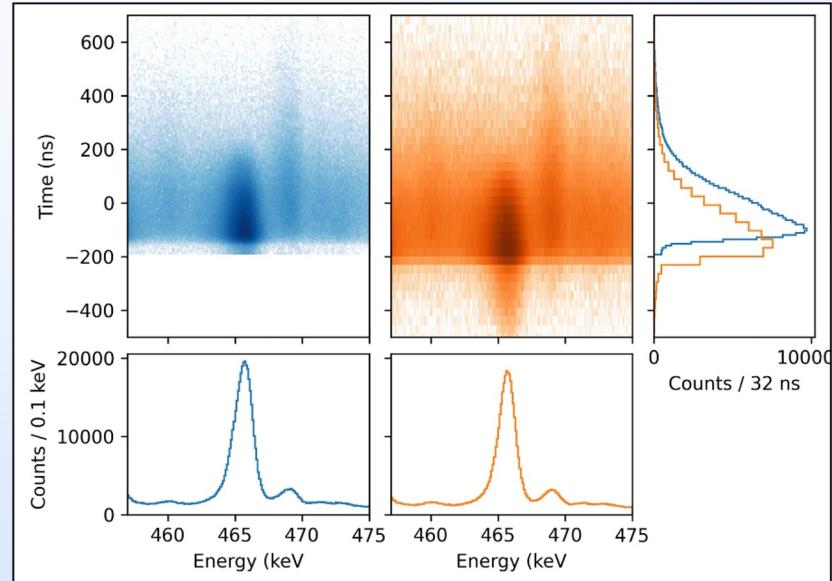


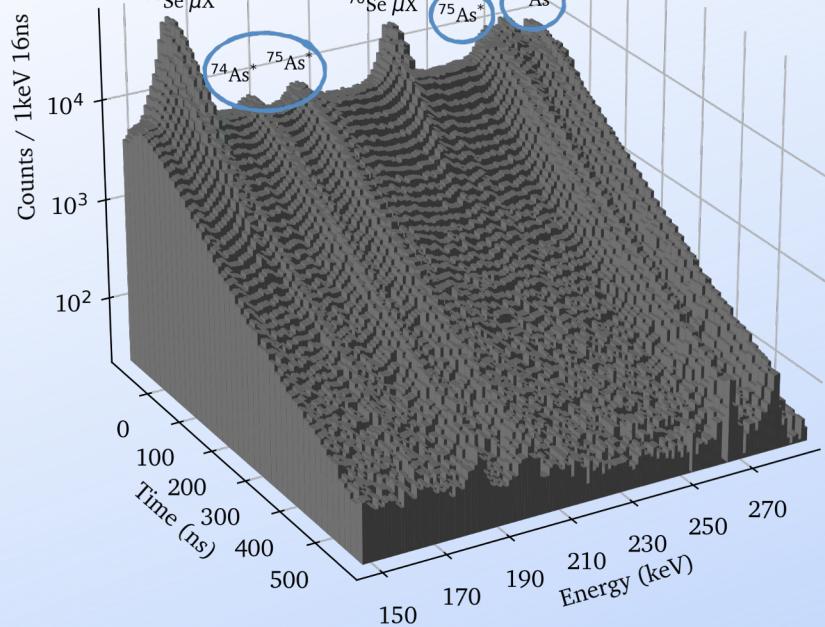
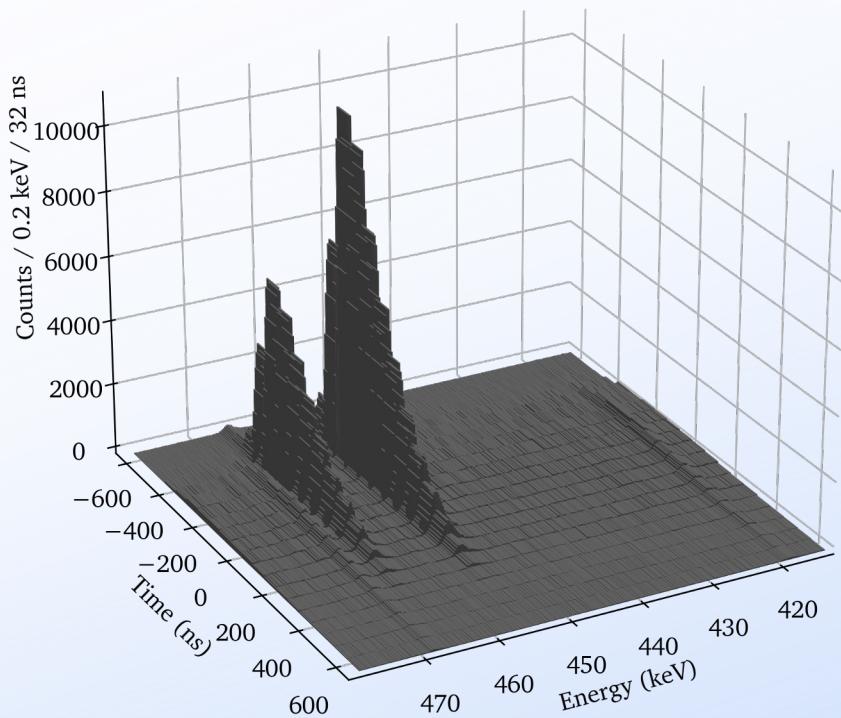
# Dataset

126 out of 132 h of beam-on data,

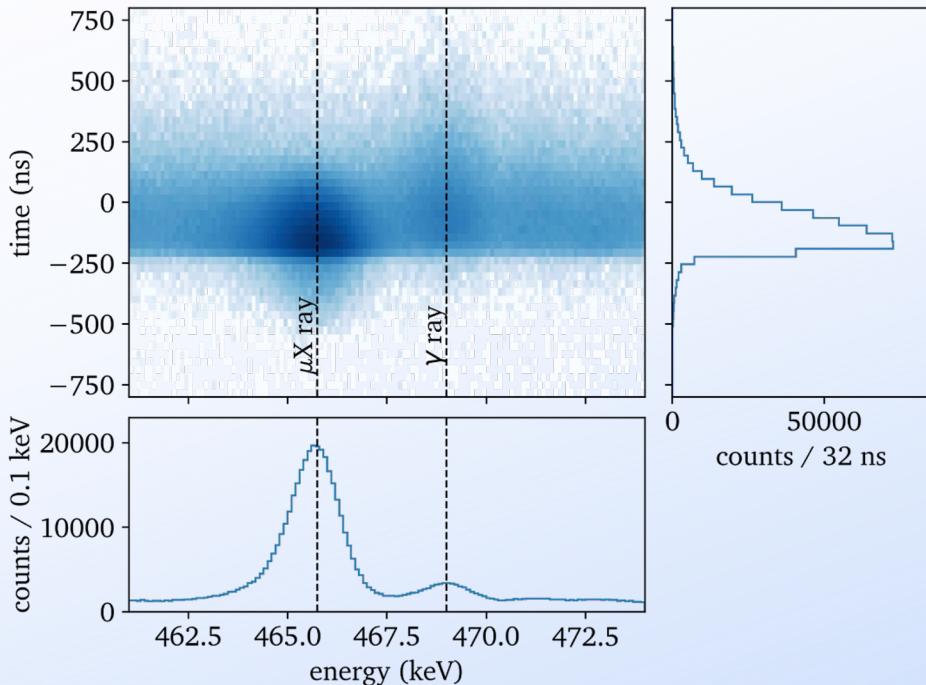
2D histograms mapping HPGe energy over time since last muon:

- Correlated events with  $\Delta t = \pm 800$  ns
- High-frequency HPGe waveforms (8ns sampling)
- Low-frequency PMT waveforms (32ns sampling)





# High-level analysis: muon lifetime



- BEGe detector #6
- Doublet of  $\mu X$  and  $\gamma$  ray at (466, 469) keV
- $\Delta t = \pm 640$  ns → **40 bins in time dimension**
- 10 keV with 0.2 keV binning → **50 bins in energy dimension**
- **2000 data points**



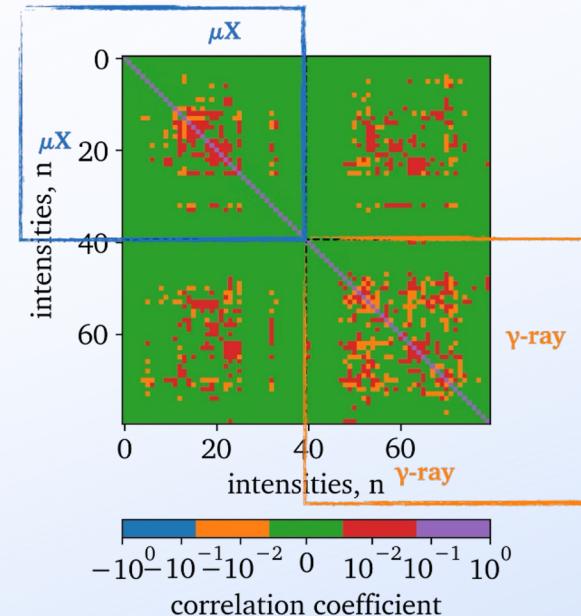
# ① Time profile extraction

- Combined maximum likelihood fit using **Poisson likelihood**
- Shared shape ( $\sigma, \alpha, \beta$ ) and position ( $\mu$ ) parameters per line, individual intensity ( $n_j$ ) and background ( $p_{0j}, p_{1j}$ ) parameters per time slice  $j$ , **168 free parameters**
- Gaussian pull terms for systematics, **160 constrained parameters\***

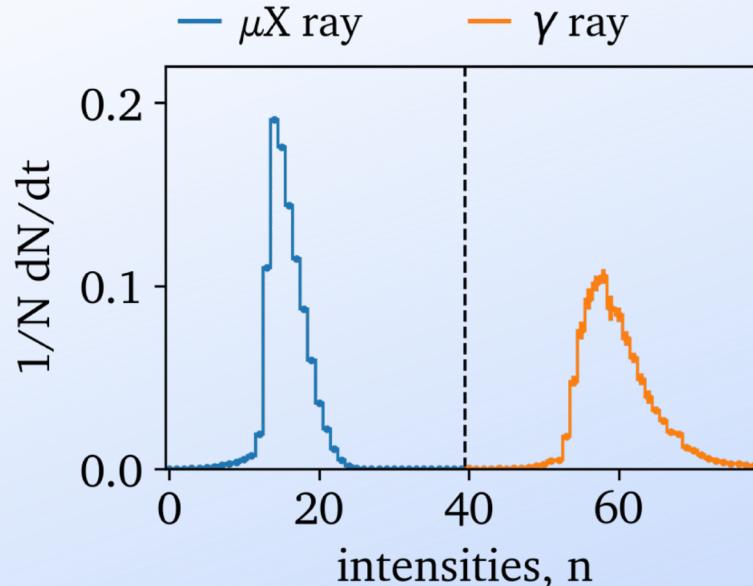
\*Discussed in Systematics



# ① Time profile extraction



Marginalised covariance matrix  $\Theta$  propagated  
to step ②, correlation not negligible, up to  
 $\mathcal{O}(10\%)$



1D histograms representing  $\mu X$ - and  $\gamma$ -ray intensities over time



# Systematics

- A. Line position drift (①, ①~②)
- B. Background shape (①~②)
- C. Prompt timing energy  
-dependence (②)

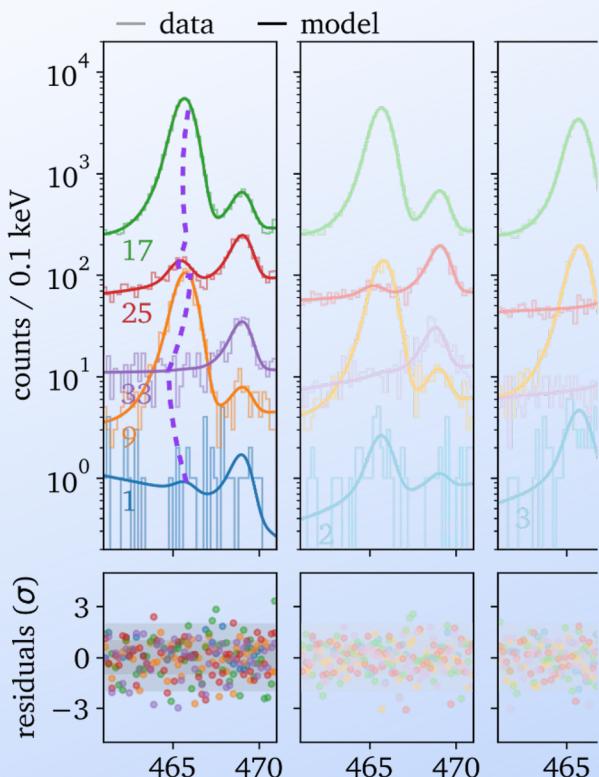


# A. Line position drift

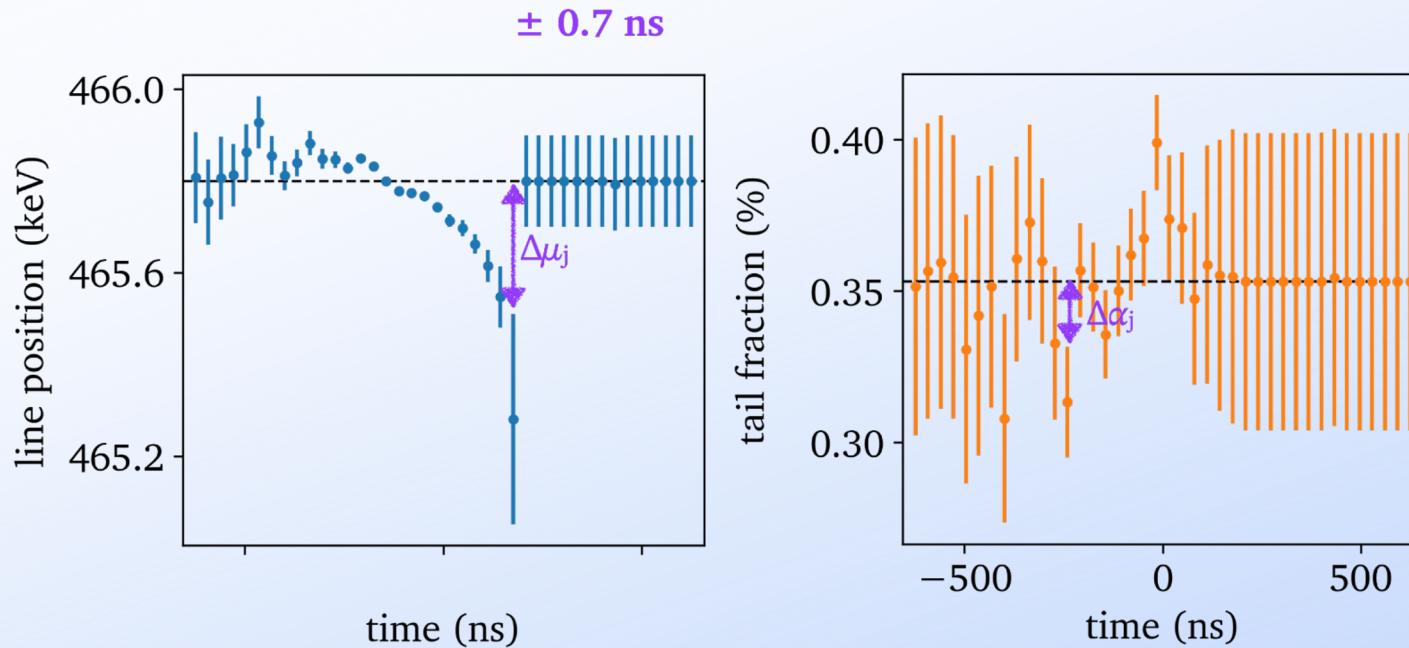
## Hypothesis:

Time slices correspond to HPGe detector **drift time selection**, later events are reconstructed with lower energies

- Include **additional parameters** ( $\Delta\mu_j$  and  $\Delta\alpha_j$ ), bound by **pull terms** (1 keV and 5%) ↗①
- Additional uncertainty for slices where no line is present (statistical uncertainty of background counts under each peak,  $\sqrt{p_0 \times FWTM}$ ) ↗①②

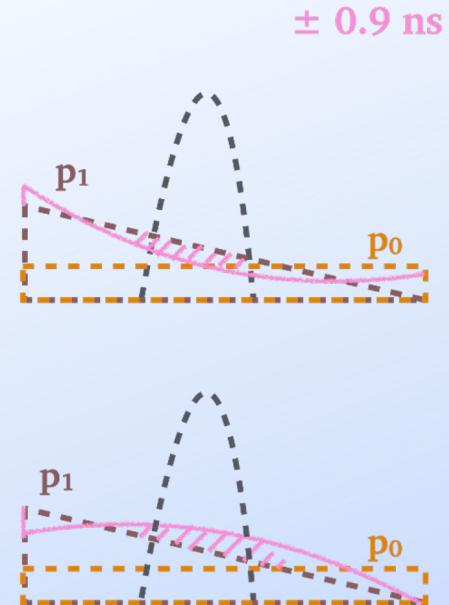


# A. Line position drift

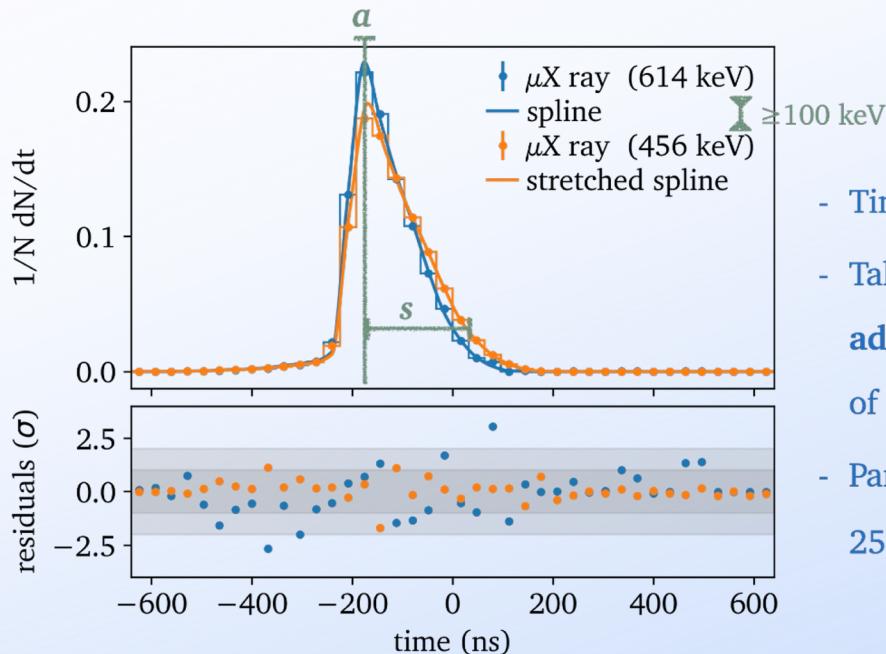


# B. Background shape

- Simple linear function might be insufficient in some cases
- Convex/concave background shape can lead to under/over-estimation of intensity
- Assume number of counts attributed to slope as uncertainty that is missed without higher order of polynomial ↪ ①~②



# C. Prompt timing energy-dependence

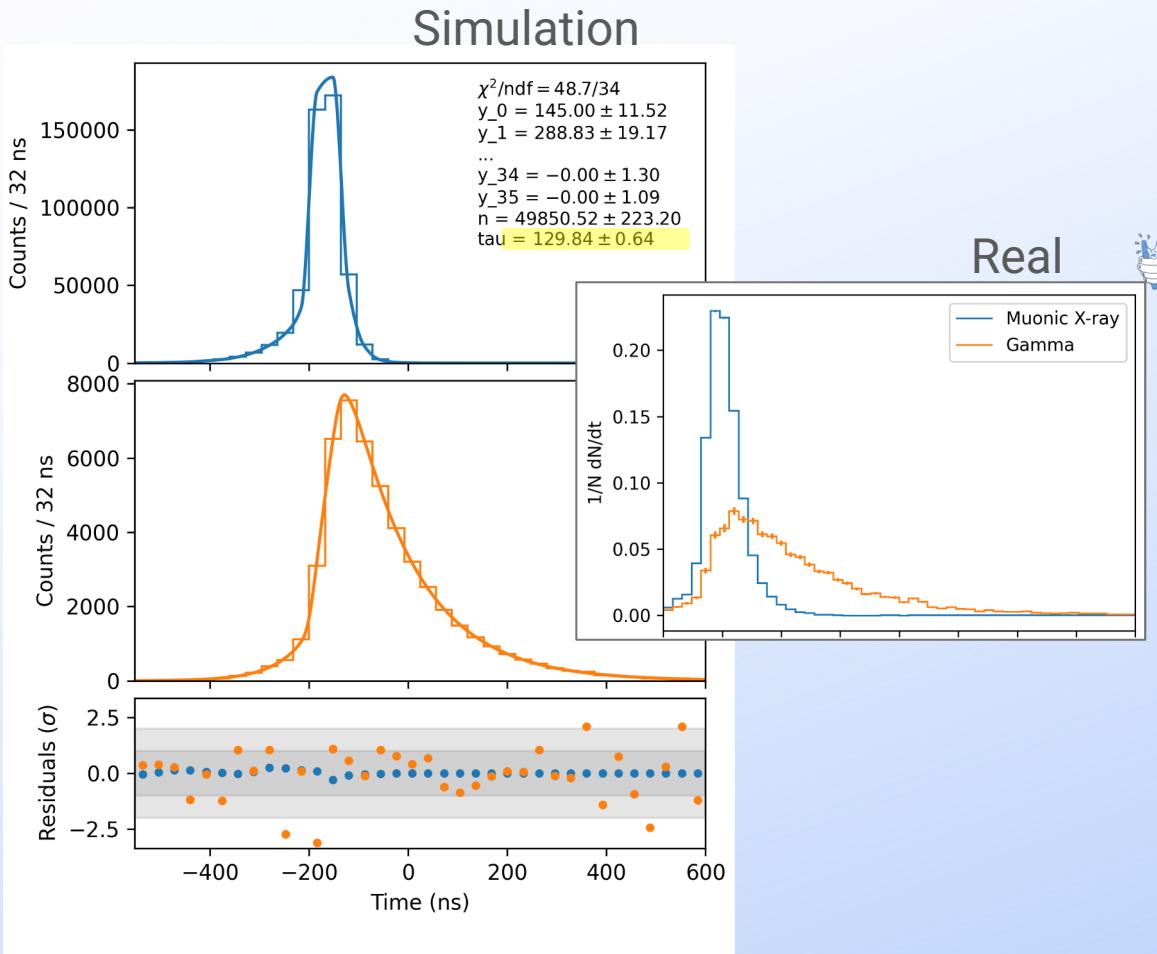


- Time response is energy and HPGe dependent
- Taken into account as **transformation adding 2 additional parameters**: stretch  $s$  from anchor  $a$  of spline before convolution
- Parameters constrained by **pull terms** (64 ns, 25%) based on  $\mu\text{X}$  rays  $\hookrightarrow$  ②

# Features

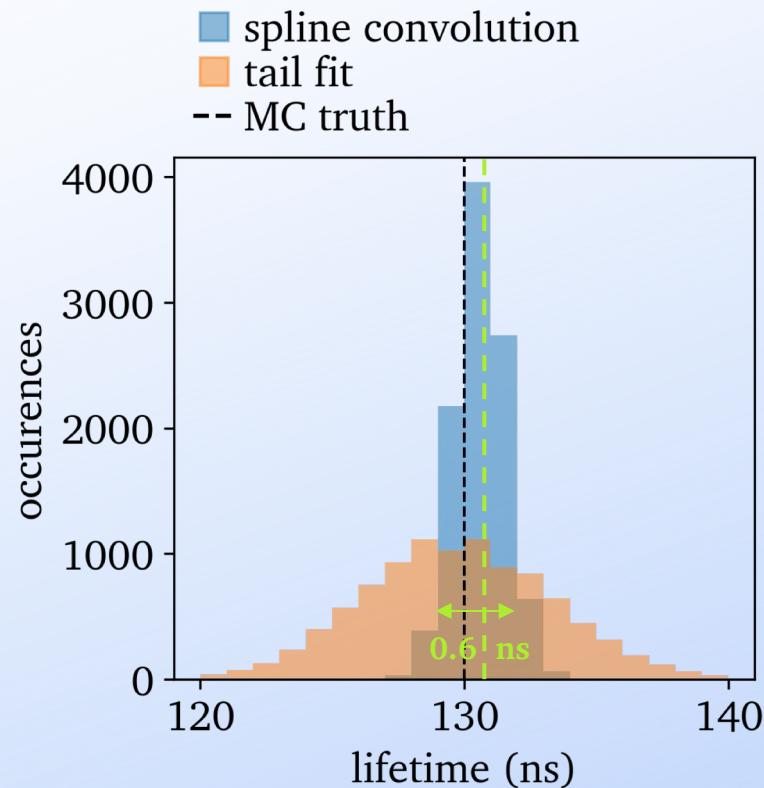
(Simulating detector 7 data...)

- **Asymmetric timing**  
modeled by two Gaussians  
with different central value  
and different left and right  
tail
- True Monte Carlo lifetime  
is 130 ns (feeding tau)

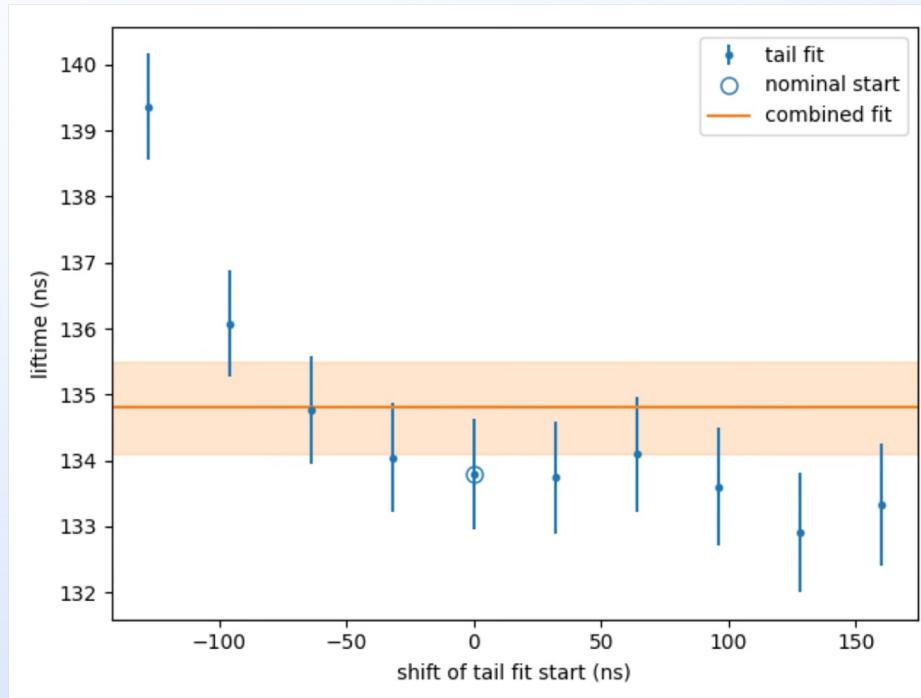


# Toy study

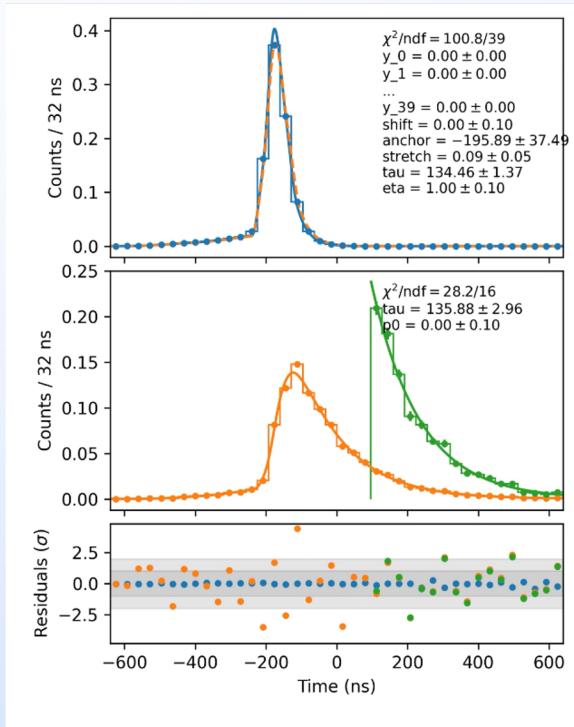
- Monte Carlo study
  - Generate time profiles that resemble the real dataset using asymmetric prompt timing distribution
  - Apply combined lifetime fit (and tail fit) method
- Median result differs from Monte Carlo truth, added as method uncertainty to final result



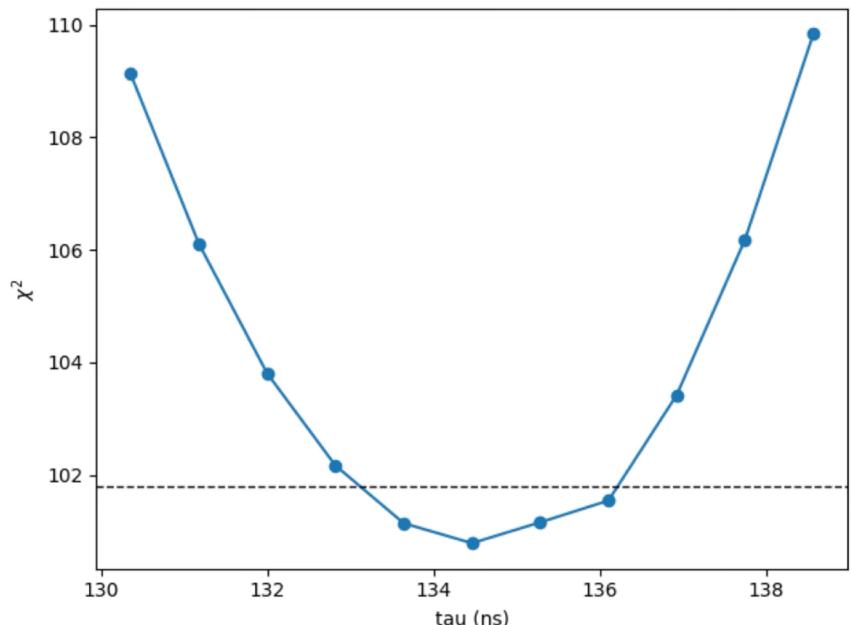
# Tail fit start dependence



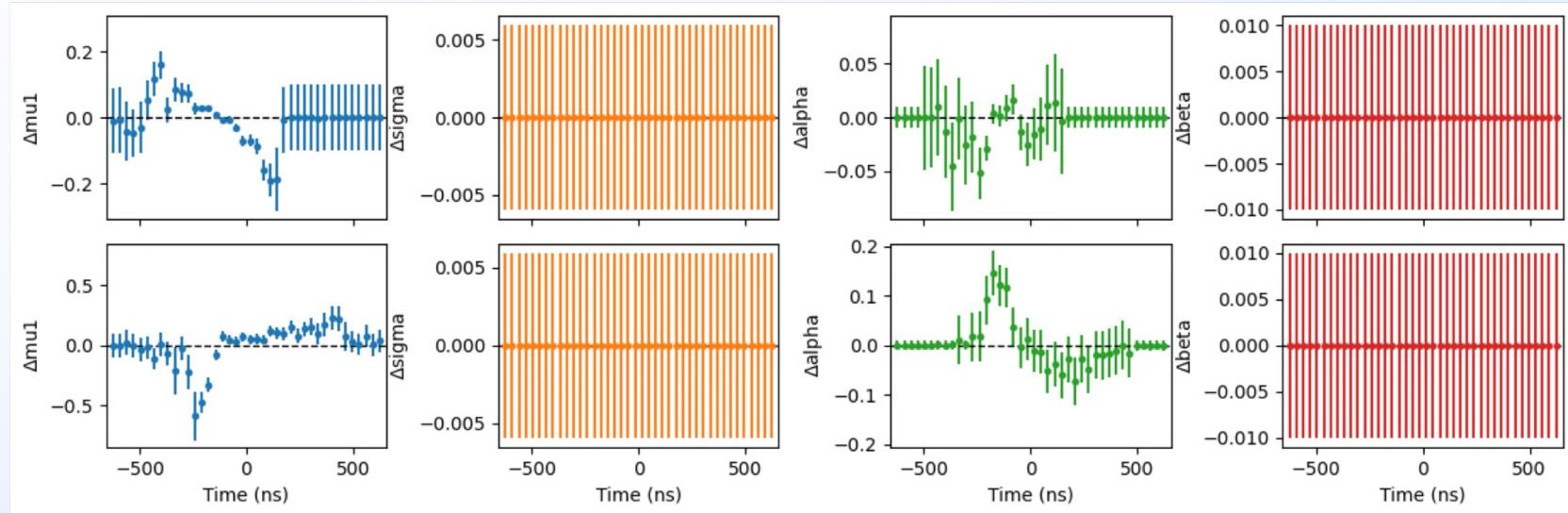
# Example of “bad $\chi^2$ -fit”



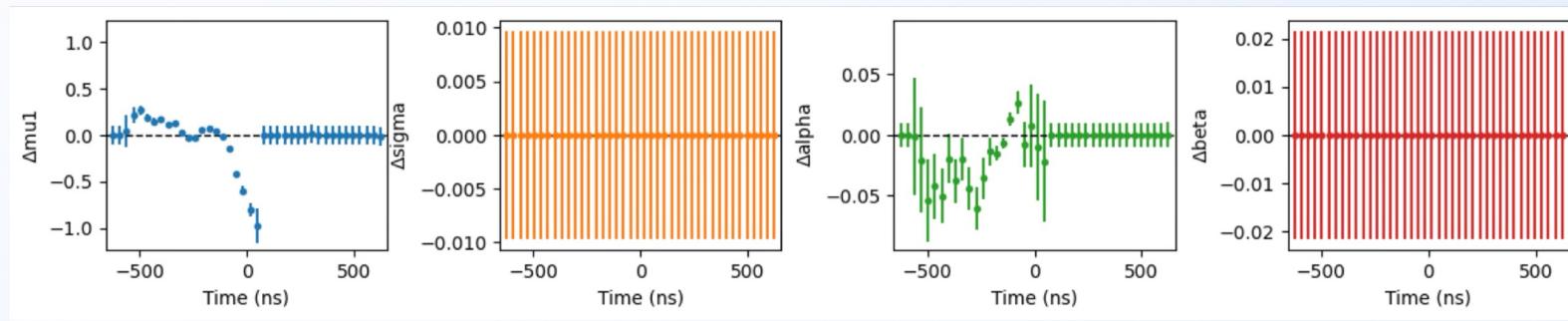
# $\chi^2$ profile



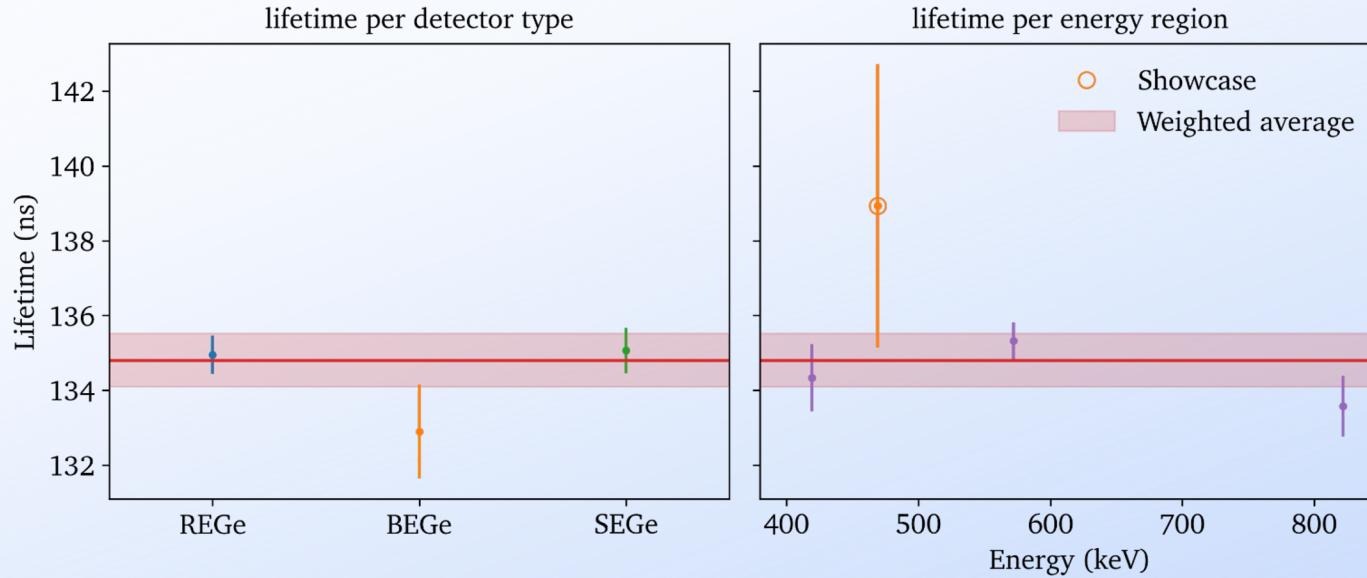
# $\mu$ and $\alpha$ change over time



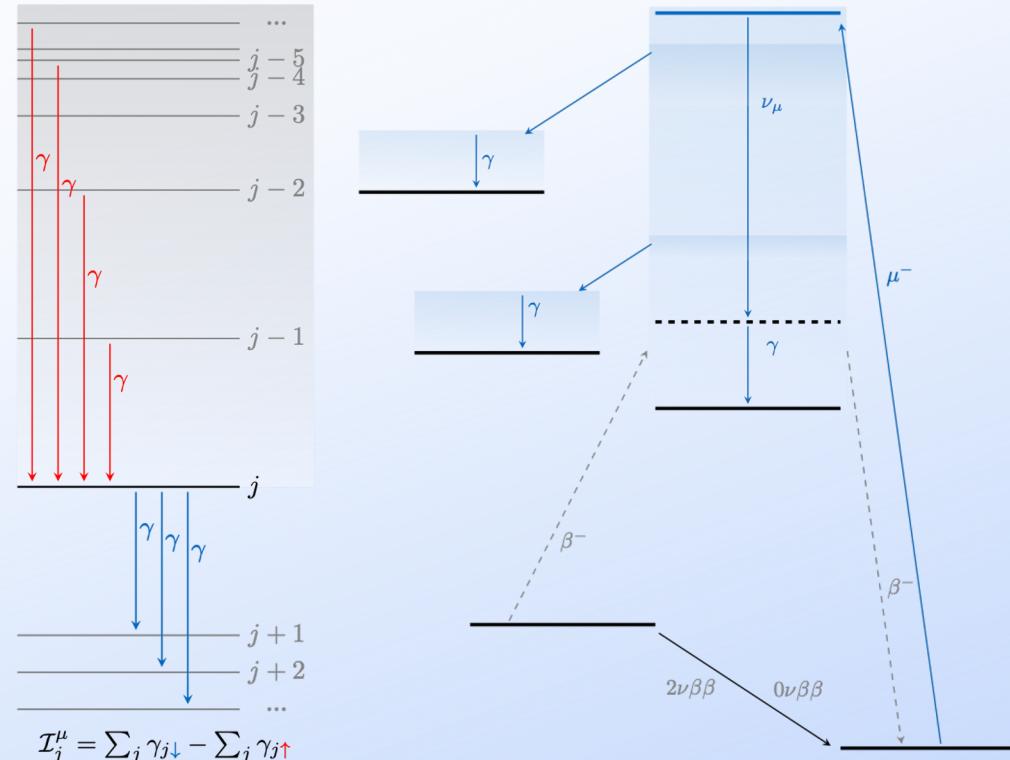
# $\mu$ and $\alpha$ change over time



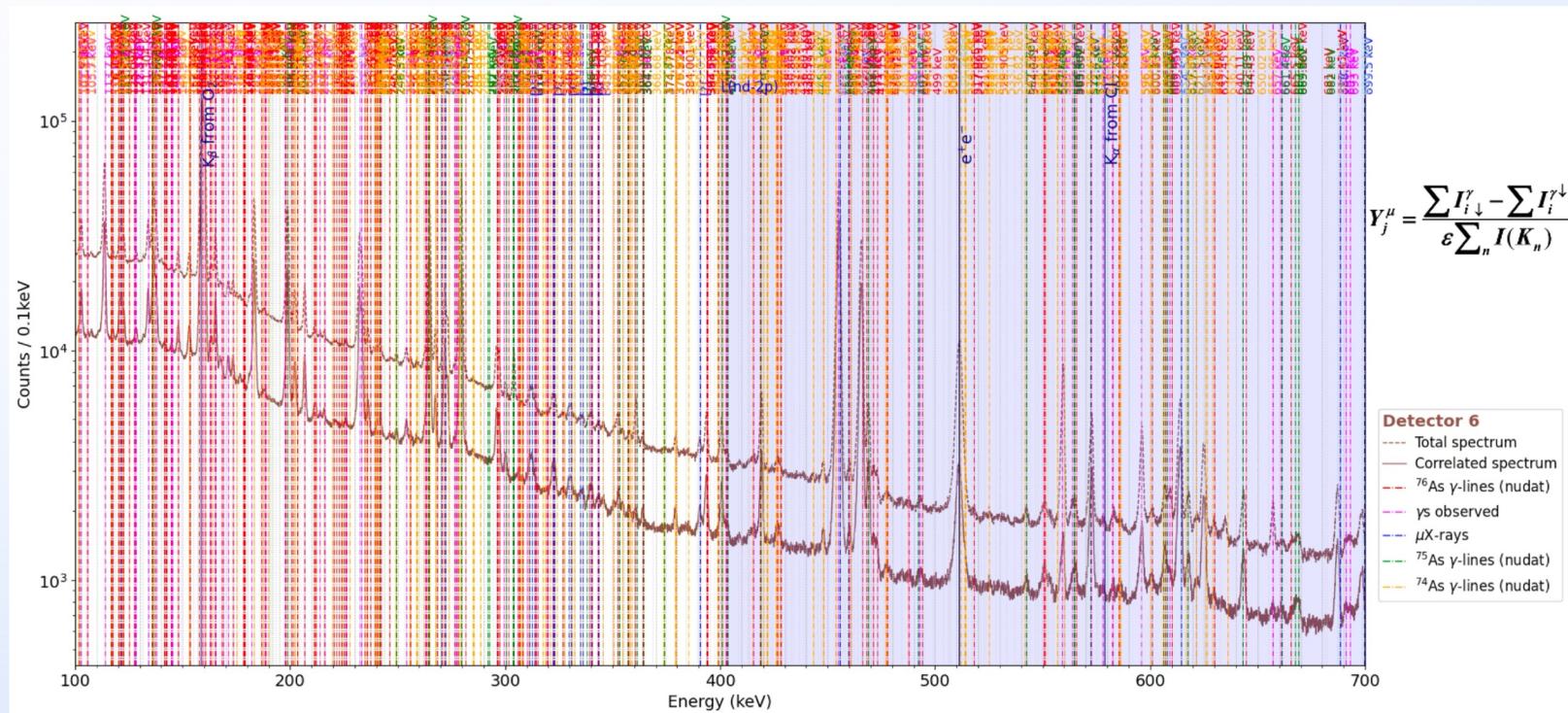
# Results: per detector / energy



# High-level analysis: strength functions



# High-level analysis: strength functions



# 499.6 keV-level

